

Multiclass Damage Identification in a Full-scale Bridge using Optimally-tuned One-dimensional Convolutional Neural Network

Sandeep Sony¹, Sunanda Gamage², Ayan Sadhu³, and Jagath Samarabandu⁴

¹PhD (Corresponding Author), Department of Civil and Environmental Engineering, Western University, Canada. Email: ssony@uwo.ca

²PhD Student, Department of Electrical and Computer Engineering, Western University. Email: sgamage2@uwo.ca

³Assistant Professor, Department of Civil and Environmental Engineering, Western University, Canada. Email: asadhu@uwo.ca

⁴Professor, Department of Electrical and Computer Engineering, Western University. Email: jagath@uwo.ca

ABSTRACT

In this paper, a novel method is proposed based on a windowed one-dimensional convolutional neural network (1D CNN) for multiclass damage identification using vibration responses of a full-scale bridge. The measured data is first augmented by extracting samples of windows of raw acceleration time-series to alleviate the problem of a limited training dataset. 1D CNN is developed to classify the windowed time-series into multiple damage classes. The damage is quantified using the predicted class probabilities, and the damage is localized if the predicted class is equal to the assigned damage class, exceeding a threshold associated with majority voting. The proposed network is optimally tuned with respect to various hyper-parameters such as window size, random initialization of weights, etc., to achieve the best classification performance using a global 1D CNN model. The proposed method is validated using the Z24 bridge benchmark data for multiclass classification for two different damage scenarios, namely, pier settlement and rupture of tendons,

24 under the various extent of the damage. The damage identification is carried out on various bridge
25 components to collectively identify the structural component with a damaged signature. The results
26 show that the proposed windowed 1D CNN method achieves an accuracy of 97%, and performs
27 well with different types of damage.

28 **INTRODUCTION**

29 In civil infrastructure, continuously increasing heavy traffic, unexpected natural calamities
30 and human-made damages reduce their load-bearing capacity and service life. With ageing, the
31 structures exhibit various damage signatures in several critical locations. In the absence of timely
32 repair and maintenance, progressive damage leads to the collapse of structures. Despite the
33 simplicity, the traditional manual inspection suffers difficulty while scanning the inaccessible areas
34 in large structures such as bridges or tall buildings. Over the past few decades, structural health
35 monitoring (SHM) has been a promising tool to supplement the knowledge of structural integrity
36 over time. However, efficient diagnosis and prognosis of large-scale infrastructure require a reliable
37 assessment of its damage under in-service conditions. SHM aims to provide suitable diagnostics
38 and prognosis, and assist infrastructure owners and decision-makers in maximizing the safety,
39 serviceability, and functionality of critical structures. An autonomous SHM will allow efficient
40 and cost-effective disaster management and will lead to resilient infrastructure with faster recovery
41 under natural disasters. In this paper, an autonomous multiclass damage identification method is
42 proposed by utilizing artificial intelligence in the sequential data, such as vibration measurements.

43 Data-driven damage diagnosis is a critical component of infrastructure asset management
44 (Piryonesi and El-Diraby 2019). Although there is a plethora of research on parametric methods
45 based on time-frequency (TF) decomposition techniques (Staszewski and Robertson 2006, Sadhu
46 et al. 2017, Almasri et al. 2020, Barbosh et al. 2020, Kankanamge et al. 2020, Sony and
47 Sadhu 2020, Sony and Sadhu 2021), non-parametric methods (Nakamura et al. 1998, Wang
48 and Ong 2015, Abdeljaber and Avcı 2016) have shown significant promises in data-driven SHM
49 methods. Parametric methods include extracting dynamic parameters such as modal parameters,
50 while inferring the change in these parameters to detect any possible changes in the structures. On

51 the other hand, non-parametric methods include extracting parameters that are estimated based on
52 the computational models, where the parameters are mathematically derived in a statistical sense.

53 Structural damage identification can be considered as a pattern recognition-based non-parametric
54 problem, which is divided into three stages, namely, data acquisition, feature extraction, and feature
55 classification. With proliferation of various machine learning (ML) algorithms, the SHM com-
56 munity has prominently used various supervised learning algorithms (Hou and Xia 2020, Avcı et
57 al. 2021). In (Gardner et al. 2020), the authors explained the interface between nondestructive
58 evaluation and machine-learning-based SHM for damage detection. In another study, Su et al.
59 (2020) presented a critical review of field monitoring of high-rise structures. The study reviewed
60 techniques for comfort assessment, seismic and wind effects, and environmental effect on monitor-
61 ing of super-tall structures. Recently, the SHM community has explored both vibration and image
62 data for structural damage identification and localization.

63 With advancements in artificial intelligence, image-based SHM has garnered as an inexpensive
64 way to monitor large scale structures using Convolutional Neural Networks (CNNs). While image-
65 based 2D CNN techniques remain a popular method for SHM (Kumar et al. 2019, Chang and Chi
66 2019, Gulgec et al. 2019, Sony et al. 2019), they involve significant complexity in obtaining a
67 large amount of labelled data, pre-processing and classifying the images. As a solution, researchers
68 have studied algorithms that directly operate on the sequential data such as vibration data. Guo
69 et al. (2014) proposed sparse coding as a feature extraction method for unlabeled acceleration
70 measurements obtained from wireless sensors. The damage classification was carried out using
71 a CNN, and the results were compared with logistic regression and decision trees. A three-span
72 bridge was considered to evaluate the efficacy of the proposed method, and it was shown that sparse
73 coding-CNN based method outperforms other methods with an accuracy of 98%. Gulgec et al.
74 (2017) conducted a simulation study on a steel gusset plate connection by varying the size and
75 location of the damage. A CNN was used to classify damaged signals, and the proposed method
76 achieved a testing error of 2% and showed robustness against environmental noise.

77 Fallahian et al. (2018) explored the applicability of dynamic features such as mode shapes,

78 frequency response functions, and natural frequencies as damage indicators under varying tem-
79 peratures. The authors used a combination of coupled sparse coding and deep neural network as
80 an ensemble method for damage detection and localization. The proposed method was validated
81 on a numerical truss bridge and experimental benchmark dataset. Bao et al. (2019) proposed a
82 CNN-based anomaly detection using acceleration measurements by converting them into grayscale
83 images. The authors used several anomaly parameters such as missing, minor, outlier, square,
84 drift, and trend data points to train the datasets using a stacked autoencoder architecture. In another
85 recent study, Shang et al. (2020) proposed deep convolutional denoising autoencoders for structural
86 damage detection. The proposed method extracted damage features from field measurements under
87 environmental noise. However, most of these methods are based on 2D CNN (Sony et al. 2021),
88 which are primarily relied on images.

89 **RECENT DEVELOPMENT OF 1D CNN-BASED SHM**

90 Recently, 1D-CNN has shown promising results in capturing the temporal information and
91 damage detection using vibration data. For example, Abdeljaber et al. (2017) introduced 1D CNN
92 for real-time vibration-based damage detection. The authors trained 1D CNN on a vibration signal
93 database obtained from a truss, named Qatar Grandstand, by damaging each joint and keeping the
94 other joints undamaged. The proposed model was trained individually on each joint, and near-
95 perfect classification accuracy was proposed. However, the proposed method was not tested for a
96 multiclass damage scenario. Zhang et al. (2019) utilized the computational powers of 1D CNN
97 to detect changes in structural parameters such as stiffness and mass. Three different structural
98 components were used for data acquisition and model validation, namely, T-shaped steel beam,
99 short and long steel girder bridge, and a mean classification accuracy of 98% was achieved. In
100 another study, Ni et al. (2019) showed the applicability of 1D CNN with autoencoders for anomaly
101 detection under data compression. The proposed algorithm was validated using a long-span
102 suspension bridge with an accuracy of 97.53%.

103 A recent study by Azimi and Pekcan (2020) explored the concept of transfer learning in
104 vibration measurements. The authors used a four-story IASC-ASCE SHM model for numerical

105 training, and the proposed model was tested on experimental studies using IASC-ASCE SHM
106 benchmark building and the Qatar University Grandstand Simulator with an accuracy of 90-100%.
107 Recently, Sharma and Sen (2020) showed the applicability of 1D CNN for damage detection in
108 the structural frames. Experimental validation was performed on a 2D-steel frame with different
109 damage location and severity of the damage. The method was shown to identify different damage
110 scenarios and the false-positive rate was also evaluated and found to be well within the acceptable
111 limits. Furthermore, Liu et al. (2020) conducted a study by integrating traditional TF methods
112 with the capability of neural networks. The authors used transmissibility function-based 1D CNN
113 to effectively identify damage at the ASCE SHM benchmark structure. The proposed method was
114 compared with the time-series and fast Fourier transform-based frequency-domain information,
115 where the TF signals exhibited more significant damage-sensitive features.

116 Overall, 1D CNN exhibited superior performance over artificial neural networks (ANNs) in
117 the context of computation efficiency and noise insensitivity for big data (Kiranyaz et al. 2019).
118 Recently, Bao et al. (2020) evaluated a combination of finite element method (FE) and 1D CNN for
119 localizing damage for a jacket-type offshore structure. However, the data was generated synthetically
120 using a finite element model, which might not resemble the actual real-world data with operational
121 and environmental noise contamination. In addition, the damage was induced artificially using the
122 FE model that was clearly distinguishable from an undamaged structure that does not concur with
123 the real-world data. In another recent study, Sarawgi et al. (2020) used 1D CNN for each joint in an
124 experimental setup to identify hypothetical damage simulated using removal or addition of external
125 braces. However, such individual CNN model per damaged node does not scale well to real-world
126 structures with multiclass damages due to computational complexity. Moreover, the need for large
127 datasets and the selection of the appropriate architecture of the network still remain a challenge.

128 The proposed research explores the existing challenges of multiclass damage identification in a
129 full-scale bridge. Unlike the simulated data, the real-world data is limited and noise-contaminated,
130 where multiclass damage localization becomes a significant challenge. In this paper, an enhanced
131 windowed-1D CNN is explored for multiclass damage localization with varying damage severity

132 under different damage scenarios. The issue of the limited dataset is solved by augmenting the data
133 using windowing the acceleration measurements, and the classification results are improved using
134 a novel majority voting approach of a global 1D CNN model. The effectiveness of the proposed 1D
135 CNN model is evaluated using a systematic suite of hyperparameter tuning such as window size,
136 random initialization of weights, and optimum learning rates to show the robustness of the selected
137 optimal architecture of the 1D CNN network.

138 The paper is structured as follows. A brief introduction of the structural damage identification,
139 its need, and a literature review based on 1D CNN techniques are presented first, followed by the
140 theoretical background of the proposed algorithm. The capability of the proposed algorithm to
141 identify multiclass damage, the importance of hyperparameter tuning and various metrics to show
142 the damage parameters of the structures is explained later along with the key conclusions.

143 **PROPOSED METHODOLOGY**

144 **Formulation of 1D CNN**

145 Convolutional Neural Networks (CNNs) are a type of feedforward neural network model that
146 is designed to approximate a function $y = f(x; \theta)$. For classification, the model maps an input x to
147 a category (class) y . The parameters θ are learned to best fit a given training dataset by a gradient
148 descent optimization algorithm (Goodfellow et al. 2017). The most common type of CNNs are 2D
149 CNNs used in the field of computer vision for tasks such as image classification, where the inputs
150 x are matrices (2D-shaped) representing images. 1D CNNs are a simpler variant of CNNs, where
151 the inputs x are vectors (1D-shaped), typically representing a time-series. They are commonly used
152 for tasks involving sequential signal processing such as speech recognition (Kiranyaz et al. 2019).
153 Since the last few years, 1D CNNs became popular in SHM due to its computational simplicity in
154 comparison to its parent family of 2D CNNs as it requires simple array application and a shallow
155 network.

156 A typical 1D CNN architecture used in this study is shown in Fig. 1. It consists of an input
157 layer (time-series), multiple alternating convolutional and pooling layers, and one or more fully
158 connected layers at the end. An input time-series x presented to the input layer is transformed by

159 the forward pass through the hidden layers and the output softmax layer produces the class label y .
 160 When the number of hidden layers is high, this architecture is referred to as a deep convolutional
 161 neural network. The convolutional layer is the core building block of a CNN. The parameters of
 162 each convolutional layer consist of a set of learnable kernels, which are defined by a kernel length
 163 (m). Convolutional layers have a reduced number of parameters in comparison to fully connected
 164 layers as a single kernel shares the weights for spatial locations in the input. The convolution
 165 process can be expressed as Eq. 1 (Goodfellow et al. 2017):

$$166 \quad y(n) = f(x(n) \otimes h(m)) \quad (1)$$

167 where $x(n)$ is the input vector of length n and $h(m)$ is kernel of length m . The symbol \otimes denotes
 168 the traditional 1D convolution between two signals as defined in Eq. 2,

$$169 \quad x(n) \otimes h(m) = \sum_{k=0}^n x(k)h(n-k) \quad (2)$$

170 The function f is called an activation function, which is typically a non-linear transformation on the
 171 traditional 1D convolution. Non-linear activations enable the network to learn complex mappings
 172 between the input signal and the class labels. In this study, Rectified Linear Unit (ReLU) is used as
 173 the activation function, which effectively removes negative values from an activation map by setting
 174 them to zero. A pooling layer is added after the convolution layer to sub-sample the convolution
 175 output. The pooling operation reduces the dimensionality of a given mapping while highlighting
 176 the prominent feature and it also helps to reduce overfitting. Max pooling refers to selecting the
 177 maximum value in a window that slides over the input map. In Fig. 1, the max pooling layer
 178 has reduced the size of each convolution output size by a factor of two. For the output layer, the
 179 choice of activation function depends on the type of output. For classification problems, SoftMax
 180 activations are preferred. SoftMax function for a n -class problem (representing n probabilities of
 181 input belonging to each of n -classes) is shown in Eq. 3.

$$P(\text{class} = j|z) = \frac{e^{z_j}}{\sum_{k=1}^n e^{z_k}} \quad (3)$$

where z_j is the input to the softmax node j from the previous layer.

Multiclass damage detection using windowed-voted 1D CNN

A method based on a 1D CNN model is proposed to classify the vibration measurement into multiple damage classes (i.e., multiclass classification). First, each acceleration signal is scaled to fit a standard normal distribution. The scaling improves the convergence rate of models trained on the dataset and prevents any outlier from dominating the input (Ioffe and Szegedy 2015). In order to train a neural network to achieve high test accuracy, a large amount of training data is required. Due to the scarcity of vibration-based multiclass data for civil infrastructure, it is critical to augment the training dataset. In the proposed method, the dataset of raw acceleration signals is augmented by extracting windows of samples from the original signals, as shown in Fig. 2. Each extracted window is assigned the same damage level as the original time-series. A new dataset is formed by taking the extracted windows and their labels as the training instances. In addition to increasing the number of training instances, this windowing technique also reduces the data dimensionality (i.e., shorter input signals), which allows training machine learning models with less over-fitting.

The dataset is then split into training, validation and test sets. A 1D CNN model is trained on the dataset using a standard gradient descent optimizer. Hyper-parameters of the 1D CNN model include the number of layers and number of nodes in each layer, activation function and the kernel size in convolutional layers. Additionally, the length of the extracted windows is also a hyper-parameter. Finding the optimal hyper-parameters (also known as hyper-parameter tuning) is conducted using a random search over the parameter space and selecting the configuration that yields the high accuracy on the validation set (Bergstra and Bengio 2012).

In order to classify a new acceleration signal at test time, windows are extracted as before and fed into the trained 1D CNN model, which outputs a set of classification probabilities for each window. The predicted set of classification probabilities $P_p(y_c)$ for a full acceleration measurement

207 is obtained by summing the class probabilities of all the window sequences in a single time-series.
208 The class with the maximum probability is the predicted damage level classification of the series
209 as shown in Fig. 2. It may be noted that this is equivalent to voting for the majority classification
210 label of the individual window sequences to arrive at the prediction based on the entire time-series.
211 Although it is possible for a well-trained model to misclassify some of the individual window
212 sequences that comprise a time-series, the probability of misclassifying a majority of them is
213 very low (Sony 2021). Therefore, the voting process improves the prediction accuracy and other
214 evaluation metrics in the time-series. This result is empirically observed in the full-scale studies
215 and discussed in model performance section. The proposed machine learning pipeline for the
216 multiclass damage classification problem is shown in Fig. 3.

217 **Performance criteria**

218 In machine learning, a number of performance metrics are used to evaluate the efficacy of the
219 computational model. A brief description of metrics used to evaluate classification models in the
220 context of SHM is provided below. The confusion matrix is a tabulation of classifications made
221 by a model, typically with the actual class in rows and predicted class in columns. There are
222 various metrics that are derived from confusion matrix and are presented in Table 1. In the context
223 of SHM and multiclass damage detection, ROC-AUC, Accuracy, FNR and F1 score are used to
224 evaluate the performance of the proposed method. Accuracy is a primary performance metric used
225 to evaluate the ability of a model to correctly classify the data samples into various class labels.
226 Another important metric that has not been discussed in the literature is FNR. In the SHM context,
227 it is critical that a damage detector have a low false negative rate, as a false negative corresponds
228 to the potentially catastrophic case of a damaged signal being classified as an undamaged signal.
229 Furthermore, a damage detector must have high values for accuracy, and F1 score. Additionally,
230 two curves are used to evaluate the trade-off between performance metrics. The receiver operating
231 characteristic (ROC) curve shows the trade-off between True Positive (TP) Rate (TPR) and False
232 Positive (FP) Rate (FPR) as the decision threshold of the classifier varies. The precision-recall (PR)
233 curve shows the trade-off between precision and recall as the decision threshold of the classifier

234 varies. The area under the curves (AUC) for both ROC and PR is a summary metric that reflects
235 the level of possible trade-off. Both curves are useful for an academic and practicing engineer to
236 find a suitable decision threshold.

237 **Algorithm for Component-level Damage Identification**

238 Component level damage is identified for multi-class problems using Algorithm 1. The entire
239 structure is modeled as one experiment rather than modeling each sensor separately as in (Abdeljaber
240 et al. 2017) and prediction probabilities are acquired for each sensor location. This provides control
241 over all the features for one experiment and prevents errors arising from multiple models working
242 on different sensors. However, as there are multiple sensors covering the entire structure, different
243 structural components are collectively used to localize damage using a limited number of sensors
244 for each component. The damage is confirmed if the true predicted probability class is equal to
245 allocated class label for all cumulative windowed series for each sensor location and $P_p(y_c)$ is
246 greater than the threshold.

Algorithm 1: Multiclass damage identification

Input: A signal $x(t)$

Output: Prediction probabilities $P_p(y_c)$ for damage component level identification.

- (a) The acceleration data is pre-processed into multiple windows of time-series and damage class-label is allocated to each windowed data.
 - (b) The structure is modeled as whole (i.e., a global CNN model) as compared to per sensor (Abdeljaber et al. 2017) for computational efficiency and ease of modeling.
 - (c) The windowed data is trained using 1D CNN with optimal parameters (e.g., window size, random initialization of weights etc.) and tested on a separate dataset.
 - (d) The probabilities of classification are obtained for each sensor of every windowed series and damage is confirmed if true predicted probability class of a sensor is equal to allocated class label, while an average of $P_p(y_c)$ for various structural components is used as threshold of damage.
 - (h) If the $P_p(y_c) \geq \text{threshold}$, a localized damaged is confirmed.
-

247 **FULL-SCALE STUDY**

248 **Details of the Z24 Bridge**

249 Damage detection, where classification is more than two classes, is considered as a multiclass
250 problem. In this study, two types of damage cases are considered, namely, rupture of tendons,

251 and pier settlement of a full-scale bridge, namely, Z24 Bridge (Maeck and Roeck 2003). All the
252 damage classes have multiple damage levels are used to evaluate the performance of the proposed
253 method for multiclass damage detection. The bridge was located in the canton Bern near Solothurn,
254 Switzerland. It was a classical post-tensioned concrete two-cell box-girder bridge with a main span
255 of 30 m and two side spans of 14 m, as shown in Fig. 4. The bridge was demolished at the end of
256 1998 because a new railway adjacent to the highway required a new bridge with a larger side span.
257 During the demolition, the bridge data was acquired using 15 accelerometers placed at different
258 spans of the bridge, as shown in Fig. 5. The bridge was excited by two shakers, one at the mid-span
259 of the bridge and another at a side-span. Because of the size of the bridge, response was measured
260 in nine setups of up to 15 sensors each, with three accelerometers and the two force sensors common
261 in all setups. The data was sampled at 100 Hz, and the data was made publicly available by the
262 researchers at the Katholieke Universiteit Leuven (<https://bwk.kuleuven.be/bwm/z24>). The data
263 was acquired by performing various progressive damage scenarios during the demolition period.
264 For the brevity of this study, only two different damage scenarios are considered: rupture of tendons,
265 and pier settlement. It may be noted that each damage scenario have different classes of damage, and
266 they were chosen to evaluate the performance of the proposed method to classify various multiclass
267 damage cases. For example, rupture of tendons have three levels, and pier settlements have four
268 levels, and together they made a case of two separate damage classes. For detailed explanation of
269 how the damages were induced in the bridge, the readers are suggested to refer (Roeck and Teughels
270 2004). The reference undamaged condition is considered as class-zero for all the cases and the other
271 damages were assigned classes starting from 1 to n depending upon the level of damage, as shown
272 in Table 2. For example, in the case of rupture of tendons, the damage was induced at first, rupture
273 of two tendons, and second, rupture of four tendons, third, rupture of six tendons, thereby creating
274 three classes of damages for rupture of tendons. Similarly, there are four classes for pier settlement.
275 The rupture of tendon dataset contains 1,231 time-series (i.e., vibration signals) and the lowering of
276 pier dataset contains 1,056 time-series. Each time-series contains 65,530 samples. Both datasets
277 are class-balanced, and they are split into three sets of train-validation-test as 60%-10%-20% of the

278 original suite of time-series.

279 **Hyper-parameters of the 1D CNN model**

280 A variety of hyper-parameters is incorporated to improve the robustness of the proposed model
281 and avoid overfitting. For example, learning rate is evaluated for various scenarios to improve
282 the accuracy while reducing the overfitting by empirically changing the gradient during back-
283 propagation. In this study, first a search space of hyper-parameters is designed by considering
284 a wide range of values for each hyper-parameter. In order to make the search feasible, extreme
285 values (e.g., very small window sizes) that yielded poor performance or unstable training dynamics
286 (training error does not decrease) were removed from the search space. A random search is
287 performed on this hyper-parameter space, and the set of hyper-parameters that yielded highest
288 accuracy is selected as the optimal configuration. The evaluation metrics based on the proposed
289 method are described later with a comparison between window-voted and non-voted results. In this
290 study, a range of hyper-parameters are selected first and tuned using random search algorithm to
291 achieve a set of hyper-parameter that provides the optimal accuracy. The range of hyper-parameters
292 used for 1D CNN is presented in Table 3. For example, window size is adopted within a range of
293 32-512 samples. Window size is the only external parameter and is decided by the user. Thus, a
294 sensitivity analysis is performed to understand the behavior of the performance evaluation metrics
295 (P_m) under different window sizes (w). Two different metrics, accuracy and FN, are used for
296 sensitivity analysis as they represent overall accuracy of the model and false-negative alarm critical
297 for civil infrastructure.

298 The optimal hyper-parameters of this dataset are obtained after tuning and are presented for all
299 the models in Table 4. An analysis is performed to understand the effect of w versus P_m . The results
300 are shown for various damage cases in Fig. 6. For example, Fig. 6 (a-b) shows that the optimal
301 performance is achieved at $w=256$, with highest ROC and accuracy, and lowest false-negative.
302 Although, the FNR remains consistent after $w=512$ and other metrics are at their peak, however,
303 due to larger w , the data size reduces per damage class and it leads to over-fitting of the data.

304 **Random initialization of weights**

305 Deep learning algorithms are iterative and require the user to specify value of initial weights
306 of neurons to initiate the iteration and its optimization. In practice, all weights in the model are
307 randomly drawn from a Gaussian or uniform distribution (Goodfellow et al. 2016). However, the
308 scale (low or high magnitude) has a large effect on both the outcome and optimization procedure. In
309 this study, random initialization with early stopping criteria is used and Adam optimizer (Kingma
310 and Ba, 2014) is used with dropout in each layer for regularization. After acquiring the optimal
311 tuned parameters, a parametric study is conducted to understand variance in the metrics of 1D CNN
312 model for random initialization of weights. The metrics used for evaluating random initialization of
313 weights are ROC-AUC, accuracy, FNR, and F1 score and are shown in Table 5. It can be observed
314 that for pier settlement, the mean (μ) of ROC-AUC is 0.97 with an accuracy of 0.85. The FNR is
315 0.15 and the standard deviation (σ) for all the trials is at its minimal of 1%. Similarly, for rupture
316 of tendons, the ROC-AUC is 0.92 with an accuracy of 0.67 and FNR of 0.33 with minimal σ of
317 2%.

318 **Effect of window size**

319 The window size used to augment the data is an external parameter apart from other model
320 parameters and it is critical to understand its effect on model performance. It can be observed that
321 the best performance with a combination of maximum ROC-AUC and accuracy and minimum FNR
322 is achieved at 256 samples per window. It is shown in Fig. 6 (a), ROC-AUC increases to 1.0 at
323 512, 800, 1024 samples per window, however, it leads to overfitting with increased FNR. A similar
324 result can be observed from Fig. 6 (b) with optimal performance at 256 samples per window.

325 **Model performance**

326 The optimal parameters are first used to evaluate the performance of the proposed model on
327 an entire series versus windowed and voted-windowed samples. The reason for comparison of the
328 entire time-series, windowed and voted windows is to show the improved performance by voting the
329 windowed samples. It should be noted that model performance on entire series results in very poor
330 accuracy due to nonlinearity, and nonstationarity in the signal. It may be noted that micro-averaged

331 is the average of area under the curve for all the classes. It can be observed from Figs. 7 (a) &
332 (b) for pier settlement, the ROC-AUC of a full-series signal is merely 0.56 while PR-AUC is only
333 0.21. A similar observation can be deduced in case of rupture of tendon in Figs. 8 (a) & (b),
334 where ROC-AUC and PR-AUC is 0.55 and 0.28, respectively. However, it is observed that voting
335 on windowed dataset increases accuracy considerably and it exhibits in ROC-AUC and precision-
336 recall (PR)-AUC curves, as presented in Figs. 7(c-f), and 8(c-f), respectively. The accuracy in
337 terms of ROC-AUC and PR-AUC increased by 71% and 314% for pier settlement case, and by
338 58% and 153.5% in case of rupture of tendons. Moreover, as shown in Fig. 7, majority voting on
339 samples has further improved the AUC for both ROC and PR. It can be observed that in case of pier
340 settlement, there is meager increase on ROC-AUC, however, there is a considerable improvement
341 in the area under the curve for PR. This behaviour can be attributed to a more localized damage
342 in case of pier settlement. Similarly, as observed in Fig. 8, when the damage was considerably
343 distributed in case of rupture of tendons, majority voting on windows highly increase the PR-AUC
344 for rupture of tendons.

345 It can be observed that majority voting on windows of distributed damage signal increases
346 the probability considerably by allocating the majority class and ignoring the non-prominent class
347 along with augmenting the data samples per class. Another critical performance metric, FNR
348 is used to evaluate the false negative alarm of damage in the proposed model. It can be noted
349 that the FNR reduces as the entire time-series is windowed and further reduces with the majority
350 voting. For example, in case of pier settlement, FNR reduces from 0.80 to 0.17 for the entire series
351 versus majority voted augmented dataset. Similarly, FNR reduces from 0.71 to 0.34 for rupture of
352 tendons, as shown in Table 6. The label 0, 1, and 2 are used to denote performance metrics of the
353 entire time-series, windowed time-series and majority voted-windowed time series, respectively.
354 The tuning process and the resulting performance improvement provide adequate justification to
355 counter any potential errors caused by the windowing.

Component-level damage identification

Component level damage identification is performed using Algorithm 1, for two multiclass damage scenario, namely, pier-settlement and rupture of tendons. The sensor locations are identified first, then, three different structural components of the bridge are used to localize the damage caused by the pier settlement and rupture of tendons during the demolition period of the bridge. An undamaged pier (Utzenstorf), bridge deck, and damaged pier (Koppigen) are used for representation of predicted probability (P_p) and infer damages in three components. The Koppigen pier is used for inducing the damage by lowering it in several increments starting with 20 mm, 40 mm, 80 mm, and moving to 95 mm at the last stage. Twelve different sensors are used to identify the location of damage, namely, 4 sensors (411, 421, 431, 441) on the undamaged pier (UDP), 4 sensors (216, 221, 226, 231) on the bridge deck (BD), and 4 sensors (511, 521, 531, 541) on the damaged pier (DP), as shown in Fig. 9.

The P_p is plotted against the sensor index and a dash-dotted average of P_p is shown as a representation of combined P_p for the corresponding structural component, as shown in Fig. 10 for 20 mm, and 40 mm and in Fig. 11 for 80 mm, and 95 mm lowering of pier, respectively. For example, Fig. 10 (*a, b, c*) represents P_p for undamaged pier (UDP), bridge deck (BD), and damaged pier (DP) for 20 mm lowering of piers. Similarly, Fig. 10 (*d, e, f*) is for 40 mm lowering of piers, respectively. It can be observed that, unlike in pier settlement of 40 mm, the proposed algorithm does not provide conclusive evidence of nominal damage of 20 mm. However, Fig. 11 (*a, b, c*) and (*d, e, f*) shows identification of damage for 80 mm and 95 mm, and it can be observed that the identification is clearly achieved through the proposed threshold where the P_p is highest for DP followed by BD which is affected by differential settlement of one of the piers.

It may be noted that, as the severity increases, the signals become more distinguishable and 1D CNN learns the classification more effectively. It can be observed from Fig. 12 that UDP shows lowest predicted probability due to its similarity to the response of the undamaged pier, however, both BD, and DP shows higher prediction accuracy. The reason for BD's highest probability is attributed to the surface area and larger affect of differential pier settlement of the entire bridge. In

383 summary, it can be concluded that the proposed method performs well for damage levels of 40 mm,
384 85 mm, and 95 mm, however, does not perform well for a very low level of damage, as shown in
385 case of pier settlement of 20 mm. Finally, Table 7 shows the confusion matrix for the multi-class
386 pier settlement damage classification problem with five classes, starting from no damage (class-0)
387 to 95 mm damage (class 5).

388 For rupture of tendons, the most affected area would be the bridge deck and the damage induced
389 due to rupture of tendons will create a non-localized and distributed damage throughout the bridge
390 deck in comparison to the damage in the bridge piers. The damage identification per sensors is
391 avoided due to non-conclusive inference and a comparison between structural components of the
392 bridge is provided in Fig. 13. It should be noted that rupture of tendons affects bridge deck and it
393 is shown in Fig. 13, however, the proposed algorithm could not clearly show the effect of rupture
394 of two and four tendons, while the rupture of six tendons proves to be the worse damage level
395 scenario.

396 **CONCLUSIONS**

397 In this paper, a windowed-1D CNN is employed for multi-class damage detection using limited
398 datasets. First, the limited dataset is augmented using windowing of the vibration data and the
399 prediction accuracy is improved by a novel majority voting approach on windowed classes. It is
400 observed that due to non-localization of sensors for data acquisition, damage identification for a
401 minor level of damage (say, 20 mm of pier settlement) is a challenge to predict. However, the
402 overall accuracy significantly improves with the increase in the severity of the damage (i.e., a
403 pier settlement of 40-95 mm). The proposed algorithm is analyzed with a sensitivity analysis on
404 window-size as the external parameter to the model as well as a parametric study to evaluate its
405 sensitivity with random initialization of weights. The improvement in the accuracy is illustrated
406 through a comparison between a single series dataset and windowed-voted time-series for ROC
407 and precision-recall AUC. In this paper, it is demonstrated that a simple 1D CNN architecture with
408 only one hidden layer is capable of classifying the time-series of vibration data into multi-class
409 with high accuracy. There are still a few limitations of the proposed algorithm, which are reserved

410 to be addressed in the future research.

- 411 • The obtained damage classification provided superior results; however, damage localization
412 at the sensor level was not achieved. It may be noted that damage is identified with the
413 exception of minor level of damage (e.g., 20 mm pier settlement). Future research is
414 reserved to improve the proposed method and accommodate the minor level of damage by
415 conducting an experimental simulation of a series of progressive damage cases with a wide
416 range of minor damage.
- 417 • The proposed 1D CNN model based on sequential data is independent of any feature selec-
418 tion process and offers robust and accurate approaches to complex damage identification.
419 However, like any other supervised technique, the 1D CNN also requires a significant
420 amount of training data to classify and predict the damage, which can be considered as a
421 limitation. However, with the recent advancement of remote and autonomous sensors and
422 internet-of-things, long-term SHM technologies have shown significant promise to monitor
423 critical infrastructure in smart cities. It is anticipated that the long-term monitoring will
424 allow the SHM researchers and practitioners to acquire low-cost periodical data with multi-
425 class health conditions of the structures, serving as the potential future training data for the
426 deep learning techniques.

427 **DATA AVAILABILITY STATEMENT**

428 All of the data, models, or code that support the findings of this study are available from the
429 corresponding author upon reasonable request.

430 **ACKNOWLEDGMENTS**

431 The authors would like to acknowledge funding provided to the first author through Government
432 of Ontario, Canada as Ontario Graduate Scholarship (OGS), and Queen Elizabeth II Graduate
433 Scholarship in Science and Technology (QEGS-II) for PhD studies. The authors also acknowledge
434 NSERC for providing the financial support to conduct this research through the third and fourth
435 author's NSERC Discovery grant.

REFERENCES

- Abdeljaber, O., and Avci, O. (2016). Non-parametric structural damage detection algorithm for ambient vibration response: utilizing artificial neural networks and self-organizing maps. *Journal of Architectural Engineering*, ASCE, 22(2), 04016004.
- Abdeljaber, O., Avci, O., Kiranyaz, S., Gabbouj, M., and Inman, D. J. (2017). Real-time vibration-based structural damage detection using one-dimensional convolutional neural networks. *Journal of Sound and Vibration*, 388, 154-170.
- Almasri, N., Sadhu, A., and Ray Chaudhuri, S. (2020). Toward Compressed Sensing of Structural Monitoring Data Using Discrete Cosine Transform, *Journal of Computing in Civil Engineering*, ASCE, 34(1).
- Avci, O., Abdeljaber, O., Kiranyaz, S., Hussein, M., Gabbouj, M., Inman, D. J. (2021). A review of vibration-based damage detection in civil engineering structures: from traditional methods to machine learning and deep learning based applications, *Mechanical Systems and Signal Processing*, 147, 107077.
- Azimi, M., and Pekcan, G. (2020). Structural health monitoring using extremely compressed data through deep learning. *Computer-Aided Civil and Infrastructure Engineering*, 35(6), 597-614.
- Bao, X., Fan, T., Shi, C., and Yang, G. (2020). One-dimensional convolutional neural network for damage detection of jacket-type offshore platforms. *Ocean Engineering*, 108293.
- Bao, Y., Tang, Z., Li, H., and Zhang, Y. (2019). Computer vision and deep learning-based data anomaly detection method for structural health monitoring. *Structural Health Monitoring*, 18(2), 401-421.
- Barbosh, M., Singh, P., and Sadhu, A. (2020). Empirical mode decomposition and its variants: a review with applications in structural health monitoring, *Smart Materials and Structures*, 29(9), 093001.
- Bergstra, J., and Bengio, Y. (2012). Random search for hyper-parameter optimization. *Journal of Machine Learning*. 13, 281-305.
- Chang, K., and Chi, S. (2019). Bridge clustering for systematic recognition of damage patterns on

463 bridge elements, *Journal of Computing in Civil Engineering*, ASCE, 33(5), 04019028.

464 Fallahian, M., Khoshnoudian, F., and Meruane, V. (2018). Ensemble classification method for
465 structural damage assessment under varying temperature. *Structural Health Monitoring*, 17(4),
466 747-762.

467 Gardner, P., Fuentes, R., Dervilis, N., Mineo, C., Pierce, S.G., Cross, E.J., and Worden, K. (2020).
468 Machine learning at the interface of structural health monitoring and non-destructive evaluation,
469 *Philosophical Transactions of Royal Society*, A378: 20190581.

470 Goodfellow, I., Bengio, Y., and Courville, A. (2017). Deep learning. Cambridge, MA: MIT Press.

471 Gulgec, N. S., Takáč, M., and Pakzad, S. N. (2017). Structural damage detection using convolu-
472 tional neural networks. *Conference Proceedings of the Society for Experimental Mechanics Series*,
473 3 Part F2 (June), 331-337.

474 Gulgec, N. S., Takáč, M., and Pakzad, S. N. (2019). Convolutional Neural Network Approach for
475 Robust Structural Damage Detection and Localization, *Journal of Computing in Civil Engineering*,
476 ASCE, 33(3): 04019005.

477 Guo, J., Xie, X., Bie, R., and Sun, L. (2014). Structural health monitoring by using a sparse
478 coding-based deep learning algorithm with wireless sensor networks. *Personal and Ubiquitous*
479 *Computing*, 18(8), 1977-1987.

480 Hou, R., and Xia, Y. (2020). Review on the new development of vibration-based damage identifi-
481 cation for civil engineering structures: 2010-2019, *Journal of Sound and Vibration*, 115741.

482 Ioffe, S., and Szegedy, C. (2015). Batch normalization: accelerating deep network training by
483 reducing internal covariate shift. arXiv:1502.03167.

484 Kankanamge, Y., Hu, Y., and Shao, X. (2020). Application of wavelet transform in structural health
485 monitoring, *Earthquake Engineering and Engineering Vibrations*, 19, 515-532.

486 Kingma, D.P., and Ba, J.L. (2014). ADAM: a method for stochastic optimization. *3rd International*
487 *Conference for Learning Representations*, San Diego, arXiv:1412.6980v9.

488 Kiranyaz, S., Avci, O., Abdeljaber, O., Ince, T., Gabbouj, M., and Inman, D. J. (2019). 1D Convolu-
489 tional Neural Networks and Applications: A Survey, 1-20. Retrieved from <http://arxiv.org/abs/1905.03554>.

490 Kumar, S.S., Wang, M., Abraham, D.M., Jahanshahi, M.R., Iseley, T., and Cheng, J.C.P. (2019).
491 Deep learning based automated detection of sewer defects in CCTV videos, *Journal of Computing*
492 *in Civil Engineering*, ASCE, 34(1), 04019047.

493 Liu, T., Xu, H., Ragulskis, M., Cao, M., and Ostachowicz, W. (2020). A data-driven damage
494 identification framework based on transmissibility function datasets and one-dimensional convolu-
495 tional neural networks: Verification on a structural health monitoring benchmark structure, *Sensors*,
496 20(4), 1–25.

497 Maeck, J., and Roeck De. G. (2003), “Description of Z24 benchmark,” *Mechanical Systems and*
498 *Signal Processing*, 17(1), 127-131.

499 Nakamura, M, Masri S. F., Chassiakos, A.G., and Caughey T. K. (1998). A method for non-
500 parametric damage detection through the use of neural networks. *Earthquake Engineering and*
501 *Structural Dynamics*, 27, 997-1010.

502 Ni, F. T., Zhang, J., and Noori, M. N. (2020). Deep learning for data anomaly detection and data
503 compression of a long-span suspension bridge. *Computer-Aided Civil and Infrastructure Engineer-*
504 *ing*, 35(7), 685-700.

505 Piryonesi, S.M., and El-Diraby, T.E. (2019). Data analytics in asset management: cost-effective
506 prediction of the pavement condition index. *Journal of Infrastructure Systems*, ASCE, 26(1),
507 04019036.

508 Roeck, De. G., and Teughels, A. (2004), “Structural damage identification of the highway bridge
509 Z24 by FE model updating,” *Journal of Sound and Vibration*, 278, 589-610.

510 Sarawgi, Y., Somani, S., Chhabra, A., and Dhiraj (2020). Nonparametric Vibration Based Damage
511 Detection Technique for Structural Health Monitoring Using 1D CNN. *In book: Computer Vision*
512 *and Image Processing*, 146-157.

513 Sadhu, A., Narasimhan, S., and Antoni, J. (2017). A review of output-only structural mode iden-
514 tification literature employing blind source separation methods. *Mechanical Systems and Signal*
515 *Processing*, 94, 415-431.

516 Shang, Z., Sun, L., Xia, Y., and Zhang, W. (2020). Vibration-based damage detection for bridges

517 by deep convolutional denoising autoencoder. *Structural Health Monitoring*.

518 Sharma, S., and Sen, S. (2020). One-dimensional convolutional neural network-based damage
519 detection in structural joints. *Journal of Civil Structural Health Monitoring*, 0123456789.

520 Sony, S., Laventure, S., and Sadhu, A. (2019). A literature review of next-generation smart sens-
521 ing technology in structural health monitoring. *Structural Control and Health Monitoring*, 26(3),
522 e2321.

523 Sony, S., and Sadhu, A. (2020). Synchrosqueezing transform-based identification of time-varying
524 structural systems using multi-sensor data. *Journal of Sound and Vibration*, 486, 115576.

525 Sony, S., and Sadhu, A. (2021). Multivariate empirical mode decomposition-based structural
526 damage localization using limited sensors. *Journal of Sound and Vibration*, 10775463211006965.

527 Sony, S., Dunphy, K., Sadhu, A., and Capretz, M. (2021). A Systematic Review of Convolutional
528 Neural Network-based Structural Condition Assessment Techniques. *Engineering Structures*, 226,
529 111347.

530 Sony, S. (2021). Towards Multiclass Damage Detection and Localization using Limited Vibration
531 Measurements, Western University, Canada, *Electronic Thesis and Dissertation Repository*. 7659.

532 Srinivasan, A. (1999). Note on the location of optimal classifiers in n-dimensional roc space.
533 *Technical Report PRG-TR-2-99*, Oxford University Computing Laboratory, England.

534 Staszewski., W. J., and Robertson, A.N. (2006). Time-frequency and time-scale analyses for struc-
535 tural health monitoring, *Philosophical Transactions of Royal Society*, A365, 1851.

536 Su, J., Xia, Y., and Weng, S. (2020). Review on field monitoring of high-rise structures. *Structural*
537 *Control and Health Monitoring*, 27(12), e2629.

538 Wang, V. Z., and Ong, K.C.G. (2015). Nonparametric statistical formulations for structural health
539 monitoring. *Computers and Structures*. 148, 63-74.

540 Zhang, Y., Miyamori, Y., Mikami, S., and Saito, T. (2019). Vibration-based structural state identifi-
541 cation by a 1-dimensional convolutional neural network. *Computer-Aided Civil and Infrastructure*
542 *Engineering*, 34(9), 822-839.

543
544
545
546
547
548
549
550

List of Tables

1	Description of various performance metrics.	23
2	Description of the multiclass damage scenarios and the class labels.	24
3	Hyper-parameters used in 1D CNN for tuning by random search algorithm.	25
4	Optimal configuration of the hyper-parameters of the selected 1D CNN.	26
5	Random initialization of weights.	27
6	Training and testing performance of 1D CNN.	28
7	Confusion matrix for a pier settlement damage problem.	29

TABLE 1. Description of various performance metrics.

Metric	Formula	Remarks
ROC-AUC	Recall Vs FPR	Degree of separability between classes
Accuracy	$\frac{TP+TN}{TP+FN+FP+TN}$	Less useful for heavily imbalanced data
Precision	$\frac{TP}{TP+FP}$	Positive predicted value
Recall	$\frac{TP}{TP+FN}$	True positive rate or sensitivity
False Positive Rate (FPR)	$\frac{FP}{TN+FP}$	False alarm when there is no damage
False Negative Rate (FNR)	$\frac{FN}{TP+FN}$	No alarm for actual damage

TABLE 2. Description of the multiclass damage scenarios and the class labels.

Problem	Damage scenario	Class label
0	Undamaged	0
1	Rupture of 2 tendons	1
	Rupture of 4 tendons	2
	Rupture of 6 tendons	3
2	Lowering of pier, 20 mm	1
	Lowering of pier by 40 mm	2
	Lowering of pier by 80 mm	3
	Lowering of pier by 95 mm	4

TABLE 3. Hyper-parameters used in 1D CNN for tuning by random search algorithm.

Parameter	Values
Window size	32, 64, 128, 160, 256, 512
No. of hidden convolutional layers	1 - 6
No. of filters	1024, 512, 256, 128, 64, 32, 16
No. of fully connected layers	1 or 2 layers with 16 and 32 nodes
Learning rate	0.0003, 0.001, 0.01, 0.1
Batch size	32, 64, 256, 512
Kernel size	4, 8, 16, 32, 64

TABLE 4. Optimal configuration of the hyper-parameters of the selected 1D CNN.

Parameter	Values
Window size	256
No. of hidden convolutional layers	1
No. of filters	32
No. of fully connected layers	2 with 32 and 16 nodes, respectively
Learning rate	0.0003
Batch size	256
Kernel size	16

TABLE 5. Random initialization of weights.

Pier settlement				
Trial #	ROC-AUC	Accuracy	FNR	F1 score
1	0.98	0.85	0.15	0.85
2	0.97	0.85	0.15	0.85
3	0.98	0.86	0.14	0.86
4	0.97	0.83	0.17	0.83
5	0.98	0.86	0.14	0.86
μ	0.97	0.85	0.15	0.85
σ	0.00	0.01	0.01	0.01
Rupture of tendons				
1	0.92	0.69	0.31	0.69
2	0.93	0.68	0.32	0.68
3	0.90	0.66	0.34	0.66
4	0.91	0.65	0.35	0.65
5	0.92	0.66	0.34	0.66
μ	0.92	0.67	0.33	0.67
σ	0.01	0.02	0.02	0.02

TABLE 6. Training and testing performance of 1D CNN.

Lowering of pier								
Dataset	ROC	PR	A	P	R	FPR	FNR	F1 score
0	0.56	0.21	0.20	0.20	0.20	0.2	0.80	0.20
1	0.95	0.84	0.77	0.77	0.77	0.06	0.23	0.77
2	0.97	0.91	0.83	0.83	0.83	0.04	0.17	0.83

Rupture of tendons								
Dataset	ROC	PR	A	P	R	FPR	FNR	F1 score
0	0.55	0.28	0.29	0.29	0.29	0.23	0.71	0.29
1	0.87	0.71	0.59	0.59	0.59	0.14	0.41	0.59
2	0.92	0.82	0.66	0.66	0.66	0.11	0.34	0.66

TABLE 7. Confusion matrix for a pier settlement damage problem.

		Predicted Class				
		Pred-0	Pred-1	Pred-2	Pred-3	Pred-4
True Class	True-0	192	8	3	0	5
	True-1	56	137	16	0	3
	True-2	1	0	203	3	5
	True-3	0	0	24	183	5
	True-4	1	0	8	4	199

551
552
553
554
555
556
557
558
559
560
561
562
563
564
565
566
567
568
569
570
571
572
573

List of Figures

1	The proposed 1D CNN architecture used in this study.	31
2	Extracting data sequences of windows from the vibration data using 1D CNN architecture.	32
3	Data pipelines for training the proposed 1D CNN network and obtaining predictions for a given time-series.	33
4	Schematic of the Z24 bridge.	34
5	Sensor placement for data acquisition in the Z24 bridge.	35
6	Performance evaluation of 1D CNN based on window size for (a) pier settlement and (b) rupture of tendons.	36
7	Performance of 1DCNN by windowing of the data of pier settlement (a) full series ROC, (b) full series PR, (c) windowed ROC, (d) windowed PR, (e) windowed-voted ROC, (f) windowed-voted PR.	37
8	Performance of 1D CNN by windowing of the data of rupture of tendons (a) Full series ROC, (b) Full series PR, (c) windowed ROC, (d) windowed PR, (e) windowed-voted ROC, (f) windowed-voted PR.	38
9	Schematic showing the sensor location and their numbers used in the analysis. . . .	39
10	Damage identification for pier settlement with two damage levels, (a, b, c): 20 mm and (d, e, f): 40 mm.	40
11	Damage identification for pier settlement with two damage levels, (a, b, c): 80 mm and (d, e, f): 95 mm.	41
12	Damage identification for the pier settlement.	42
13	Damage identification for the rupture of tendons.	43

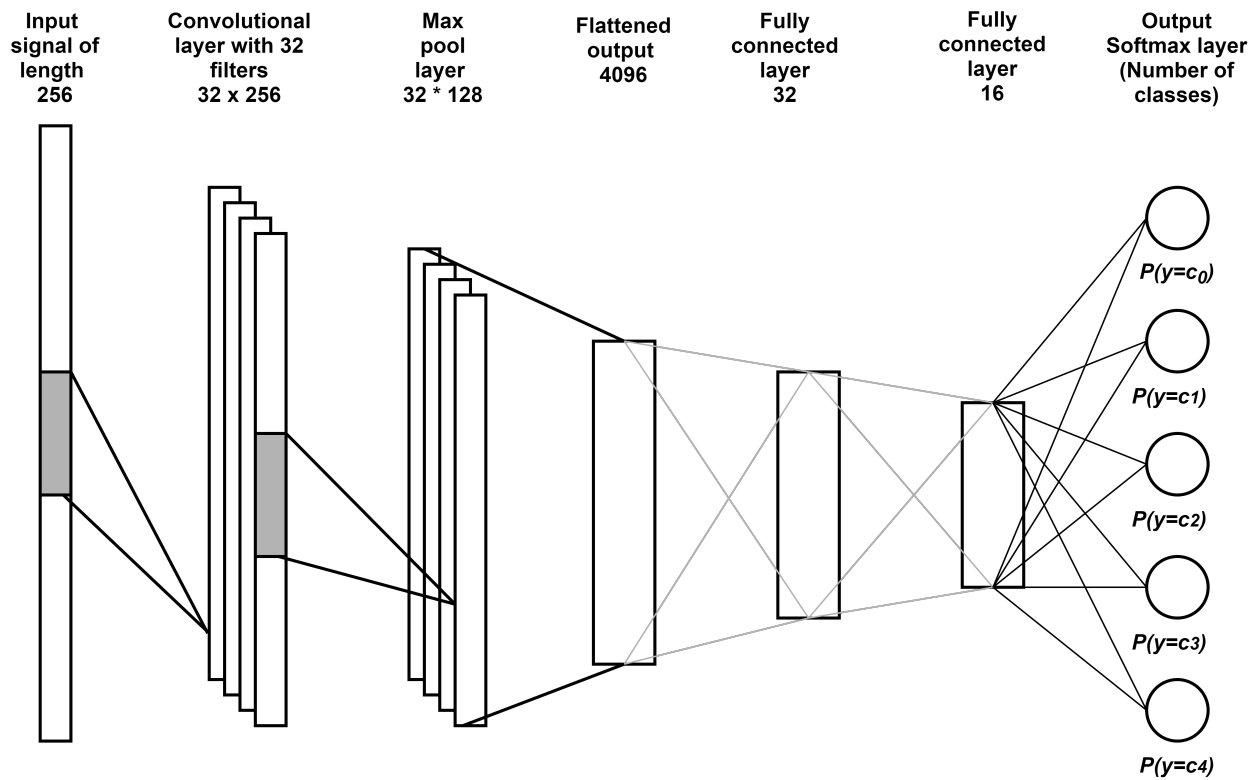


Fig. 1. The proposed 1D CNN architecture used in this study.

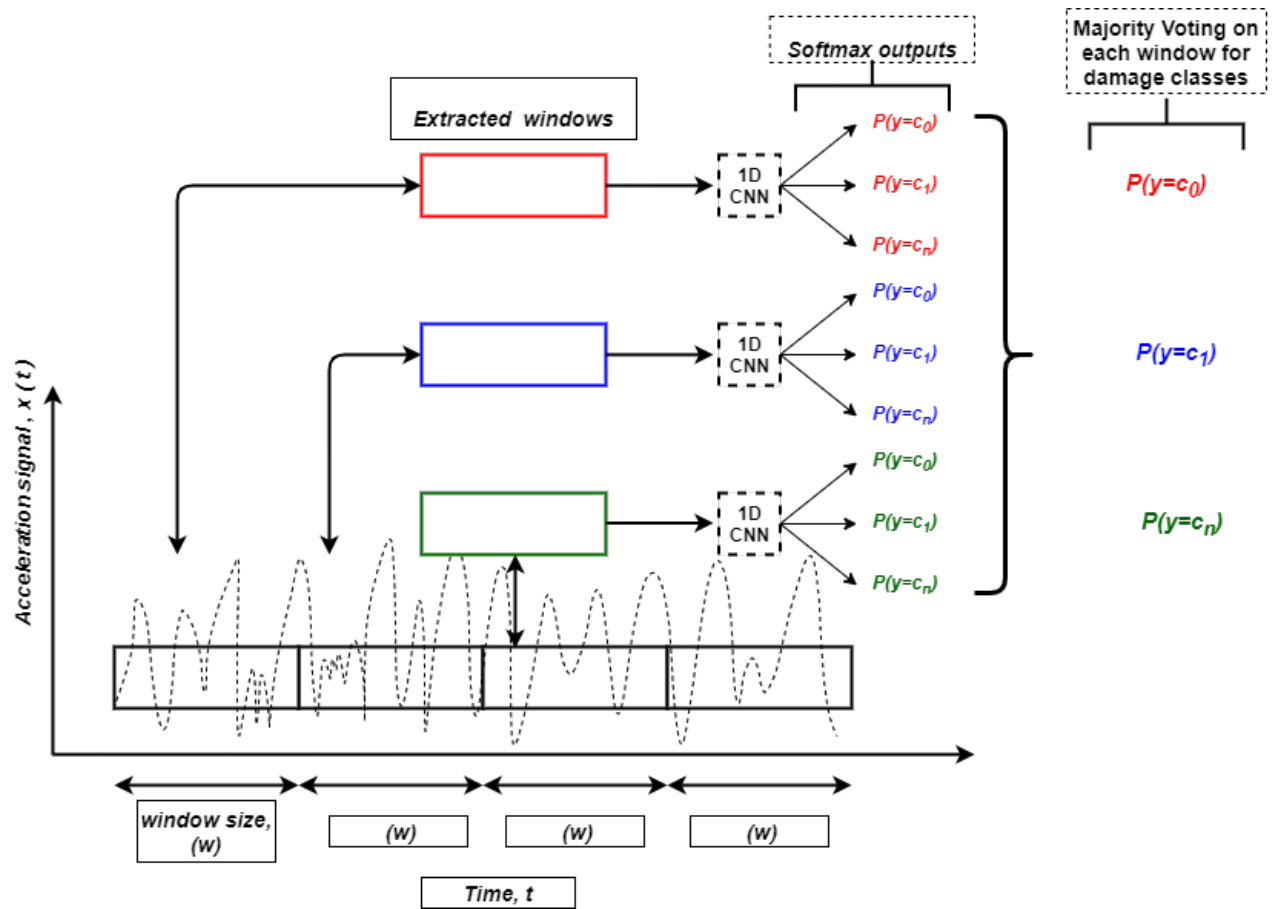


Fig. 2. Extracting data sequences of windows from the vibration data using 1D CNN architecture.

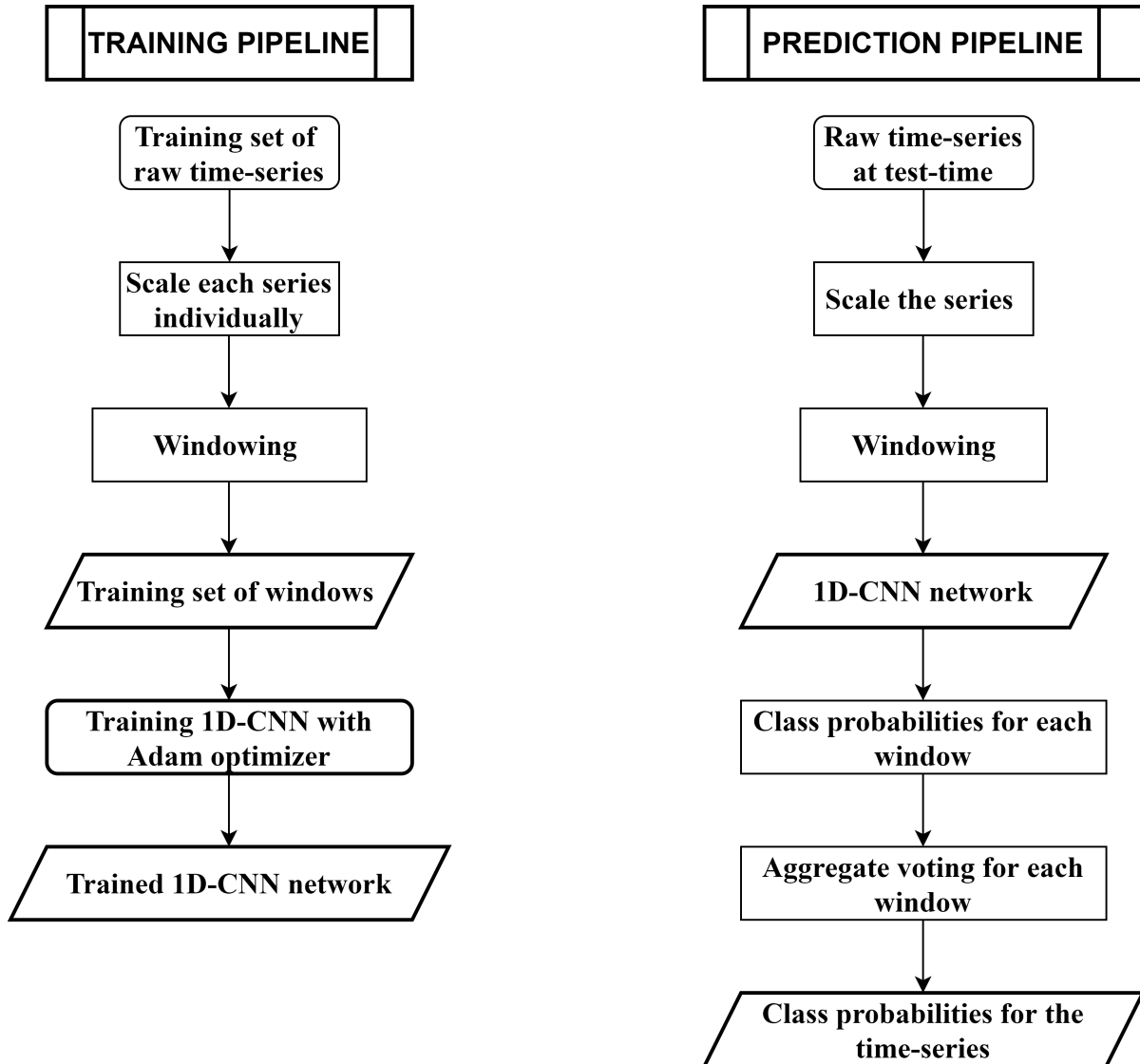


Fig. 3. Data pipelines for training the proposed 1D CNN network and obtaining predictions for a given time-series.

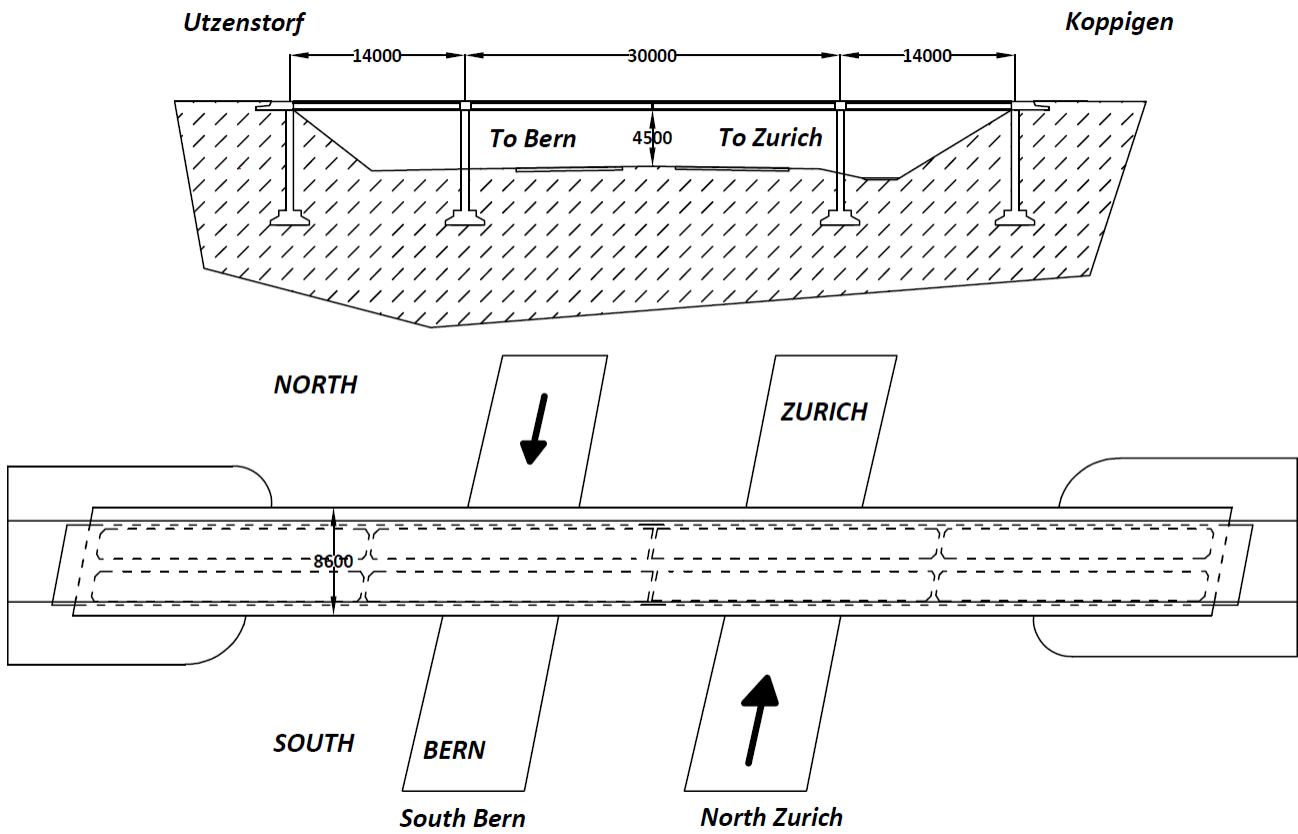


Fig. 4. Schematic of the Z24 bridge.

Utzenstorf

Koppigen

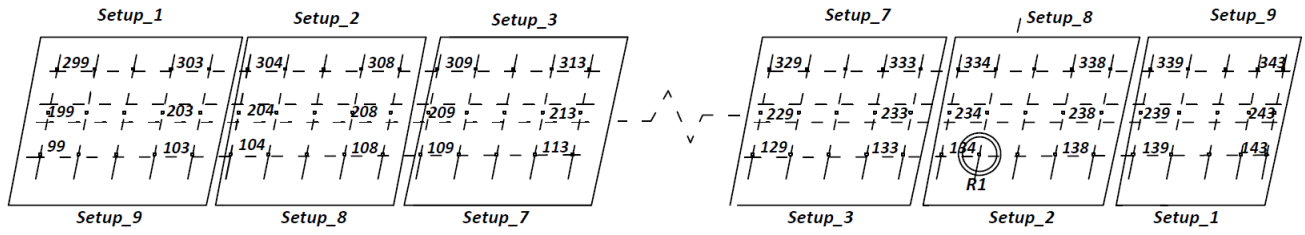


Fig. 5. Sensor placement for data acquisition in the Z24 bridge.

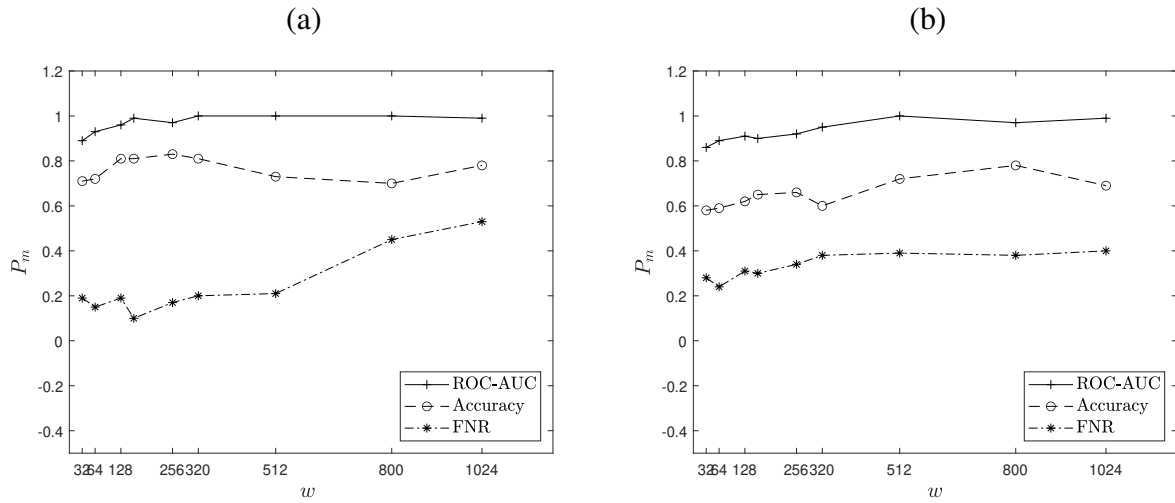


Fig. 6. Performance evaluation of 1D CNN based on window size for (a) pier settlement and (b) rupture of tendons.

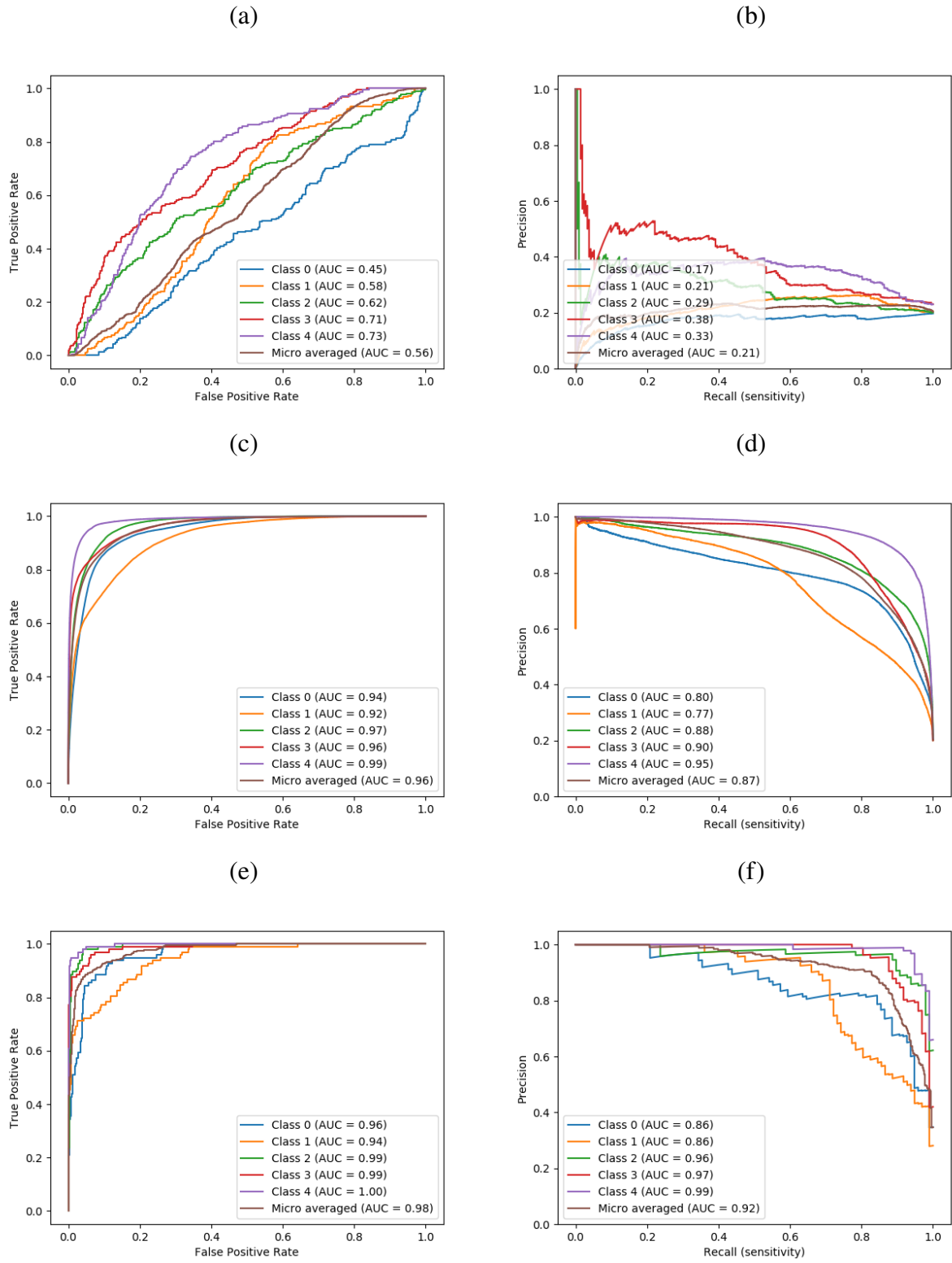


Fig. 7. Performance of 1DCNN by windowing of the data of pier settlement (a) full series ROC, (b) full series PR, (c) windowed ROC, (d) windowed PR, (e) windowed-voted ROC, (f) windowed-voted PR.

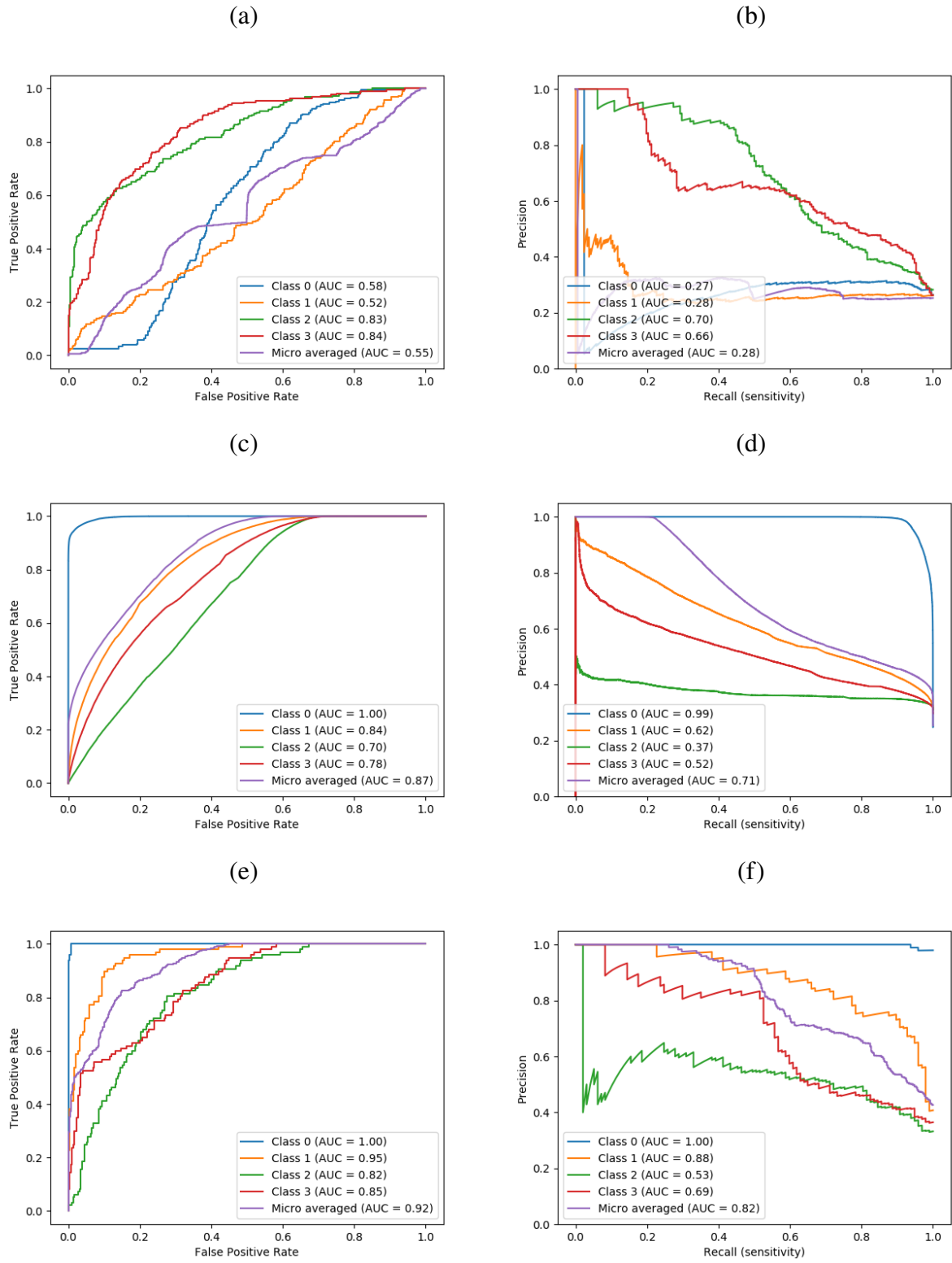


Fig. 8. Performance of 1D CNN by windowing of the data of rupture of tendons (a) Full series ROC, (b) Full series PR, (c) windowed ROC, (d) windowed PR, (e) windowed-voted ROC, (f) windowed-voted PR.

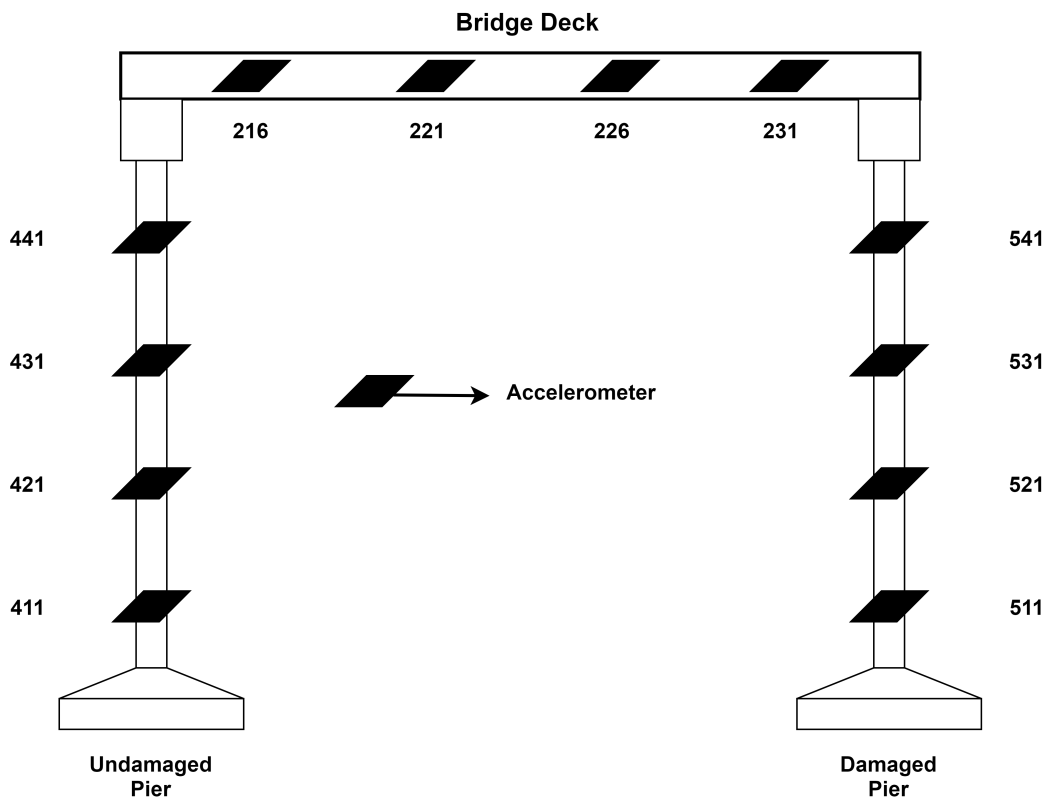


Fig. 9. Schematic showing the sensor location and their numbers used in the analysis.

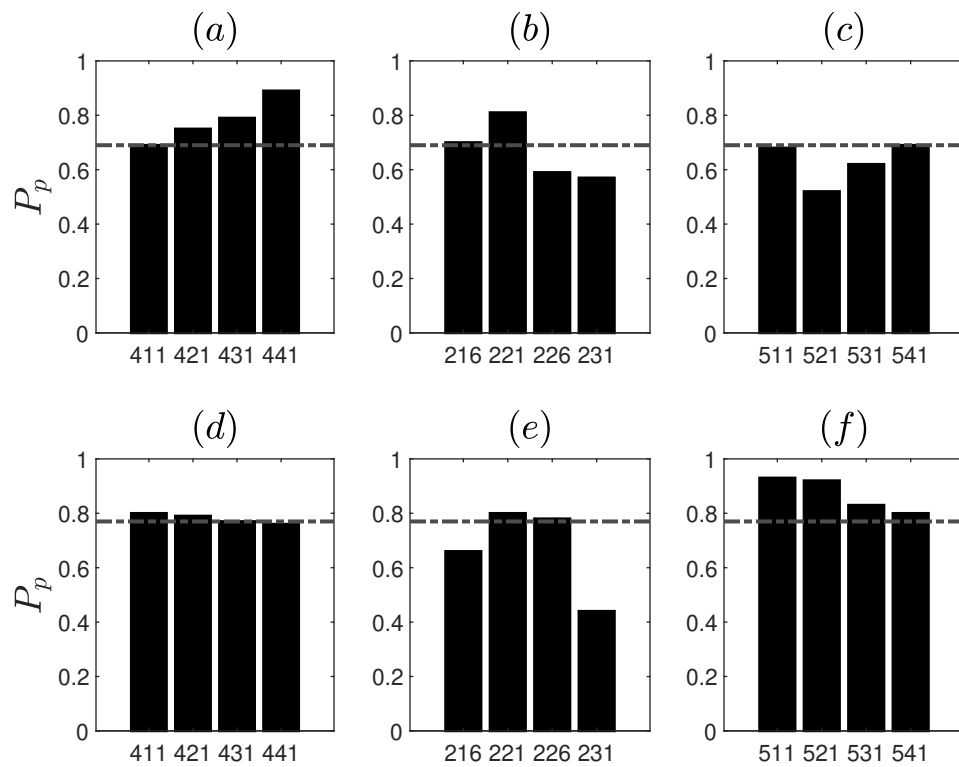


Fig. 10. Damage identification for pier settlement with two damage levels, (a, b, c): 20 mm and (d, e, f): 40 mm.

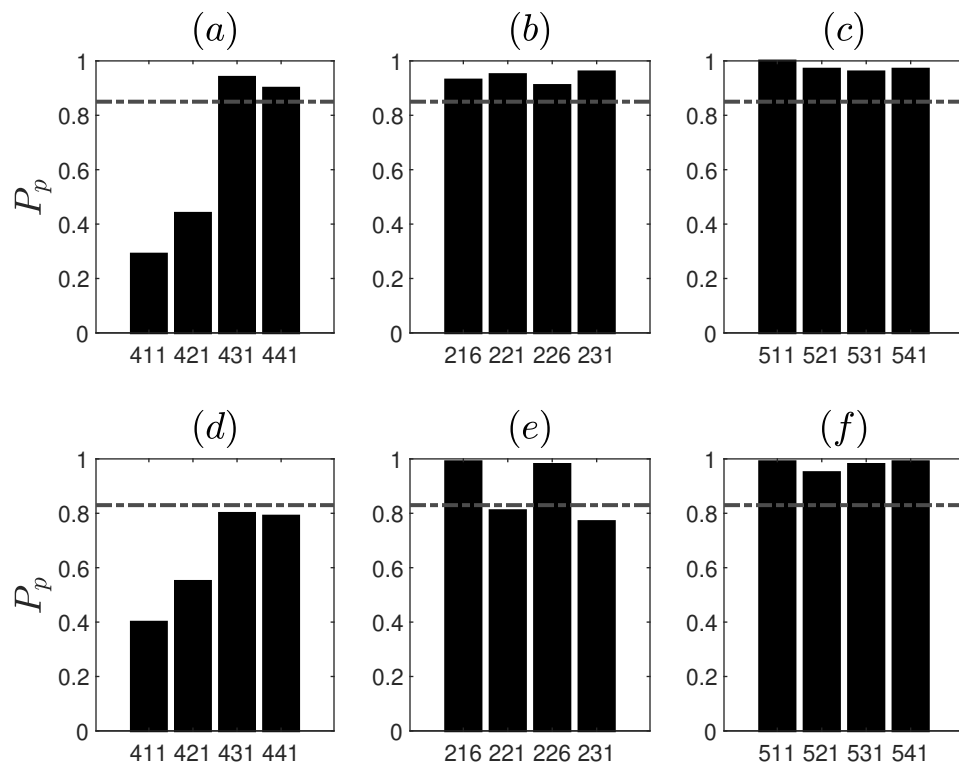


Fig. 11. Damage identification for pier settlement with two damage levels, (a, b, c): 80 mm and (d, e, f): 95 mm.

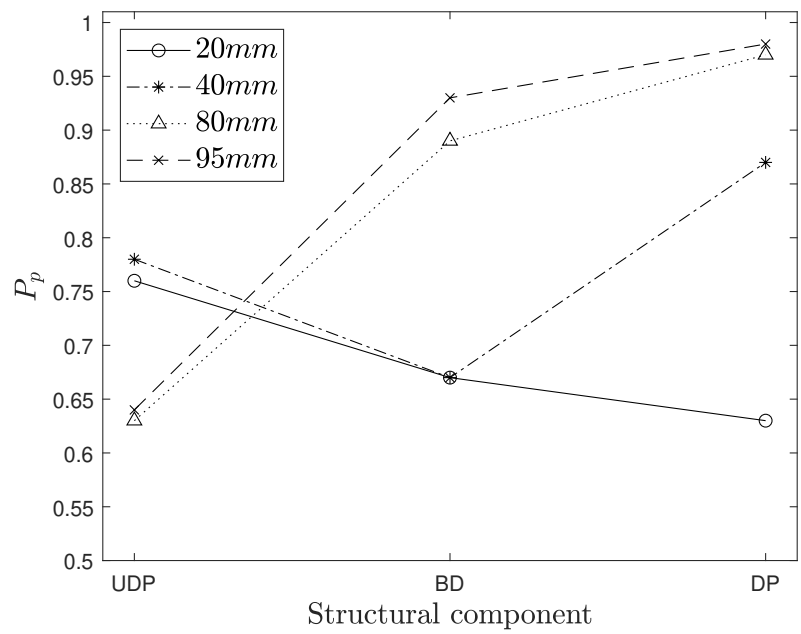


Fig. 12. Damage identification for the pier settlement.

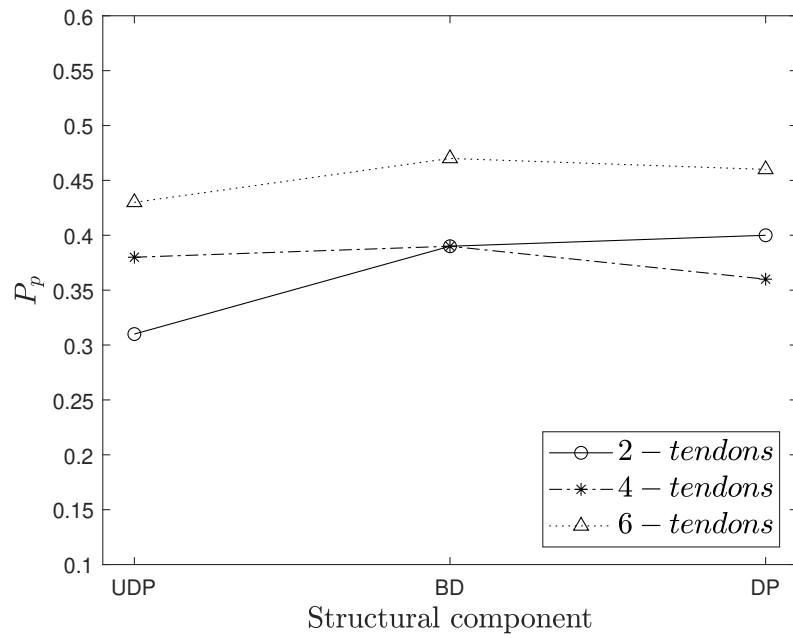


Fig. 13. Damage identification for the rupture of tendons.