Online Software Allows Ethical Safety-Conscious Design of Terrain Park Jumps

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8 Abstract

Most American snowsport resorts now have terrain parks and decadeslong epidemiological evidence correlates terrain park use with injuries. Engineering design of jumps could reduce injuries by limiting equivalent fall heights, which are proportional to dissipated landing impact energy. No evidence refutes making terrain park jumps safer in this way. We discuss case studies illustrating that large equivalent fall heights are significant factors in traumatic injuries on terrain park jumps. We argue that it is the ethical responsibility of engineers to ensure the safety, health, and welfare of the public when performing and presenting research on snowsport safety. Developing standards and adopting design tools for builders can make jumps safer. As an example proactive practice to reduce injuries, we introduce an online tool that can evaluate existing jumps as well as design jump profiles with safer equivalent fall heights.

1 Introduction

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Impacts with fixed surfaces can cause injury. Greater velocities, perpendicular to the surfaces, provide greater injury potential due to increased kinetic energy

dissipation. Equivalent fall height (EFH) is a conceptually simple and familiar measure of impact danger used in safety standards worldwide, from construction [1] to children's playground equipment [2]. EFHs of terrain park jumps can 27 be calculated using techniques in [3] from Cartesian coordinates of jump profiles. These coordinates must include starting points, takeoff ramps, and landing 29 hills, all along jumpers' paths. Limiting energy dissipation in human bodies, 30 hence EFH on jumps, reduces likelihoods of injuries and their severities. EFH 31 should be a primary attribute of jump design. It must be considered because 32 it is clearly connected to injury risk and can be used to design and construct 33 safer jumps. In fact, safety research [4] tells us that designing forgiving environ-34 ments (i.e., limiting EFH at all possible landing locations) is more effective than 35 forcing behavioral change (e.g., requiring the jumper to regulate their speed to 36 ensure a landing only in a small safe region). 37

Societal costs of jump injuries are discussed here with case studies that illustrate dangers if EFH is not limited appropriately. We also discuss papers presented as ski safety research, which attempt to sow doubt about EFH relevance and snow sport danger, written by authors that regularly provide expert testimony defending the ski industry in personal injury lawsuits. Proposals for improved safety are absent in the papers. We present a user-friendly web application that can facilitate jumping injury reduction by calculating EFH on current and future jumps.

$_{ ext{\tiny 46}}$ 1.1 History

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Terrain park jumps are not new. Gradual introduction in the 1980's was accom-47 panied by increased interest in aerial maneuvers and extreme sports participation. Jumps have proliferated since and are today nearly ubiquitous. Roughly 95% of US ski resorts include terrain parks. Unfortunately, this growth correlates with injuries. Two early longitudinal studies in the 1980's and early 51 1990's [5, 6] already found significant increases in head injuries and concussions. 52 Between 1993 and 1997 head injuries accompanied most skiing and snowboarding deaths [7]. Koehle et al. [8] stated "[S] eventy-seven percent of spinal in-54 juries [9] and 30% of head injuries [10] in snowboarding were a result of jumps." 55 Jackson et al. [11] determined that by 2004 snow skiing replaced football as the 56 second leading cause of serious head and spinal cord injuries in America. 57

These early increasing injury assessments persisted. According to [12], "between 5 and 27% of skiing and snowboarding injuries occur[red] in terrain parks [13, 14, 15, 16, 17, 18]". Incredibly, at the first Winter Youth Olympic Games more than a third of all snowboard half-pipe and slope-style competitors were injured [19]. Epidemiological research [20, 21, 22] continues to show that injuries on terrain park jumps are more likely and more severe than on normal slopes. Audet et. al [21] provides evidence that skiing or snowboarding in a terrain park is a risk factor for head, neck, back, and other severe injuries. Hosaka et. al [22] concludes that jumping is a main cause for serious spinal injuries, regardless of skill level, and suggests that, because spinal injuries incidence have not decreased over time, the ski industry should focus on designing fail-safe jump features to

minimize risks of serious spinal injuries. Similar suggestions have appeared in peer-reviewed literature for more than a decade [23, 24, 25, 26, 27, 28, 3, 29, 30].

71 2 Methods

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2.1 Equivalent Fall Height

 73 EFH, a common proxy measure for impact danger in industrial safety standards, is the weight-specific kinetic energy that must be dissipated on falling impact from height h [31, 23, 32]. Initial potential energy mgh is transformed to kinetic energy available to injure in non-rotating falls. Injury potential can be reduced by controlling impact circumstances, e.g. impact cushioning, and body orientation, configuration, and motion; however this energy must still be dissipated. Larger EFHs require more elaborate measures to reduce injury; reducing EFH does not.

EFH can be interpreted by the general public. People have an intuitive sense of danger when faced with potential falls from large heights and a strong experiential common sense for relating fall height to likelihood of injury. People sense increasing danger associated with falling from larger heights because injury severity increases with increasing fall height [33]. Ground, second, and third floor falls are about 2.6, 5.1, 8.8 m, respectively [34]. The German Society for Trauma Surgery's threshold for trauma team activation is a fall height of 3 m [35]. The US Occupational Safety and Health Administration has for decades required protection for heights greater than 1.2 m for general workplace safety [1]. Chalmers et al. [2] argues for 1.5 m maximum fall heights for playground equipment. The Swiss Council for Accident Prevention makes specific recommendations for EFHs below 1.5 m for terrain park jumps requiring basic skills [36]. Even with no standards in Olympic Nordic ski jumps, typical "equivalent landing height" [32] is only about 0.5 m.

EFH h of objects is formally defined as

$$h = \frac{v^2}{2g} \tag{1}$$

where v is impact velocity and g gravitational acceleration. Kinetic energy of objects moving at velocity v is transformed from potential energy at height h; indisputable, fundamental physics.

Beginning from equation 1 equivalent fall heights h can be determined for any surface, i.e., sloped landing profile or shape, after jumping [29]. The result, neglecting air drag, is

$$h = \left[\frac{x^2}{4(x\tan\theta_T - y)\cos^2\theta_T} - y\right]\sin^2\left[\tan^{-1}\left(\frac{2y}{x} - \tan\theta_T\right) - \tan^{-1}\frac{dy}{dx}\right]$$
(2)

a function only of takeoff angle θ_T , impact coordinates (x,y) relative to takeoff, and landing surface slope $\frac{dy}{dx}$, but not a function of takeoff speed [29]. To analyze jumps, one measures Cartesian coordinates of landing surfaces along jumpers' flight paths and takeoff angles. Slopes $\frac{dy}{dx}$ are computed from measured coordinates (x, y). Curvature for the last several meters before takeoffs must be near zero to avoid unintentional inversion, although this does not influence EFHs.

2.2 Software and Online Access

We presented the first version of software for designing ski jumps with a specified EFH in [30]. It comprises a general-purpose, extensible, object-oriented software library with tools for 2D skiing simulation. Using this code, a web application was developed for interactive jump design. The web application is designed for a non-technical end-user and operable on any desktop, tablet, or mobile device supporting a web browser.

We have extended the capabilities of the software in version 1.4.0 (March 25, 2021) to assist work described in this paper. New library features automate calculation of EFH for jump profiles described by a set of Cartesian coordinates. Additionally, a new "analysis" page allows users to upload measured jump profile coordinates in either a comma separated value or Microsoft Excel spreadsheet file. The jump is then analyzed and EFHs are displayed graphically for interactive user manipulation and viewing. Figure 1 shows the web application with one of the case study jumps (Salvini v. Ski Lifts Inc.) loaded for analysis and explains its primary features.

The software is written in Python and directly depends on popular packages including Cython [37], matplotlib [38], NumPy [39], pandas [40], Plotly & Dash [41], pycvodes [42], SciPy [43], SymPy [44], and xlrd. This software is open source and licensed under the MIT redistribution license. The source code is distributed on PyPi ¹. Users can submit bug reports, feature requests, code improvements, and additions at the Gitlab repository ². The software library's documentation is hosted via Read the Docs ³. Basic examples of using the library are provided in the documentation and this paper's supplementary materials. We have also made the web application available for free use online. ⁴

We do not view the software as the definitive ski jump design and analysis tool, but rather as a foundation. The tool has been released as open-source so that refinements and modifications are easy and encouraged. The software was carefully designed with extensibility and modularity in mind. New surface shapes such as different takeoff ramps are easily added by building upon the basic surface object using object-oriented programming principles. Similarly, new skier models can be added that incorporate more complex biomechanical features and actions. We make use of this flexible software design for the web application and for the calculations and visualizations presented in the following section.

¹https://pypi.org/project/skijumpdesign

²https://gitlab.com/moorepants/skijumpdesign

 $^{^3}$ https://skijumpdesign.readthedocs.io

⁴http://www.skijumpdesign.info



Figure 1: Screenshot of the ski jump design and analysis web app To use the analysis portion of the app, a user selects "Ski Jump Analysis" from the primary menu [1], uploads a .CSV or .XLS file by dragging it onto the screen [3], inspects the input data for accuracy in the table [4], sets the takeoff angle [5], runs the analysis by pressing the "Run Analysis" button [6], views results in an interactive plot [2], and downloads results by pressing the "Download EFH" button [7].

3 Results

In these case studies of American lawsuits, juries ruled for injured plaintiffs.

Negligent jump design and construction contributed significantly to injuries [45,
46]. Simulations below use methods in [3], assuming the same skier mass, frontal
area, and drag coefficient of 75 kg, 0.34 m², and 0.821, respectively.

46 3.1 Vine v. Bear Valley Ski Company

In April 2000, Ms. Vine's lower spine was injured when she landed badly skiing a jump at Bear Valley in California. The jump shape (Fig. 2) was a common form called a "table-top". Builders intend that jumpers completely clear the table, landing on down-slopes near a "sweet spot". The upper panel of Fig. 2 shows the measured jump surface from accident investigation. Vine landed short of the knuckle (end of the table-top). This table-top, typically flat and horizontal, was instead concave, compounding dangers of short landings. At the 11 m landing horizontal distance measured from takeoff, the surface sloped upwards approximately 5°. The concave shape emphasizes detrimental effects of not aligning surface tangents closer to jumper flight paths at impact.

The lower panel displays EFHs at different landing locations, which are greatest just short of the knuckle. At the sweet spot, just past the knuckle, EFHs drop precipitously to about 1 m although landing in this narrow region requires jumpers to control takeoff speeds within 1 m s $^{-1}$. Landing at 11 meters, Vine's EFH was almost 4 meters, equivalent to falling from between one and two stories [34]. She had also rotated backward in flight, landed on her lower spine and was paralyzed. A lower EFH could have decreased likelihood of injury, due to lower impact forces.

In contrast, landing surfaces designed to have smaller EFHs can be created at similar cost. The green jump profile in the upper panel of Fig. 2 shows a possible jump design, see [3], of similar size with similar flight times that ensures constant (smaller) EFHs of about 1 m. The convex shape of this jump is interestingly close to the original concave table-top inverted, showing that convex landing shapes are critically important for limiting EFHs. This alternative jump design would have lowered impact forces for landings at all locations. In 2002, the jury ruled in favor of Ms. Vine, agreeing that Bear Valley was responsible for providing unsafe jumps.

3.2 Salvini v. Ski Lifts Inc.

In 2004, Mr. Salvini attempted a table-top jump on skis in the terrain park of The Summit at Snoqualmie Ski Resort, in Washington state. Salvini overshot the intended landing location while traveling at typical skiing speeds [47], rotated backward during flight and landed on his back, ultimately suffering quadriplegia. The jury sided with Mr. Salvini and he was awarded a judgment of \$14M.

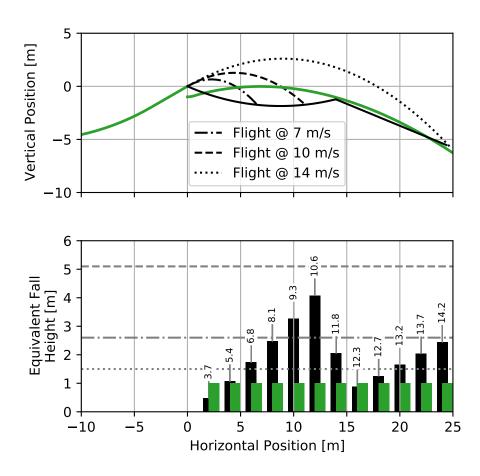


Figure 2: Bear Valley jump compared to possible safer design Top: Measured landing surface (solid black) and jumper flight paths (intermittent black) from measured 30° takeoff angle. A 14 m s⁻¹ takeoff speed is used as the design speed [3] for a comparison jump (solid green) shaped to have constant EFH of 1 m. Bottom: EFH for both jumps in corresponding colors at 2 m intervals. Numbers above bars indicate takeoff speeds required to land at that location. Intermittent horizontal gray lines indicate increasing relatable fall heights: knee collapse, average 1st story fall, and average 2nd story fall.

At his landing location of 30 m the EFH exceeded 10 meters, approximately a 3-story fall. Figure 3 shows the measured jump surface from the accident investigation. For takeoff speeds greater than $13~{\rm m\,s^{-1}}$, the lower panel shows that the EFH is greater than 10 m and growing linearly with larger takeoff speeds. Severe injury is almost certain in falls this high, especially if landing body orientation loads the spine, as in this case.

The upper panel also shows a jump profile (green) designed to have a 1 m EFH for all speeds below $16~{\rm m\,s^{-1}}$. This profile requires significantly more snow than the measured jump but alleviates dangerous impacts. This jump highlights how extreme EFHs can become if jumps are not properly designed. Few recreational skiers will jump out three story windows, snow or not. Injuries are clearly likely. Our internal altimeter tells us so, but it's not easy to discern when visually assessing a jump's safety.

These two case studies clearly demonstrate that deficient jump landing shapes have devastating consequences and that engineering analysis and design, based on laws of mechanics, can be used to shape jump landings that limit EFHs. Designing jumps this way is based on well-established, centuries-old mechanics of Isaac Newton and Émilie du Châtelet [48], a fundamental of physics and engineering education. Designing jumps to limit EFHs unquestionably reduces injury risks by reducing impact energies and associated forces.

4 Discussion

4.1 Moral Imperative

"Hold paramount the safety, health and welfare of the public" [49], is the first canon of engineering ethics. Ethics is not a matter of opinion and should not be optional. It is the foundation for engineering. The first canon compels engineers to use their technical expertise to protect snowsport participants from injuries. Reducing EFHs cannot increase likelihoods of injuries. Building well designed, safer jumps is no more laborious than building poorly designed, unsafe jumps. There is no reason not to control EFHs with good design methods. Nonetheless skiing industries and their insurance companies are reluctant to adopt and endorse such design methods, choosing instead to invest in litigation defense rather than technologies for constructing safer jumps. They hire engineers to profess doubt on the fundamental physics of EFHs during litigation. Publications cited in litigation to support these doubts provide little or nothing for the safety, health, and welfare of the public, that engineers should hold paramount.

In their book "Merchants of Doubt" [50], Oreskes and Conway have studied this problem more generally. They show that in numerous industries over the last 60 years, scientific evidence accumulated that commonly accepted industrial activities were harmful, either to individuals or society. However, industries had vested interests in continuing practices that were dangerous to the public, because operational changes would have led to significant, short-term costs. Examples carefully described and analyzed [50] include using DDT, smoking

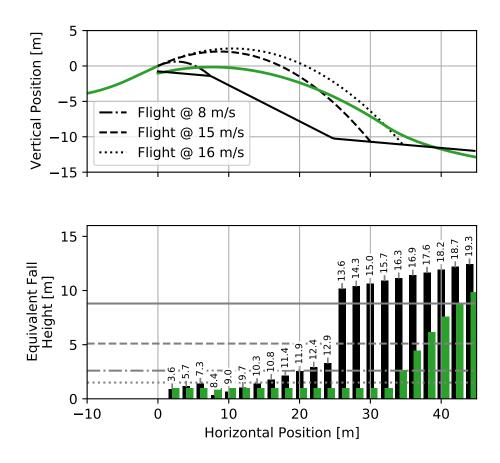


Figure 3: Snoqualmie jump compared to possible safer design Top: Measured landing surface (solid black) and jumper flight paths (intermittent black) for measured 25° takeoff angle. The 16 m s⁻¹ takeoff speed is used as the design speed for a comparison jump (solid green) with constant EFH of 1 m. Bottom: Equivalent fall height for both jumps in corresponding colors at 2 m intervals. Numbers above bars indicate takeoff speed required to land at that location. Intermittent horizontal gray lines indicate increasing relatable fall heights: knee collapse, average 1st story fall, average 2nd story fall, and average 3rd story fall.

tobacco, producing acid rain from coal-fired power plants, causing ozone holes from CFCs, damaging health with second-hand tobacco smoke, and changing our climate with CO2 emissions. Rather than using proven science as a basis for changes in practice, strategic responses of industries have been to "emphasize the controversy among scientists and the need for continued research" [50].

This same strategy is used by the snowsport industry and its defense experts, who disparage EFHs. To sow doubt and counter solid, fundamental, scientific concepts of landing hill design limiting EFH, defense experts introduce confounding factors to cloud and confuse basic issues. Consider as evidence three papers [51, 52, 53] co-authored by well-known skiing industry defense experts who have testified for snowsport resorts and their insurance companies. We do not fundamentally question their empirical findings but we do reject their interpretation of the findings, namely their conclusion that greater fall height is not a cause of greater injury.

Shealy et. al [51] conducted an experimental study attempting to test the hypothesis that takeoff speed is a predictor of the distance from a jump take-off to landing. They reached the mechanically impossible conclusions both that there is "no statistically significant relationship between takeoff speed and the distance traveled" and that "takeoff speed is not a dominant or controlling factor (in how far a jumper travels)" [51]. These conclusions were used to question the soundness of analytical mechanical modeling of jumper flight used in [23, 26].

Some of these same authors later vouched for terrain park jump safety. Using data held by the National Ski Areas Association (NSAA), Shealy et. al [52] concluded that their "hypothesis that jumping features resulted in an increase risk of injury [was] not ... substantiated." [52] This is the only study we are aware of with this conclusion. It is difficult to reconcile it with the voluminous contradictory research documenting the unique dangers posed by terrain park jumps in tens of other studies cited both herein and in [23, 24, 26, 27, 28, 3, 29, 30]. Although NSAA releases yearly totals of resort-related fatalities and catastrophic injuries, the raw data on which [52] was based is not even publicly available. The data was collected from press releases produced by the NSAA [52], which has an inherent conflict of interest, thus making these results unverifiable.

In a third experimental study (N=13) specifically designed "to evaluate injury mitigation potential of surfaces limiting EFH" [53], Scher et al. clearly show that body orientation, i.e. falling directly on one's head (in all trials), can cause dangerous cervical spine compression loads [53], even at low fall heights. They report on effects of EFH but only test heights from 0.23 m to 1.52 m, committing a similar fault as in [51], restricting ranges of their independent variables, and ignoring fall heights known to have caused severe injuries regardless of body orientation. Yet, they insinuate that EFH has no appreciable effect on injuries. The title, "Terrain Park Jump Design: Would Limiting Equivalent Fall Height Reduce Spinal Injuries?" implies that they appear to believe that falling from greater heights might not cause greater injuries. Why propose such mechanically flawed hypotheses? Sowing doubt on EFH as an indicator of risk appears to be paramount.

Extending the scope of the findings in these ways are common mistakes, but ones that should not be made by professional engineers. Fundamental laws cannot be disproved by these kinds of jumping experiments. If statistical or experimental results seem in conflict with predictions from classical mechanics, the problems are most certainly with the statistical or experimental design or their interpretations, but not fundamental laws of mechanics. Defending practices that lead to injuries helps prolong these dangerous practices, which leads to further injuries, clearly contradictory to ethical engineering. Ski industry defense engineering experts are complicit in the continued societal damage. As Upton Sinclair wrote "it is difficult to get a man to understand something when his salary depends on his not understanding it" [54].

It is not evident that these papers [51, 52, 53] "hold paramount the safety, health and welfare of the public". They are silent on how their findings can be used to reduce injuries. They obscure a scientifically fundamental, mechanically irrefutable fact that impacting surfaces at lower normal velocities is safer. They "create the appearance that the claims being promoted were scientific" [50, page 244]. Fundamental laws have made mechanics a science. Findings that contradict such fundamental laws should be carefully scrutinized and review processes accepting such articles should be questioned.

Organizations also merchandise doubt. A decade ago, NSAA argued [55] that, because of rider and snow variability, terrain park jump "standards are essentially impossible." While it is true that the "virtually ... infinite number of ways that a given feature may be used by an individual ... varying speed, pop, body movement, takeoff stance, angles of approach, the attempting of different kinds of maneuvers, landing stance, and the type of equipment used (skis or snowboard) ... create a wide variety of experiences for the users" [55], none of these in fact preclude analysis or design. This was shown clearly in reference [25] which examined quantitatively the effects of variations in factors actually involved in the mechanics: takeoff speed, snow friction, air drag, tail wind, snow melt and jumper pop. These so-called "uncontrollable factors" fell into three groups: (1) those for which there is zero sensitivity, i.e., an uncontrollable factor that makes no difference in the ability of the designed jump to deliver the designed EFH; (2) those for which fairly large parameter variations cause only insignificant maximum deviations in EFH, and (3) those for which the factor can be taken into account in the design process itself and its larger effect on EFH completely eliminated in the unsafe direction. The allegation that design of limited EFH surfaces is prevented by the complexity of the problem and by the large number and types of parameter variations away from nominal is false; in fact the allegation is just more merchandised doubt.

In snowsport injury cases, testifying for injured plaintiffs and testifying defending corporations are not ethically equivalent. The former attempts to address problems that cause injuries, holding paramount the public's safety, health and welfare. The latter attempts to defend practices that might have contributed to the injury, to limit financial losses of corporations. The idiom "two sides to every question", is not appropriate in science and engineering [50, page 268].

Engineers whose scholarly work ignores engineering's first canon of ethics in favor of merchandising doubt can diminish the scientific integrity of engineering journals and engineering conferences. Journal editors should recognize papers primarily intending to cast doubt on good science and engineering for what they are, tools of insurance companies for defending civil suits, and reject them. Papers helping to perpetuate dangerous practices do not belong in engineering journals or conference proceedings.

4.2 What Can Be Done?

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Absolutely, the most important change will be to incorporate rigorous, rational processes and scientific principles that consider mechanical impact safety into designing freestyle jumps. At present a large fraction of, if not most, jumps in the USA are created in a formulaic way using two straight lines, a horizontal deck (tabletop) and nearly constant-slope landing region, linked by a curved knuckle. This design philosophy is recommended in the instructions provided by the NSAA [56] and is presumably followed by their members. Although such jumps are simple and thus easy to design, previous research has shown that jumps with bi-linear geometry have generally poor EFH behavior [24], i.e. that they can have low EFH only in a small region just past the knuckle (called the "sweet spot"). In the more recent version of their freestyle terrain park notebook [56], the jump landing area is even termed the "landing plan" because it is envisioned to be planar! There is no reference whatsoever to any concept such as EFH or similar measure of impact or its effect on safety because the NSAA's strategy is to put the responsibility for safety fully on the jumper. There is no quantitative consideration of jump impact safety (e.g. from the point of view of EFH) beyond seat-of-the-pants experience of the designer. The skiing industry continues to resist more scientifically-based rational approaches to design, in spite of the fact that computer aided design (and even computerassisted fabrication and maintenance) of snow park jumps (see Figure 4) has been available from snow groomer manufacturers for more than 5 years [57]. The 2015 NSAA reference in [56] still contained the statement that "Standards are essentially impossible ...".

Once the jump surface has been designed, the next most important change is to build accurately what was designed. Presently a dominant fraction of jumps are simply fabricated by groomer operators, based on perhaps a few measurements of distances and slopes (deck length, takeoff angle, landing region angle and length) during the process. But the design concepts are overly simple and do not incorporate or address quantitative indicators of safety such as EFH. The introduction of computer controlled grooming (see Figure 4), similar to computer aided manufacturing (CAM), will facilitate precise construction of more complex designed shapes. These would include the non-trivial constant EFH surfaces provided by our online ski jump design software that limit landing impulses to acceptable levels.

Every jumper (and parent of young jumpers) should be able to confirm that a jump is safe before trying it. Appropriate inspection, evaluation, and cor-

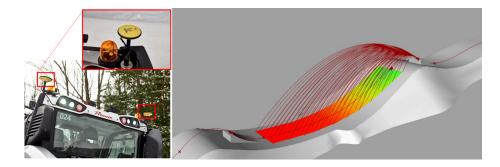


Figure 4: Commercial availability of computer-aided design and computer-controlled fabrication of snow park surfaces began as early as 2016. The right panel shows Prinoth's computer generated 3-D jump landing surface with their family of simulated jumper paths, even ones outside the central vertical bisecting plane, with the landing surface colored corresponding to the EFH incurred by the jumper at that landing point. The left panel shows a computer-controlled snow groomer fitted with two GNSS receivers that allow real time measurement of their position to an accuracy of about 2 cm, calculation of the yaw and roll of the groomer blade, and precise closed loop control of the snow addition and removal process. Images courtesy of Prinoth, supplier of snow groomers for the winter Olympics in China 2022.

rection of existing jumps, and the design and construction of safer new jumps should be promoted. Postings should be required and include EFHs, the certified inspectors name, and when last inspected. Inspections should be frequent enough to ensure that jumps meet the standards, particularly regarding take-offs and starting points to prevent inadvertent inversions. Standards need to be developed that limit EFHs in collaboration between industry and research engineers to design, build, inspect, maintain, and post safer jumps. An example of first steps in this area is a terrain park safety guide by the Swiss Council for Accident Prevention [36].

To complement standards, certification programs are needed for jump building, inspection, and maintenance. As an example of a successful certification program, around 1980 ASTM Committee F27 began to develop ski binding standards. Proponents were led by orthopedic surgeons and academic researchers [58]. Industry argued that standards were impossible because release value measurement was impossible by ski shops (industry now makes similar arguments about jumps [56]). Nevertheless certifications and inspection standards for bindings were developed, which led to fewer lower-extremity equipment-related injuries [58]. But now no medical professionals and almost no academics remain in F27. Efforts to create similar standards for terrain park ski jumps began in F27 more than a decade ago [59], yet no standards have yet been developed. The US skiing industry, aided by the NSAA, has been successful in delaying the implementation of standards.

In parallel with standards development, assessing and possibly reshaping existing jumps to eliminate dangerous EFHs should be an straightforward route for ski resorts to proactively increase terrain park safety. Accurate enough measurements of existing surfaces can occur even with simple tools, e.g. tape measure and digital level, and consume relatively little time and effort per jump (see supplementary materials for details). Calculation and visualization of EFHs from these measurements can take some time without a computational program for calculating EFHs from hill profiles. The user-friendly, freely-accessible open-source online web application tool that we have made available for jump designers and builders has almost instantaneous calculation and visualization steps, solving this problem.

With this software jump builders can easily add safety assessment to their toolbox, even accessing it from a smartphone or tablet on hills. We see no reason that this basic assessment should not be part of jump construction processes. The only ethical decision is to adopt these methods; saving even one person from a life of paralysis, or even death, must be worth the relatively minor inconvenience of shaping jumps using the methods in reference [3].

5 Conclusion

There are, of course, more factors than jump takeoff and landing surface shapes that contribute to injuries on terrain park jumps. Yet normal impact velocity can be easily controlled with a properly designed and fabricated landing surface shape. There is no evidence that decreasing designed EFH increases injuries in falls; injuries only decrease. Thus we see no reason not to adopt constant low values of EFH for public-use jump designs. Fabricators of jumps that are not designed as forgiving environments are negligent. Public safety must be held paramount to short-term return-on-investment.

The methods implemented in the software illustrated in Section 2.2 provide a starting point for realizing EFH-conscious designs in terrain parks. We hope to see the design and analysis adopted by commercial grooming equipment manufacturers so that safety is made integral to jump design. Our software can grow and evolve through contributions from other researchers to incorporate many other nuances of injury prevention. We also see the methods providing a structure for standards development. And minimally, we see the software as an immediately usable tool for jump fabricators in the field.

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$_{\scriptscriptstyle 18}$ Declarations

- Funding Not applicable
- Conflict of interest MH served as a plaintiff's expert witness in the two case
 studies discussed above and in numerous other similar cases since. CB
 testifies occasionally on behalf of plaintiffs in ski and snowboard injury
 cases. He has collaborated with Shealy and C. D. Mote, Jr., Sher's doctoral advisor, on ski safety research, has participated in ASTM F27 since
 the 1980s on standards for bindings, boots, and skis, and holds patents on
 ski and snowboard binding designs intended to reduce injuries.
- Availability of data and material All data is available at https://gitlab.

 com/moorepants/skijumpdesign and https://gitlab.com/mechmotum/
 ski-jump-analysis-paper.
- Code availability The skijumpdesign version 1.4.0 source code is archived at

 https://doi.org/10.5281/zenodo.4637076. Additionally, it and the
 paper's source code is available at https://gitlab.com/moorepants/
 skijumpdesign and https://gitlab.com/mechmotum/ski-jump-analysis-paper.
- Author's contributions JM and MH contributed to the study conception and
 design. Material preparation, data collection and analysis were performed
 by JM and MH. The first draft of the manuscript was written by JM,
 BC, MH, and CB. MH and CB were primarily responsible for drafting the
 parts on merchandising doubt and ethics, respectively. All authors read
 and approved the final manuscript. BC and JM wrote the accompanying
 software.
- 441 Ethics approval Not applicable
- 442 Consent for publication JM, BC, MH, and CB consent for publication.

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- Supplementary Materials for Online Software Allows Ethical Safety-Conscious Design of
- Terrain Park Jumps
- Jason K. Moore Bryn Cloud Mont Hubbard Christopher A. Brown
 - September 15, 2021

1 Example Software Library Use

The closed form equation

$$h = \left[\frac{x^2}{4(x\tan\theta_T - y)\cos^2\theta_T} - y\right]\sin^2\left[\tan^{-1}\left(\frac{2y}{x} - \tan\theta_T\right) - \tan^{-1}\frac{dy}{dx}\right]$$
(1)

is useful for understanding the fundamental relationship of equivalent fall height (EFH) to the landing surface shape. It will predict EFH for small jumps but other factors may be useful to include in the model. For example, jumpers are subject to aerodynamic drag and this is not negligible for larger jumps. If 11 drag is included there is no closed form solution for the EFH, but the EFH can 12 be computed through iterative simulation [1]. The jumper's flight path is found 13 by integrating the flight equations of motion at various takeoff velocities and 14 computing the misalignment of jumper landing and slope angles to then compute the EFH. This more general simulation method is implemented in the software described herein and the results reflect the inclusion of both gravitational and drag forces. Even with drag incorporated, the calculating EFH still only require measurements of the landing surface cross-sectional profile coordinates (x,y)relative to the takeoff point and a measurement of the takeoff angle. Listing 1 20 demonstrates the new software library features creating a surface from some 21 measured data points and then calculating the EFH at 0.2m increments.

2 Jump Shape Measurement

Calculating EFH requires the Cartesian coordinates and slope of the landing surface along the path of the jumper. There are a number of possible measurement techniques for collecting data adequate for the EFH calculation but the

```
>>> import numpy as np
>>> from skijumpdesign import Surface, Skier, plot_efh
>>> takeoff_ang = 10 # degrees
>>> takeoff_point = (0, 0) # (x, y) in meters
>>> x_ft = np.array([-232.3,-203.7,-175.0,-146.3,-117.0,-107.4,
       -97.7,-88.0,-78.2,-68.5,-58.8,-49.1,-39.4,-34.5,-29.7,
       38.8,43.3,47.8,52.3,56.8,61.5,66.2,70.9,75.7,80.6,85.5,
. . .
. . .
       88.4,88.4])
>>> y_ft = np.array([55.5,46.4,37.7,29.1,22.2,19.7,17.2,14.8,
      12.5,10.2,7.7,5.2,2.9,1.8,0.7,-0.2,-1.0,-1.2,-1.4,-1.6,
      -16.2,-18.1,-19.8,-21.4,-22.9,-24.0,-25.0,-25.6,-25.6])
. . .
>>> x_mt = x_ft*0.3048 \# convert to meters
>>> y_mt = y_ft*0.3048 # convert to meters
>>> # create a surface from the data
>>> measured_surf = Surface(x_mt, y_mt)
>>> # create a skier
>>> skier = Skier(mass=75.0, area=0.34, drag_coeff=0.821)
>>> # calculate the EFH
>>> x, efh, v = measured_surf.calculate_efh(
       np.deg2rad(takeoff_ang), takeoff_point, skier, increment=0.2)
>>> x # display the x coordinates
array([ 0. , 0.2, 0.4, 0.6, 0.8, 1. , 1.2, 1.4, 1.6, 1.8, 2. ,
       2.2, 2.4, 2.6, 2.8, 3., 3.2, 3.4, 3.6, 3.8, 4., 4.2,
       24.2, 24.4, 24.6, 24.8, 25., 25.2, 25.4, 25.6, 25.8, 26., 26.2,
       26.4, 26.6, 26.8])
>>> efh # display the EFH for each x coordinate
array([0. , 0.02541035, 0.03479384, 0.03264587, 0.05956476,
       0.09096091, 0.12358184, 0.13702364, 0.15202999, 0.17018343,
       3.93910556, 3.97387212, 4.00891899, 4.04424779, 4.07984952,
       4.11573359, 4.68049185, 5.53413479, 6.45253722, 7.42628019])
>>> v # display takeoff speeds to reach x positions
array([0.07373847, 0.13081777, 0.1878382 , 0.2447865 , 0.30166299,
       0.35851949, 0.41537661, 0.47221055, 0.52897197, 0.58564902,
       6.71699974, 6.76760188, 6.81816819, 6.86869777, 6.9191902 ,
       6.96962124, 7.02001551, 7.07037288, 7.1206941 ])
>>> # calculate and plot the efh curve
>>> plot_efh(measured_surf, takeoff_ang, takeoff_point, increment=0.2)
```

Listing 1: Python interpreter session illustrating how one could compute the EFH of a measured jump.

simplest method requires only a digital level ¹, a flexible tape measure, and less than an hour's time from one person per jump. A tenth of a degree accuracy from the level and down to 25 cm accuracy from the tape measure should be more than sufficient for typical snowsport jumps.

To measure the jump, the takeoff point should be identified and the tape measure should then be draped over the contour of the landing surface along the projection of the expected flight path onto the landing surface. The origin of the tape measure should be aligned with the takeoff point. Starting with the takeoff point, the digital level should be used to record the absolute angle at regular increments along the tape. The increment can be varied between 25 cm and 100 cm, with the former used for steep slope changes and the later for less steep; 50 cm increments are appropriate for average jump shapes. Positive angles should be recorded for positive slope and negative angles for negative slope. The tabulated data should include the distance along the surface from the takeoff point, d_i , and the associated surface angle, θ_i , at each distance measurement for n measurements. Assuming θ_i is in radians, the Cartesian coordinates can be computed using the average angle to find the adjacent coordinates. The following equations show the calculation of the Cartesian coordinates from these two measures used in the software.

$$\frac{dy_i}{dx_i} = \tan^{-1}\theta_i \quad \text{for } i = 1\dots n$$
 (2)

$$x_{i+1} = \begin{cases} 0 & \text{for } i = 0\\ x_i + (d_{i+1} - d_i) \cos \frac{\theta_{i+1} + \theta_i}{2} & \text{for } i = 1 \dots n - 1 \end{cases}$$
(3)

$$\frac{dy_i}{dx_i} = \tan^{-1}\theta_i \quad \text{for } i = 1 \dots n$$

$$x_{i+1} = \begin{cases} 0 & \text{for } i = 0 \\ x_i + (d_{i+1} - d_i)\cos\frac{\theta_{i+1} + \theta_i}{2} & \text{for } i = 1 \dots n - 1 \end{cases}$$

$$y_{i+1} = \begin{cases} 0 & \text{for } i = 0 \\ y_i + (d_{i+1} - d_i)\sin\frac{\theta_{i+1} + \theta_i}{2} & \text{for } i = 1 \dots n - 1 \end{cases}$$
(4)

Listing 2 demonstrates calculating the landing surface's Cartesian coordi-31 nates from measured distance and angle data collected with the method de-32 scribed above. 33

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¹Smartphone digital level measurement applications are likely sufficient and readily available.

Listing 2: Python interpreter session showing how one could compute the Cartesian coordinates from EFH of a measured jump.