

# Understanding the microstructural evolution of hypersaline cemented paste backfill with low-field NMR relaxation

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## Abstract

Cemented paste backfill (CPB) comprising mineral tailings, binders and mixing waters is an important potential support material in the mining industry. As the mechanical properties of CPB are significantly influenced by its microstructural characteristics the development of measurement tools to better understand its pore structure evolution is important for its increased utilisation. This study reports the application of low-field nuclear magnetic resonance (NMR) relaxation time measurements to characterise the microstructural evolution of CPB materials over 56 days of hydration, contrasting common tap water and hypersaline water (~22 wt% salt) as mixing waters. Distinct NMR relaxation time populations were evidenced within each CPB sample, revealing the presence of both capillary ( $T_{1,2} \approx 10$  ms) and gel pore water ( $T_{1,2} \approx 300 - 500$   $\mu$ s), with time-dependent relaxation measurements facilitating characterisation of capillary pore structure evolution over the hydration period assessed. Hypersaline samples demonstrated a time-lag in this measured capillary pore evolution, relative to those hydrated with tap water, while pore structure evolution rates were observed to increase with increased CPB binder content. Further, both  $T_1$  and  $T_2$  NMR relaxation times were found to correlate with the uniaxial compressive strength of the CPB materials investigated, facilitating the formulation of a predictive correlation function between NMR relaxation characteristics and mechanical properties.

## Keywords

Cemented paste backfill; Tailings Management; Nuclear Magnetic Resonance; Microstructure

## 1 **Highlights**

- 2   ▪ Microstructural evolution of CPB, prepared with tap and hypersaline water, is monitored using low-field
- 3   NMR relaxometry.
- 4   ▪  $T_1$  and  $T_2$  NMR relaxation measurements compared with mechanical strength via UCS tests.
- 5   ▪ Hypersaline mixing water results in slower structural evolution and lower mechanical strength.

6

## 7 **Introduction**

8 It is estimated that the production rate of mine tailings ranges between 5 and 7 billion tonnes per year worldwide  
9 [1]. While mine tailings are often discharged into tailings ponds, the emergence of cemented paste backfill  
10 (CPB) technology has the potential to substantially alter and enhance the role of tailings in the mining industry  
11 [2]. CPB comprises three main components, namely dewatered mine tailings (70-85 % solids by weight),  
12 mixing water and hydraulic binders (3-7 % by paste weight), which may include Ordinary Portland Cement  
13 (OPC), fly ash, and ground granulated blast furnace slag; these components combine via hydration reactions to  
14 form a complex porous structure which may be utilised as a passive support material within underground mining  
15 operations [3].

16 It is well-known that mixing water chemistry, including acidity and ionic concentrations, can impact the  
17 mechanical properties of hydrated CPB materials [2,4]. As access to low-salinity water in many mining  
18 operations is limited, and the local source water typically hypersaline, it is therefore of significant interest to  
19 determine the influence of hypersaline mixing water on the evolution of hydrated CPB materials. As such, in  
20 the present study we compare the effects of hypersaline water (~22 wt% salt) obtained from a Western  
21 Australian mine site, combined with mine tailings from the same site, against the effects of tap water on both  
22 the microstructural and mechanical strength evolution of the resultant CPB.

23 A number of recent studies have investigated the relationship between the microstructure of next-generation  
24 cementitious materials and the resulting mechanical properties. For example, Burciaga-Diaz *et al.* contrasted  
25 the compressive strength of alkali-activated slag pastes with solid state  $^{29}\text{Si}$  and  $^{27}\text{Al}$  NMR spectroscopy,  
26 facilitating quantification of the hydration products formed and their association with material strength [5]. Ma

1 *et al.* applied a similar approach to fly ash cement pastes, evidencing compressive strength enhancements which  
2 accompany Si/Al substitution reactions within the hydration products in the presence of an organic activator  
3 [6]. Fridjonsson *et al.* were the first to monitor the pore size evolution of CPB samples during their hydration  
4 using NMR, revealing through the application of nuclear spin relaxation measurements both a reduction in pore  
5 size during the hydration process, and a scaling relationship between pore size and material permeability [7].  
6 Sun *et al.* studied the evolution of CPB porosity under uniaxial compression via X-ray CT analysis [8]. This  
7 study sequenced CPB failure into four stages, namely (i) a no microcrack region; (ii) initiation and aggregation  
8 of microcracks; (iii) connection of microcracks; and (iv) formation of a macroscopic fracture region, and further  
9 showed that the CPB materials investigated displayed tensile and shear failures during early and middle-to-late  
10 stages of uniaxial compression, respectively. Furthermore Liu *et al.* studied CPB using both NMR and SEM to  
11 investigate the relationship between uniaxial compressive strength (UCS) and CPB pore characteristics,  
12 observing an exponential decrease in UCS with increasing porosity [9].

13 In the current study the results of low-field nuclear magnetic resonance (NMR) relaxation measurements are  
14 contrasted with UCS analysis to monitor the compressive strength and pore size evolution of CPB samples  
15 prepared with both tap and hypersaline mixing waters. A significant advantage of using low-field NMR is that  
16 it provides a non-destructive method for the characterisation of porous media [10]. As such, it offers  
17 opportunities for the development of robust approaches for monitoring CPB samples under early hydration  
18 conditions without the requirements for sample modifications, such as solvent exchange or oven drying, which  
19 may damage the material microstructure [11,12]. Indeed, as the longitudinal and transverse NMR relaxation  
20 times  $T_1$  and  $T_2$  are both inherently sensitive to molecular dynamics [13], the relaxation characteristics of fluids  
21 confined to porous structures can provide unique insight into material structural properties including pore size  
22 distributions and pore network connectivity [7,14–21].

## 1 Theory

2 Utilising  $^1\text{H}$  (proton) relaxation measurements this study considered the dynamics of water confined to the pore  
3 structures of the CPB materials. Such systems are assumed to exist under the conditions of biphasic fast  
4 exchange, wherein the rates of mixing between water molecules adsorbed at the pore surface and those towards  
5 the centre of the pore is considered to be rapid relative to their intrinsic rates of NMR relaxation [22]. Under  
6 such conditions the measured relaxation rates  $T_i^{-1}$  (with  $i = 1$  or  $2$  for longitudinal or transverse NMR  
7 relaxation, respectively) are given by a combination of unrestricted (bulk), surface (adsorbed) and confinement  
8 contributions according to [23]

$$\frac{1}{T_i} \approx \frac{1}{T_{i,bulk}} + \frac{2\alpha\rho_i}{d_{pore}} + \frac{8\alpha D}{d_{pore}^2}. \quad (1)$$

9 Here  $T_{i,bulk}$  are the relaxation time constants of the unrestricted fluid,  $\alpha$  is a shape parameter which takes values  
10 of 1, 2 or 3 for planar, cylindrical or spherical pores, respectively [24],  $D$  is the self-diffusion coefficient of the  
11 confined fluid, and  $\rho_i$  are the longitudinal ( $i = 1$ ) and transverse ( $i = 2$ ) surface relaxivities, which define the  
12 rates of enhanced NMR relaxation which occurs at the pore surface [17,18,25]. Importantly,  $d_{pore}$  is the pore  
13 diameter of the confining pore structure; Equation (1) therefore provides a direct link between the observed  
14 NMR relaxation time constants and the microstructural characteristics of the materials under investigation. This  
15 relationship is further resolved through the assumption of so-called surface-limited relaxation, a regularly-  
16 applied assumption for cementitious materials and other heterogeneous porous media, wherein  $4D/d_{pore} \gg \rho_i$   
17 [18,19,26,27]. In this case Equation (1) simplifies to [23]

$$\frac{1}{T_i} \approx \frac{1}{T_{i,bulk}} + \frac{2\alpha\rho_i}{d_{pore}}, \quad (2)$$

18 such that the observed relaxation time constants  $T_i$  are proportional to  $d_{pore}$ . It follows that the measurement  
19 of these time constants throughout the CPB hydration process can provide valuable information on the rates and  
20 extent of pore structure evolution, and the influence of different mixing waters on hydration behaviour. Herein  
21 we apply this approach to study the pore structure evolution of CPB samples over the first 56 days of hydration,  
22 contrasting the behaviour of tap water and hypersaline water hydrated mixtures. We then further investigate the  
23 relationship between apparent pore size and material strength characteristics through the comparison of these  
24 NMR relaxation times with the results of UCS measurements.

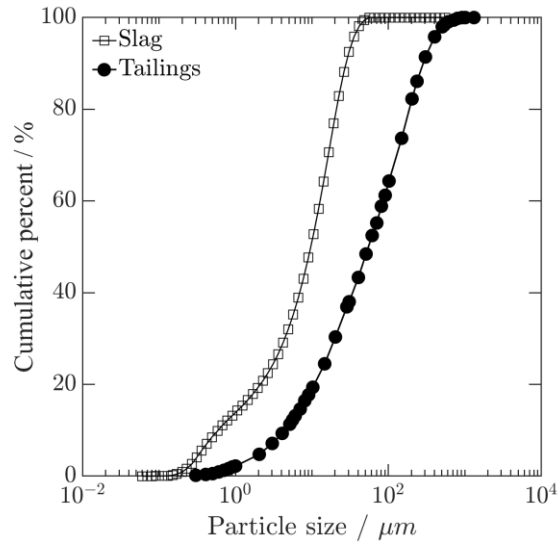
# 1 **Materials and Methods**

## 2 **Material preparation**

3 Minerals tailings were acquired from the Frog's Leg Gold Mine, located ~19 km west of Kalgoorlie, Western  
4 Australia. The tailings were sieved to < 4.75 mm before use to remove any coagulated particles, and dehydrated  
5 by drying in air at 110 °C for 24 hours. Figure 1 illustrates the particle size distribution of both the tailings and  
6 commercially available slag (sourced from BGC Cement, Australia) used in this study, which were found to  
7 exhibit mean ( $d_{50}$ ) particle sizes of 60  $\mu\text{m}$  and 10  $\mu\text{m}$ , respectively. The chemical composition of the tailings is  
8 reported in Table 1 and was assessed by Inductively Coupled Plasma-Optical Emission Spectroscopy (ICP-  
9 OES); the tailings were first dried and finely ground, then fused with 12:22 Norrish Flux (Lithium metaborate  
10 / Lithium tetraborate) in platinum crucibles at 1050 °C to form glass beads. The beads were then dissolved in 1  
11 M hydrochloric acid, with the resulting solution analysed using an Optima 5300 DV ICP-OES. The detected  
12 elemental concentrations were converted to oxide wt% values based on the corresponding atomic weights.

13 The CPB binders comprised a mixture of slag and OPC in a 2:1 ratio by mass. As cement concentrations used  
14 in typical mine sites vary between 1 and 10 wt% we opted here to explore two different binder concentrations  
15 exhibiting 5 and 9 wt% binder content, respectively, relative to the total tailings and binder mass; a total solids  
16 content of 76 wt% was maintained across all CPB samples investigated. Common tap water and hypersaline  
17 water were used as mixing waters, with the hypersaline water obtained from the same site as the mineral tailings.  
18 Chemical analysis of these waters was conducted via ICP-OES and anion chromatography, with the resulting  
19 ionic composition data reported in Table 2. Anion chromatography tests were conducted using a Thermo  
20 Scientific Dionex IonPac AS23 instrument while cation concentrations were obtained using an Optima 5300  
21 DV ICP-OES.

22 To form the CPB samples the dehydrated tailings and hydraulic binders were mixed with either tap water or  
23 hypersaline water for 3 minutes at 90 rpm using a stand mixer. The resultant CPB pastes were subsequently  
24 transferred to cylindrical plastic moulds (diameter = 50 mm, height = 100 mm) for UCS analysis, and to  
25 cylindrical plastic containers (diameter = 44 mm, height = 108 mm) for NMR analysis; the samples were each  
26 cured at  $20 \pm 2$  °C with a relative humidity of 95 % until the appropriate hydration time was attained.



1

2 Figure 1: Particle size distributions of tailings and slag. Tailings exhibit  $d_{60} \sim 90 \mu\text{m}$ ,  $d_{50} \sim 60 \mu\text{m}$  and  $d_{10} \sim 5$   
 3  $\mu\text{m}$ , while the slag exhibits  $d_{60} \sim 13 \mu\text{m}$ ,  $d_{50} \sim 10 \mu\text{m}$ , and  $d_{10} \sim 0.6 \mu\text{m}$ . Prior to analysis both the tailings and  
 4 slag were pre-screened to remove large rocks and agglomerates.

5

6 Table 1. Chemical composition of the mine tailings used in this study obtained from ICP-OES analysis.

Chemical composition	Content (wt%)	Chemical composition	Content (wt%)
SiO <sub>2</sub>	68.49	K <sub>2</sub> O	1.34
Al <sub>2</sub> O <sub>3</sub>	9.55	SO <sub>3</sub>	1.13
Na <sub>2</sub> O	3.31	TiO <sub>2</sub>	0.54
Fe <sub>2</sub> O <sub>3</sub>	3.18	MnO	0.08
CaO	3.16	P <sub>2</sub> O <sub>5</sub>	0.05
MgO	1.56		

7

8 Table 2. Chemical compositional analysis of the mixing waters used in this study obtained from ICP-OES and  
 9 anion chromatography.

Hypersaline water / mg L <sup>-1</sup>		Tap water / mg L <sup>-1</sup>	
Ca <sup>2+</sup>	955	Cl <sup>-</sup>	620
Fe	<0.002	SO <sub>4</sub> <sup>2-</sup>	6
K <sup>+</sup>	230	Br <sup>-</sup>	1
Mg <sup>2+</sup>	7790		
Na <sup>+</sup>	61900		
Cl <sup>-</sup>	115000		
SO <sub>4</sub> <sup>2-</sup>	4480		
Br <sup>-</sup>	199		

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11

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## 1 **Uniaxial compressive strength tests**

2 UCS is a key mechanical property in CPB analysis. The UCS of our CPB samples was measured using an  
3 Electro-hydraulic Servo-controlled universal testing machine (GDS LF-50) with a maximum load capacity of  
4 50 kN. Tests were conducted once the CPB samples had been cured for 7, 14, 28 and 56 days. Following each  
5 curing process the CPB samples were placed between two parallel plates and were loaded under constant  
6 displacement conditions with a displacement rate of  $1 \text{ mm min}^{-1}$ . UCS readings were recorded every second and  
7 the axial loading terminated when the sample developed an obvious shearing plane. Tests were performed in  
8 triplicate with the average of the three values reported here; a maximum 10% standard deviation from the mean  
9 strength was observed across all samples.

## 10 **High resolution X-ray computed tomography**

11 X-ray  $\mu$ -CT was performed to obtain an estimate of the (capillary) pore size distribution of CPB materials. A  
12 single material sample comprising 5 wt% binder was prepared in a glass vial (diameter = 5 mm, height = 25  
13 mm) and scanned using a Zeiss XRM520 3D X-ray microscope with a  $1 \mu\text{m}$  voxel resolution. A total of 1600  
14 projections were recorded over  $360^\circ$  (i.e.  $0.225^\circ$  rotation of the sample between each projection). Artefacts were  
15 either reduced during acquisition or corrected during the reconstruction procedure, and image filtering was  
16 performed using a non-local mean algorithm which acted to enhance the image by reducing noise and improving  
17 phase discrimination. Segmentation into different phases (pores and solids) was achieved using a modified  
18 version of the 3D gradient watershed algorithm, attributing a range of grayscale values to a given phase, with  
19 phase boundaries being located at the point of maximum gradient in grayscale, as described elsewhere [28].  
20 Each reconstructed dataset was processed using Avizo 9.5 (ThermoFisher) and MATLAB (MathWorks Inc.)  
21 according to the workflow described in [28].

## 22 **Nuclear magnetic resonance relaxation measurements**

23 NMR relaxation experiments were conducted using a benchtop Magritek Rock Core Analyser equipped with a  
24 0.05 T cylindrical Halbach magnet array, providing a  $^1\text{H}$  NMR frequency of 2 MHz. The radio frequency (RF)  
25 pulse lengths were fixed at  $20 \mu\text{s}$  with the pulse amplitudes for  $90^\circ$  and  $180^\circ$  RF pulses set to -12.5 dB and -6.5  
26 dB, respectively. Both the longitudinal ( $T_1$ ) and transverse ( $T_2$ ) nuclear spin relaxation characteristics of our  
27 CPB materials were measured, with the RF pulse sequences used illustrated in Figure 2. Measurements were

1 performed on each day for two weeks (days 1 – 14) followed by further analysis on days 28, 30, 31 and 56. All  
 2 NMR measurements were performed with a constant magnet bore temperature of 30 °C. Both  $T_1$  and  $T_2$   
 3 measurements were performed using a recycle delay of 10 s and 4 repeat scans, resulting in acquisition times  
 4 of 15 minutes and 1 minute, respectively, and signal-to-noise ratios > 200.

5 Longitudinal relaxation times were measured using the standard inversion-recovery (IR) pulse sequence shown  
 6 in Figure 2a [29]. Starting from thermal equilibrium wherein the sample magnetisation lies parallel to the  
 7 external magnetic field (conventionally the z-axis), the IR measurement is initiated by a 180° RF pulse which  
 8 rotates the sample magnetisation onto the -z axis. Longitudinal relaxation processes are then permitted for a  
 9 variable recovery period  $\tau_1$  during which the sample magnetisation recovers towards equilibrium. Following  
 10 each recovery period a 90° RF pulse acts to rotate the magnetisation into the transverse plane, allowing the  
 11 magnitude of the sample magnetisation to be measured [30]. In this work 20 logarithmically-spaced  $\tau_1$  recovery  
 12 times between 0.5 ms and 500 ms were used. The resulting longitudinal relaxation data are described according  
 13 to a Fredholm integral equation of the first kind [31],

$$\frac{S(\tau_1)}{S(\tau_1 \rightarrow \infty)} = \int K_1(\tau_1, T_1) f(T_1) d \log_{10}(T_1) + \varepsilon(\tau_1). \quad (3)$$

14 Here  $S(\tau_1)/S(\tau_1 \rightarrow \infty)$  is the normalised NMR signal intensity following each  $\tau_1$  delay, the Kernel function  
 15  $K_1(\tau_1, T_1) = 1 - 2 \exp(-\tau_1/T_1)$  describes the expected form of  $T_1$  relaxation following the IR experiment  
 16 [29], and  $f(T_1)$  represents the distribution of  $T_1$  time constants present;  $\varepsilon(\tau_1)$  is the experimental noise, assumed  
 17 Gaussian in shape with zero mean.

18 Transverse relaxation times were measured using the standard CPMG (Carr-Purcell-Meiboom-Gill) experiment  
 19 shown in Figure 2b [32,33]. Starting again from thermal equilibrium the sample magnetisation is excited into  
 20 the transverse plane via a 90° RF pulse, which initiates transverse dephasing of the system's magnetic moments.  
 21 A series of  $n$  180° RF pulses refocusses dephasing arising from inhomogeneity of the static magnetic field,  
 22 generating a train of  $n$  spin echoes which decay according to  $T_2$ . In this work we employed  $n = 500$  echoes  
 23 separated by an echo time of  $t_e = 100 \mu\text{s}$ ; this short echo time, together with the low static magnetic field  
 24 strength employed in this study, aimed to limit the influence of undesired transverse relaxation phenomena due



1 to magnetic susceptibility contrast effects at the solid-liquid interface [21,34]. The resulting relaxation data are  
2 again described by a Fredholm integral equation of the first kind [31],

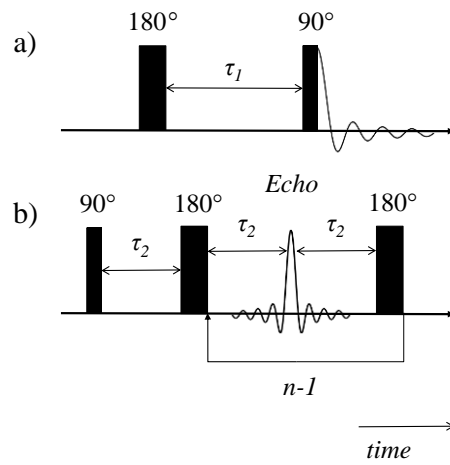
$$\frac{S(nt_e)}{S(0)} = \int K_2(nt_e, T_2) f(T_2) d \log_{10}(T_2) + \varepsilon(nt_e). \quad (4)$$

3 Here  $S(nt_e)/S(0)$  is the normalised NMR signal intensity acquired during each echo, the Kernel function  
4  $K_2(nt_e, T_2) = \exp(-nt_e/T_2)$  describes the expected form of  $T_2$  relaxation [33] and  $\varepsilon(nt_e)$  again represents the  
5 experimental noise.

6 The desired time constant distributions  $f(T_1)$  and  $f(T_2)$  were obtained via a numerical inversion of our acquired  
7 experimental data according to Equations (3) and (4); as this is an ill-posed problem it was necessary to employ  
8 Tikhonov regularisation [35] to ensure the stability of the resulting  $T_1$  and  $T_2$  distributions in the presence of  
9 experimental noise, with the smoothing parameter chosen according to the generalised cross-validation method  
10 [36]. This robust mathematical inversion technique makes no assumptions about the shape of the resultant  
11 probability distributions, and has been successfully implemented across a range of NMR data analysis protocols,  
12 including relaxation time distributions in porous media [7,37,38] and droplet sizing methods [39]. The inversion  
13 algorithm used in this work was written in MATLAB (MathWorks Inc.) and first used by Griffith *et al.* [40]  
14 As indicated by Equations (3) and (4), as the NMR relaxation time constants exhibited by fluids confined to  
15 heterogeneous porous materials are regularly found to vary across multiple decades within the  $\mu\text{s} - \text{s}$  range,  
16 such expression are typically inverted on a logarithmic – rather than a linear – scale [41].

17

1



2

3 Figure 2. Radio frequency (RF) pulse sequence diagrams for a)  $T_1$  relaxation time measurements via the  
4 inversion recovery experiment, and b)  $T_2$  relaxation time measurements via the CPMG experiment. Vertical  
5 bars represent RF pulses of constant length;  $\tau_1$  represents the variable recovery delays used in the inversion  
6 recovery experiment while the CPMG echo time is  $t_e = 2\tau_2$ .

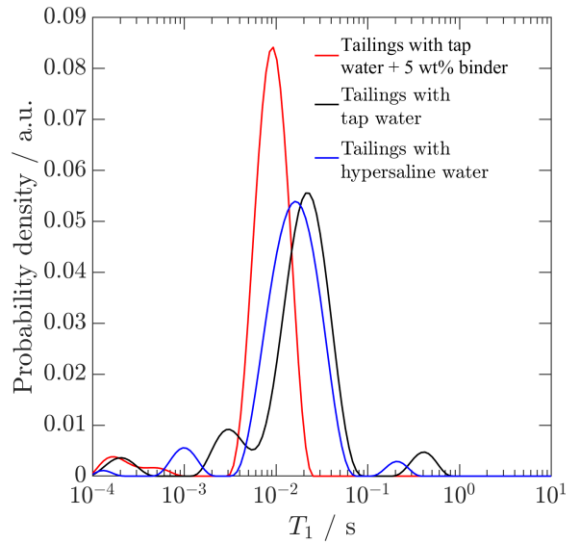
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# 1 **Results and Discussion**

## 2 **Initial characterisation**

3 Figure 3 illustrates the influence of binders (cement and slag) on the observed  $T_1$  relaxation time distributions  
4 of water-saturated tailings. Clearly, when tailings are mixed with either tap or hypersaline water the  $T_1$   
5 distributions appear similar, with dominant peaks located at approximately 15 – 20 ms; this  $T_1$  population is  
6 readily assigned to water constricted within the inter-particulate region of the tailings. The addition of 5 wt%  
7 binder has a perceivable effect on the observed  $T_1$  distribution, however, and in the case of tap water reduces  
8 the dominant  $T_1$  population to ~10 ms. This value is consistent with previous low-field relaxation studies of  
9 cementitious systems, which observed  $T_1$  times of this order to correlate with the water population of capillary  
10 pore spaces [18,42]. Figure 4 demonstrates CPB pore structure characterisation via high-resolution X-ray  $\mu$ -  
11 CT analysis of a sample containing 5 wt% solids hydrated with tap water for 21 days. This data demonstrates  
12 the typical pore size distribution exhibited by such structures, wherein the observed pore spaces are largely  
13 present across the length scale 5 – 25  $\mu\text{m}$ . Given the resolution of this  $\mu$ -CT analysis and the resultant pore size  
14 distribution, these structures are readily identified as capillary-type pores.

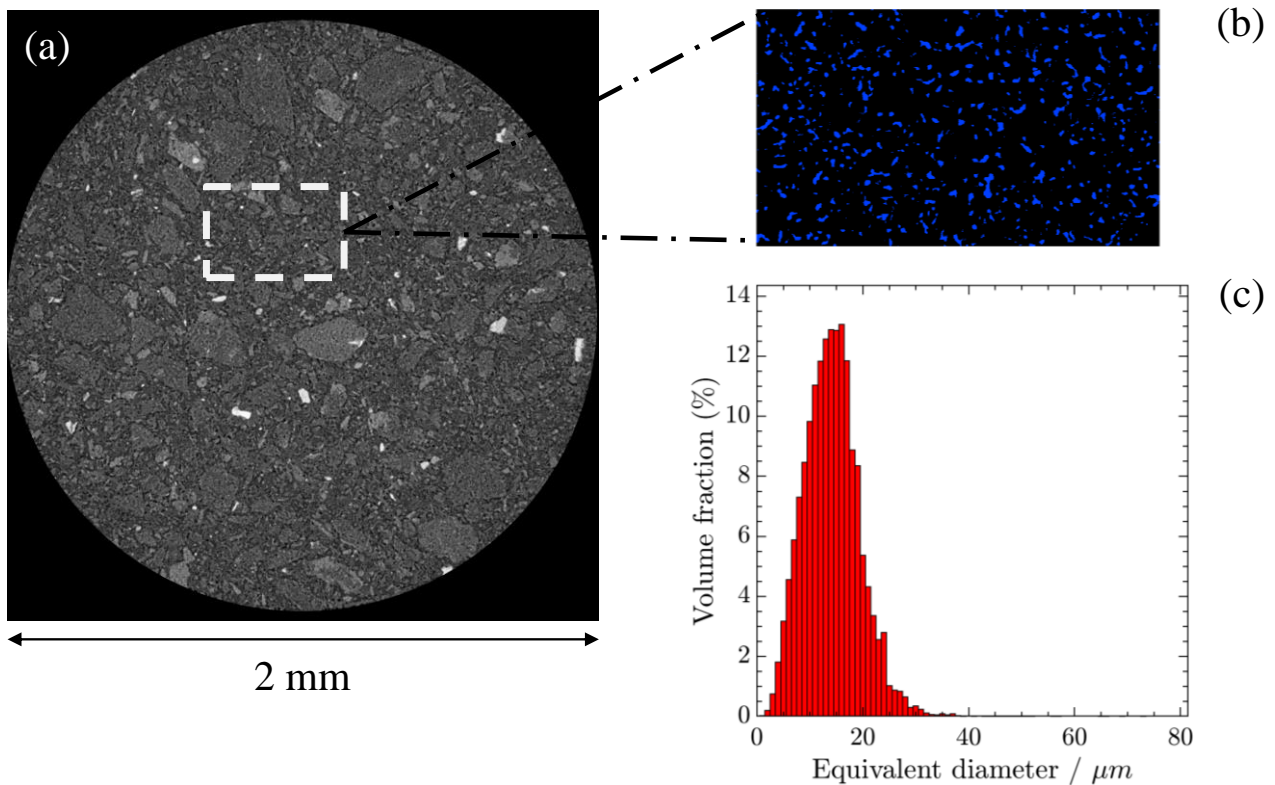
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2 Figure 3.  $T_1$  relaxation time distributions for tap water and hypersaline water saturated tailings samples, and tap  
 3 water saturated tailings with 5 wt% binder content. A shift to lower  $T_1$  values is evident upon the addition of  
 4 cement to the sample.

5



6

7 Figure 4. a) X-ray  $\mu$ -CT image of cemented paste backfill comprising 5 wt% binder content and 76 wt% solids  
 8 content following hydration with tap water for 21 days. b) Example segmented X-ray  $\mu$ -CT data identifying the  
 9 solids (black) and pore space (blue). c) Equivalent pore diameter distribution obtained from the segmentation  
 10 of image data in a), indicating that observable pores are dominant at the  $d_{pore} = 5 - 25 \mu m$  length scale; these  
 11 are assigned to capillary pore structures.

## 1 **Pore structure evolution**

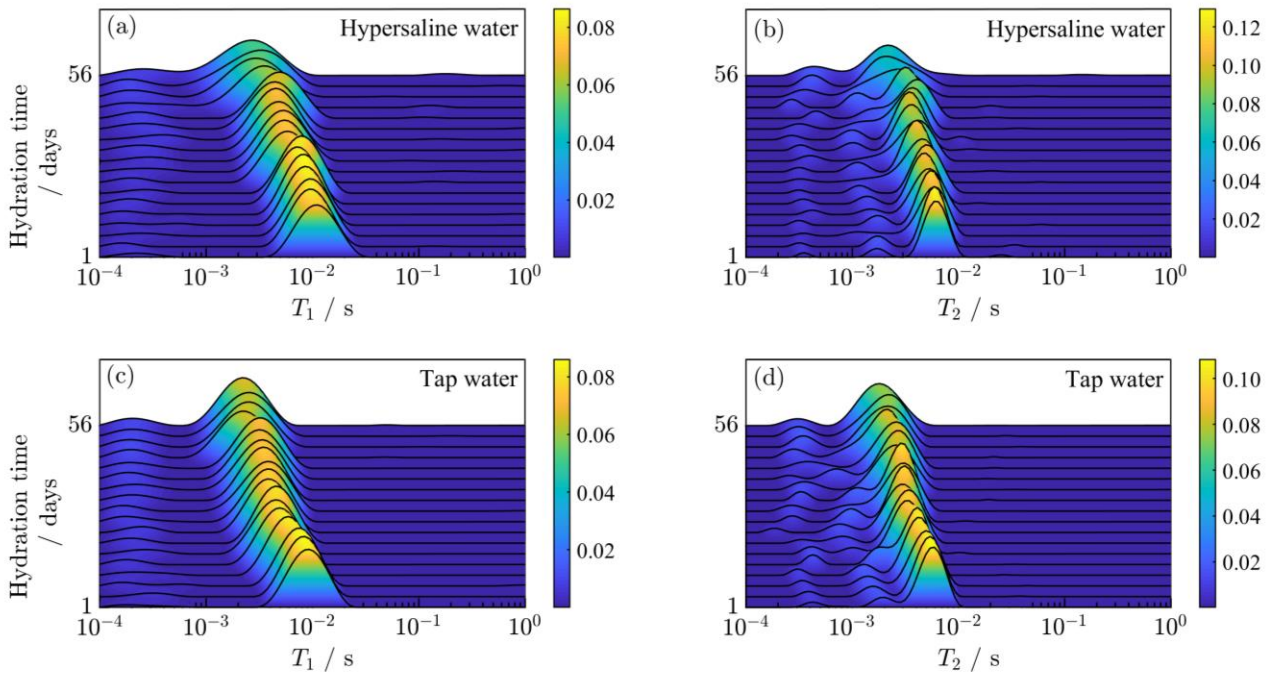
2 Figures 5 and 6 report the acquired NMR relaxation data from our CPB materials. Figure 5 illustrates the  $T_1$  and  
3  $T_2$  relaxation time distribution evolution of CPB samples with 5 wt% binder content; Figure 5a and 5b reports  
4 the evolution of hypersaline water hydrated CPB, while Figure 5c and 5d reports the evolution following  
5 hydration with tap water. In all cases a dominant relaxation peak is observed, which decreases in value over the  
6 hydration time scale. In our  $T_1$  data these dominant peaks are initially observed at  $T_1 \approx 10$  ms and decrease to  
7  $T_1 \approx 2$  ms after 56 days of hydration. As introduced previously, this initial dominant  $T_1$  population can be  
8 assigned to water confined within the capillary pore space of the cementitious matrices, [42] which for our CPB  
9 materials is expected to occur over the 5 – 25  $\mu\text{m}$  size range (Figure 4). The corresponding  $T_2$  data is displayed  
10 in Figure 5b and 5d, wherein the dominant peaks decrease from  $T_2 \approx 6$  ms to  $T_2 \approx 2$  ms after 56 days. The  
11 observation of reduced  $T_2$  values, relative to the  $T_1$  characteristics exhibited by the same porous structure, is in  
12 accordance with the known surface relaxation behaviour of fluids confined to cement-based materials [18].

13 Three distinct  $T_2$  populations are evident at the onset of the hydration process in both the hypersaline water and  
14 tap water systems; given our knowledge of the relationship between material pore size and NMR relaxation  
15 times (Equation (2)) these peaks may be assigned to distinct water populations occupying pore structures of  
16 different sizes. In particular, given the established pore hierarchy of cementitious materials, we assign these  
17 populations to capillary pore ( $T_2 \sim 3\text{-}100$  ms), interhydrate pore ( $T_2 \sim 0.8\text{-}2$  ms) and gel pore ( $T_2 \sim 300\text{-}500$   
18  $\mu\text{s}$ ) structures, in order of decreasing  $T_2$ . This expected pore hierarchy is illustrated in Figure 7 [42–44]. No  
19 clear relaxation contributions are observed from solid  $^1\text{H}$ -bearing hydration products [45], or from water within  
20 the associated interlayer spaces [46]; we attribute this absence to the very short  $T_2$  characteristics expected from  
21 such features, the measurement of which is likely beyond the echo time limitations of our NMR hardware.

22 As the hydration processes progress, the interhydrate and capillary pore  $T_2$  populations can be seen to merge,  
23 indicating that the capillary and interhydrate pore structures become indistinguishable in the latter stages of  
24 CPB hydration. This observation, together with the clear decrease in modal  $T_1$  and  $T_2$  relaxation times within  
25 increasing hydration period, is consistent with the known physical mechanisms of cement hydration, whereby  
26 hydration products forming at the surface of cement particles ingress into the capillary pore space [47].

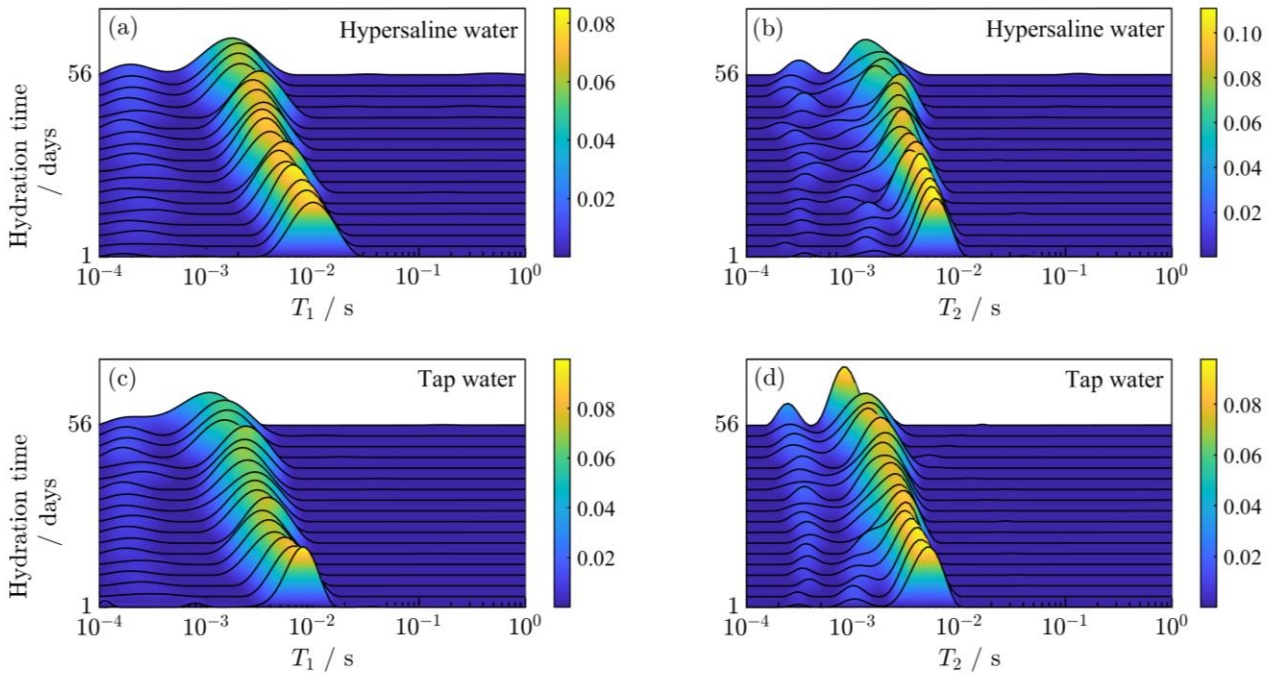
1 No interhydrate water population is observed within the  $T_1$  data presented in Figures 4a and 4b, suggesting such  
2 measurements are unable to distinguish between water within capillary and interhydrate pores, even at short  
3 hydration times. This observation is consistent with the temporally averaged nature of  $T_1$  measurements, relative  
4 to  $T_2$  analysis [48]; this phenomena facilitates a greater degree of diffusive pore-to-pore exchange during  
5 relaxation measurements, resulting in greater  $T_1$  averaging between pores of difference size, and hence reduced  
6 pore structure resolution. Notwithstanding these observations, the relative  $T_2$  populations assigned to  
7 interhydrate and capillary pores demonstrate that the major peaks within our  $T_1$  and  $T_2$  distributions are  
8 dominated by water within the capillary pore structures of the CPB materials under investigation.

9 Similar to Figure 5, Figure 6 illustrates the  $T_1$  and  $T_2$  relaxation time distribution evolution of CPB samples  
10 with 9 wt% binder content; Figure 6a and 6b reports the evolution of hypersaline water-hydrated CPB, while  
11 Figure 6c and 6d reports the evolution following hydration with tap water. These distributions again illustrate a  
12 major peak which we assign as dominated by water within the capillary pore spaces of the CPB materials, and  
13 which tends to shorter relaxation times with increasing hydration period. Our  $T_1$  data again shows two separate  
14 populations, with the dominant population decreasing from  $T_1 \approx 10$  ms to between 1 ms (tap water) and 2 ms  
15 (hypersaline water), depending on the mixing water employed. The  $T_2$  data illustrated in Figure 6b and 6d again  
16 shows three separate water populations at short hydration times, which we again assign to capillary, inter-  
17 hydrate and gel pore structures within the CPB materials. The capillary and inter-hydrate populations are again  
18 observed to merge with increasing hydration time; however, we note that this process occurs at a much earlier  
19 stage within the hydration process than observed in the 5 wt% binder CPB data shown in Figure 5. This  
20 observation therefore indicates that an increase in cement content facilitates more rapid overall structural  
21 evolution of the CPB pore hierarchy.



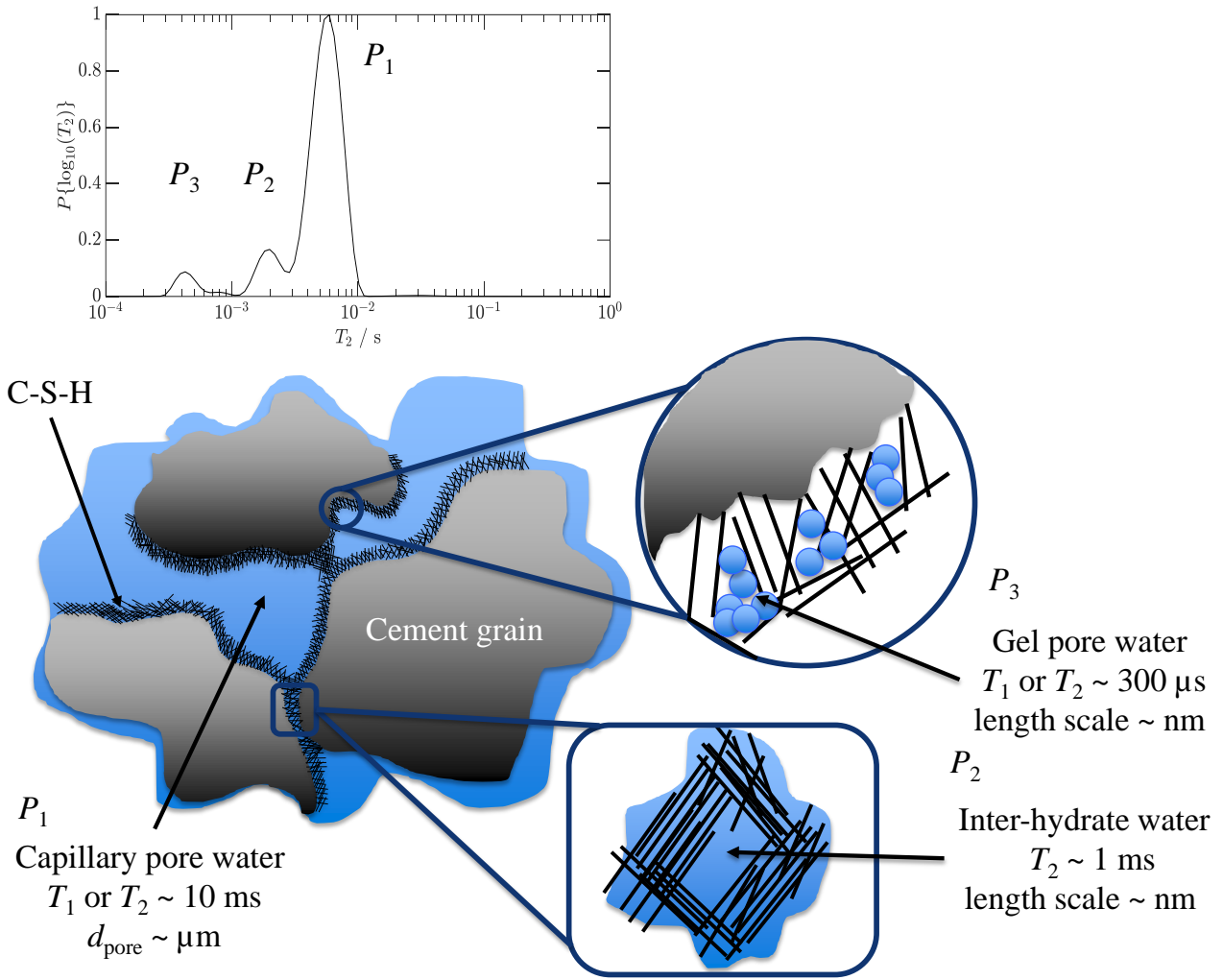
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2 Figure 5.  $T_1$  and  $T_2$  relaxation time distributions for CPB samples comprising 5 wt% binder content and 76 wt%  
 3 solids. a) and b) illustrate the relaxation distribution evolution when hydrated with hypersaline water, while c)  
 4 and d) illustrate the corresponding data when hydrated with tap water. Data was acquired on days 1-14, 28, 30,  
 5 31 and 56. Colour bars indicate the probability density of the relaxation distributions.



6

7 Figure 6.  $T_1$  and  $T_2$  relaxation time distributions for CPB samples comprising 9 wt% binder content and 76 wt%  
 8 solids. a) and b) illustrate the relaxation distribution evolution when hydrated with hypersaline water, while c)  
 9 and d) illustrate the corresponding data when hydrated with tap water. Data was acquired on days 1-14, 28, 30,  
 10 31 and 56. Colour bars indicate the probability density of the relaxation distributions.



1

2 Figure 7: Schematic relating NMR relaxation times  $T_1$  and  $T_2$  to unique water-saturated pore environments in  
 3 cementitious system. Water in capillary pores exhibit  $T_1$  or  $T_2$  relaxation times of  $\sim 10$  ms, inter-hydrate water  
 4 display observable  $T_2$  relaxation time of  $\sim 1$  ms, while rapid  $T_1$  and  $T_2$  relaxation times of  $\sim 300 \mu\text{s}$  correlate to  
 5 water in gel pores [42–44]. The abbreviation C-S-H stands for calcium silicate hydrate.

6



1 Clearly qualitatively similar trends are exhibited by the eight data sets presented in Figures 5 and 6. This is  
2 accentuated in Figure 8 where we consider a quantitative analysis of the modal  $T_1$  and  $T_2$  relaxation times (from  
3 here on in referred to as  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$ , respectively) from these distributions as a function of CPB hydration  
4 time. As detailed in Figure 8, hypersaline water CPB samples exhibit delayed hydration in terms of  $\langle T_1 \rangle$  and  
5  $\langle T_2 \rangle$  (suggestive of delayed pore size evolution), relative to the tap water CPB samples. This delay was evaluated  
6 by fitting the modal relaxation data to an empirical exponential function of the form

$$\langle T_i \rangle = a_i \exp(-b_i t) + c_i. \quad (5)$$

7 Here  $b_i$  (with  $i = 1$  or  $2$  for  $T_1$  and  $T_2$  measurements, respectively) describes the observed decay rate which  
8 characterises the size reduction of the dominant (most populous) pore structure of each sample across the 56  
9 days of hydration assessed,  $t$  is the hydration time, while  $a_i$  and  $c_i$  are a pre-exponential and offset parameters,  
10 respectively. The offset parameter  $c_i$  is necessary to describe the finite (i.e. non-zero) pore dimensions exhibited  
11 by our CPB materials at long hydration times, while the apparent pore sizes at  $t = 0$  may be estimated from  
12  $(a_i + c_i)$ .

13 The results of the above fitting are detailed in Table 3. The fitted  $T_1$  data suggest that pore structure evolution  
14 rates increase upon increasing the binder content from 5 wt% to 9 wt%, consistent with both the rates at which  
15 capillary and interhydrate  $T_2$  populations are observed to merge in Figures 5 and 6, and the concept that an  
16 increase in binder content should lead to a greater degree of hydration product ingress into the capillary voids;  
17 no clear trend emerges from our fitted  $T_2$  data. In terms of comparing the effect of different mixing water we  
18 first consider samples containing 5 wt% binder content. Here a decrease in pore structure evolution rate is  
19 observed upon moving from tap to hypersaline mixing water within both the  $T_1$  and  $T_2$  data sets, indicating that  
20 the use of hypersaline water reduces the overall rate of hydration product ingress into the available capillary  
21 voids. Contrasting the behaviour of tap and hypersaline water within samples containing 9 wt% binder content,  
22 however, reveals similar decay rates across the two mixing waters; this behaviour is also visibly evident in  
23 Figure 8. This finding, together with the above observations concerning increased rates of pore structure  
24 evolution in the presence of increased binder content, suggests that the more rapidly developing pore structure  
25 hierarchy of the materials containing 9 wt% binder may offset the retardation effects of hypersaline water.

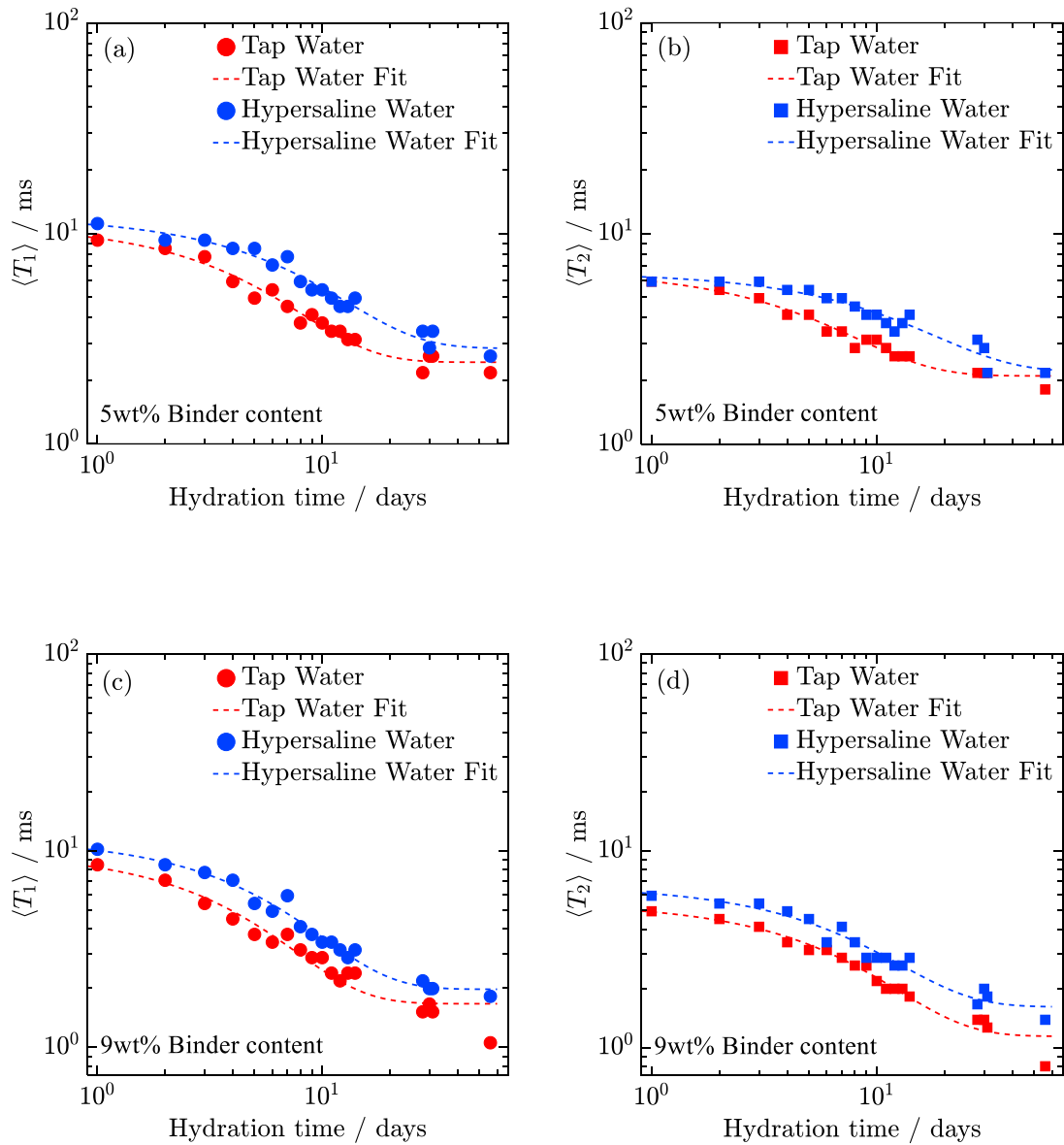
1 Instead, a clear and persistent difference is observed between the tap water and hypersaline water hydrated CPB  
 2 data in Figure 8c and d, suggesting that the difference in pore structure (as evidenced via our relaxation  
 3 measurements) within these materials is dominated by material properties at the initiation of the hydration  
 4 process.

5

6 Table 3: Exponential fitting data of the modal NMR relaxation data illustrated in Figure 8 according to Equation  
 7 (5). For brevity the rate constant  $b_{1,2}$  is given in units of  $\text{day}^{-1}$ . Uncertainty bounds indicate the 95 %  
 8 confidence intervals obtained from the fitting process.

	$\langle T_1 \rangle$				$\langle T_2 \rangle$			
	$a_1 / \text{ms}$	$b_1 / \text{day}^{-1}$	$c_1 / \text{ms}$	$a_1 + c_1 / \text{ms}$	$a_2 / \text{ms}$	$b_2 / \text{day}^{-1}$	$c_2 / \text{ms}$	$a_2 + c_2 / \text{ms}$
Tap water	$8.62 \pm$	$0.20 \pm$	$2.44 \pm$	$11.06 \pm$	$4.56 \pm$	$0.18 \pm$	$2.11 \pm$	$6.67 \pm$
5 wt% binder	0.84	0.04	0.3	0.90	0.41	0.03	0.19	0.45
Hypersaline water	$9.18 \pm$	$0.12 \pm$	$2.85 \pm$	$12.03 \pm$	$4.31 \pm$	$0.08 \pm$	$2.21 \pm$	$6.52 \pm$
5 wt% binder	0.94	0.03	0.60	1.12	0.56	0.03	0.53	0.77
Tap water	$8.26 \pm$	$0.23 \pm$	$1.67 \pm$	$9.93 \pm$	$4.29 \pm$	$0.13 \pm$	$1.14 \pm$	$5.43 \pm$
9 wt% binder	0.98	0.05	0.34	1.02	0.31	0.02	0.19	0.36
Hypersaline water	$9.61 \pm$	$0.18 \pm$	$1.98 \pm$	$11.59 \pm$	$5.04 \pm$	$0.13 \pm$	$1.61 \pm$	$6.65 \pm$
9 wt% binder	0.88	0.03	0.41	0.97	0.57	0.03	0.36	0.67

9



1

2 Figure 8: Modal  $T_1$  and  $T_2$  relaxation time data for CPB samples comprising 5 wt% (a and b) and 9 wt% (c and  
 3 d) binder content and 76 wt% solids as a function of hydration time. Both common tap water (red) and  
 4 hypersaline water (blue) data is shown in each case. Model fits correspond to Equation (5), with the resulting  
 5 parameters detailed within Table 3.

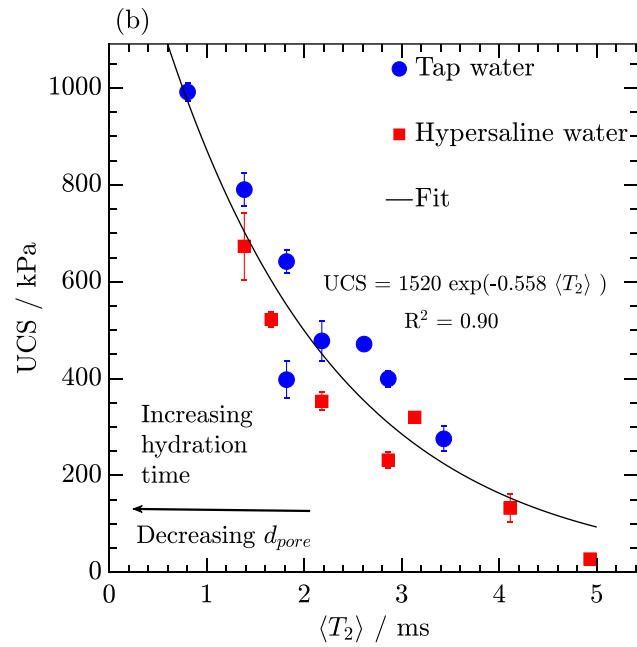
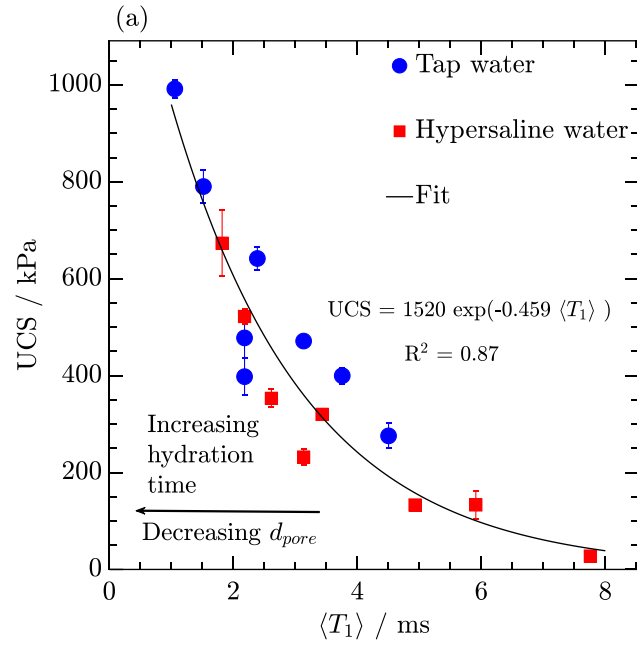
6

## 1 **NMR relaxation – strength correlations**

2 The mechanical properties of our CPB materials were assessed via uniaxial compressive strength (UCS)  
3 analysis; these tests were performed on CPB samples following hydration for 7, 14, 28 and 56 days, providing  
4 insight into the mechanical strength of these materials across the range of hydration times examined in our NMR  
5 relaxation measurements. UCS analysis on CPB materials experiencing fewer than 7 days of hydration was not  
6 possible due to the limited solidification found to have occurred before this time.

7 Figure 9 details a correlation between the observed  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  relaxation times and the results of this UCS  
8 analysis, overlaying contributions from both tap water and hypersaline water hydrated CPB materials  
9 comprising 5 wt% and 9 wt% binder content. In both data sets there exists a clear trend, with shorter relaxation  
10 times correlating with increased mechanical strength. Recalling once again the relationship between NMR  
11 relaxation time constants and pore size, these data clearly suggest that CPB materials exhibiting smaller  
12 capillary pore structures display comparatively increased mechanical strength characteristics. While there is no  
13 clear difference in the UCS results of materials hydrated with tap or hypersaline mixing water at comparative  
14  $\langle T_1 \rangle$  or  $\langle T_2 \rangle$  times, the lag behaviour of CPB materials hydrated with hypersaline water is clearly apparent within  
15 these plots, wherein the hypersaline hydrated CPB is shown to exhibit noticeably reduced UCS load capacities,  
16 relative to tap water hydrated CPB of the same age.

17 Importantly, the two data sets within Figure 9 are described well by an exponential relationship between  
18 measured UCS and NMR relaxation characteristics; this relationship takes the form  $UCS = A \exp(-B_i \langle T_i \rangle)$   
19 (with  $i = 1$  or  $2$ ). Here  $A = 1520$  kPa is a pre-exponential load factor which was found to be independent of  
20 both the NMR relaxation mechanism probed ( $T_1$  or  $T_2$  relaxation) and the binder content of CPB, while the rate  
21 constants take values of  $B_1 = 0.459 \text{ s}^{-1}$  and  $B_2 = 0.558 \text{ s}^{-1}$  for the  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  curves, respectively. The capacity  
22 to fit such a simple and predictive expression encompassing the relaxation and mechanical strength properties  
23 of both tap water and hypersaline water hydrated CPB materials exhibiting variable binder content is clearly  
24 highly desirable; indeed, this expression facilitates the prediction of CPB mechanical strength properties based  
25 on the measurement of NMR relaxation times alone. It follows that such correlations provide a potential avenue  
26 for the assessment of industrial site CPB formations using NMR logging tools or single sided magnet-based  
27 spectrometers [26,49–51].



1

2 Figure 9: Correlation of a)  $\langle T_1 \rangle$  and b)  $\langle T_2 \rangle$  NMR relaxation times against CPB UCS data. Data from materials  
 3 containing both 5 wt% and 9 wt% binder content are overlaid. A model exponential decay is detailed in each  
 4 case and discussed further in the main text.

1 **Conclusions**

2 Low-field  $^1\text{H}$  NMR relaxation measurements were utilised to investigate the microstructural characteristics of  
3 CPB materials hydrated with both tap and hypersaline mixing waters. Distributions of the NMR relaxation time  
4 constants  $T_1$  and  $T_2$  have been demonstrated to provide details on the pore structure hierarchy of such materials,  
5 with  $T_2$  data offering resolution between gel, interhydrate and capillary pore structures at short hydration times.  
6 These distributions also evidence the time-evolution of CPB capillary pore structures across the first 56 days of  
7 hydration. Contrasting the modal NMR relaxation times associated with water confined within these capillary  
8 pores provides a non-invasive route with which to quantify and compare the hydration rates of such materials;  
9 we demonstrated this approach through both the consideration of different mixing waters and through the  
10 comparison of varying binder contents. In general, the use of hypersaline water was observed to reduce CPB  
11 capillary pore hydration rates, relative to tap water. Through a direct comparison of NMR relaxation  
12 measurements with UCS analysis a predictive correlation has been developed between capillary pore size and  
13 mechanical strength, with small pore structures indicative of stronger CPB materials. This correlation is  
14 independent of both the NMR relaxation time constants considered and the CPB binder content employed.  
15 Furthermore, it highlights a clear lag effect observed in the hydration behaviour of hypersaline hydrated CPB  
16 samples, relative to tap water hydrated materials of the same age, resulting in comparatively weaker CPB  
17 structures. Overall, this study provides new and unique insight into the microstructural evolution of CPB  
18 materials, and highlights distinct relationships between NMR characteristics, pore structure and material  
19 strength which may be further exploited in the field through the application of NMR logging tools and single-  
20 sided magnets.

21

22

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5 **Conflicts of Interest**

6 The authors declare that they have no known competing financial interests or personal relationships that could  
7 have appeared to influence the work reported in this paper.

8

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