

Clustering and selection of hurricane wind records using a machine learning approach

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ABSTRACT

In wind engineering, to accurately estimate the nonlinear dynamic response of structures while considering uncertainties of hurricanes, a suite of wind records representing the hurricane hazards of a given location is of great interest. Such a suite generally consists of a large number of hurricane wind records, which may lead to highly computational cost for structural analysis. To reduce the computational demand while still preserving the accuracy of the uncertainty quantification process, this paper proposes a machine learning approach to select a representative subset of all collected hurricane wind records for a location. First, hurricane wind records, which are expressed as time series with information that includes both wind speed and direction, are collected from a synthetic hurricane catalog. The high-dimensional hurricane wind

23 records are then compressed into a set of low-dimensional latent feature vectors using an artificial neural
24 network, designated as an autoencoder. The latent feature vectors represent the important patterns of wind
25 records such as duration, magnitude and the changing of wind speeds and directions over time. The wind
26 records are then clustered by applying the k-means algorithm on the latent features, and a subset of records
27 is selected from each cluster. The wind records selected from each cluster are those whose latent feature
28 points are closest to the centroid of all latent feature points in that cluster. In order to do regional analysis
29 while taking into account that the hurricane wind records are site-specific, this paper suggests that a region
30 can be discretized into a set of grids, with the proposed hurricane selection approach applied to each grid.
31 This procedure is demonstrated using Massachusetts as a testbed.

32 **Keywords:** hurricane selection, time series clustering, autoencoder, k-means, uncertainty quantification,
33 regional analysis, wind direction

34 **Introduction**

35 Nonlinear dynamic analysis is increasingly being considered in wind design of buildings and other
36 structures as performance-based design becomes an increasingly popular option (ASCE 2019), where
37 controlled inelastic deformations are allowed under strong winds (Wang and Wu 2022). In the fully
38 probabilistic performance-based hurricane engineering framework (Barbato et al. 2013), fragility curves of
39 structures are commonly adopted to do probabilistic damage assessment. Strength limit states of structures
40 usually involve nonlinear behavior that is then integrated into the predictions of likelihood of damage that
41 is offered through fragility analysis. Fragility functions are defined as the failure probability of a structure
42 conditional on the intensity measure of hazards, including hurricanes in this work. If only the failure
43 probability or fragility is of interest for a hurricane event (i.e., at the end of the loading time history) instead
44 of for a certain time interval within the hurricane duration, the uncertainties in the loading time histories
45 can be accounted for through running a series of nonlinear dynamic analysis with a suite of hurricane wind
46 records. The hurricane wind records should include time histories that incorporate the wind directions as
47 well as wind speeds, because the changing of wind directions during hurricanes has significant effects on

48 the structural response. Consequently, the wind records in this research are time series of both wind speed
49 and direction. To develop accurate fragility curves, the structures should be analyzed with a suite of
50 hurricane wind records that can cover the record-to-record uncertainties in the changing of wind speeds and
51 directions within the hurricane durations. A large amount of hurricane wind records can be collected for a
52 location considering the existing historical and synthetic hurricanes (ASCE 2016b; Vickery et al. 2010;
53 Vickery et al. 2009b; Vickery et al. 2009c). However, it is challenging to run nonlinear dynamic analysis
54 for all of the collected hurricane records due to the high computational demand of finite element analysis
55 of structures; thus, a minimum number of hurricane records should be selected to represent the uncertainties
56 in all of the collected hurricane records.

57 In prior work, Li (2005) and Li and Ellingwood (2006) developed hurricane fragility curves for wood-frame
58 residential construction with a simplified limit state function, where the nonlinear and dynamic effects are
59 neglected. Cui and Caracoglia (2015) carried out fragility analysis on tall buildings only for the
60 serviceability limit state, so frequency domain analysis is adopted, and duration and nonstationary effects
61 of hurricanes cannot be considered. In order to avoid performing structural analysis for long durations of
62 windstorms, the dynamic shakedown method was utilized by researchers to model the inelastic behavior of
63 buildings (Chuang and Spence 2019, 2020; Tabbuso et al. 2016). Other researchers tried to develop
64 hurricane fragility curves using nonlinear dynamic analysis only for a fixed time interval with a constant
65 wind direction. For example, Hallowell et al. (2018) used wind records with 1-hour time intervals, while
66 Ma et al. (2021) used wind records with 2-minute time intervals. The fragility developed for this certain
67 time interval cannot represent the fragility for a whole hurricane because of dynamic effects, yielding and
68 changes in wind speeds and directions. Of course, one can discretize the hurricane duration into a series of
69 short time intervals and apply the developed fragility curves to each short time interval; however, the failure
70 probabilities within those short time intervals are correlated (Der Kiureghian 2005; Kim et al. 2019; Straub
71 et al. 2020). This correlation is difficult to quantify from the view of time-variant reliability and is not
72 considered by the above authors. Given the limitations of the previous research, this paper considers the

73 failure probability for a hurricane event instead of a certain time interval during a hurricane and tries to
74 select hurricane wind records that can account for the record-to-record uncertainties in hurricanes. The
75 selected wind records can be used to estimate failure probabilities of structures with nonlinear time history
76 analysis. Through this way it is no longer needed to estimate the correlations of failure probabilities in the
77 short time intervals within a hurricane.

78 In performance-based earthquake engineering (Moehle and Deierlein 2004), a probabilistic framework has
79 been proposed to integrate seismic hazard analysis and structural damage analysis, where a suite of ground
80 motions are adopted to represent the uncertainties in earthquake ground motions. Ground motion selection
81 has been widely studied in the literature (Baker and Lee 2018; Bojórquez et al. 2013; Du and Padgett 2021;
82 Jayaram et al. 2011; Naeim et al. 2004). Some generally used ground motions suites are the SAC
83 (Somerville et al. 1997) records, LMSR (Krawinkler et al. 2003) records, and FEMA-P695 records (FEMA
84 2009). Recently, machine learning approaches have also been introduced to ground motion selection, where
85 a reduced number of ground motions are obtained through clustering of a large number of ground motions
86 (Bond et al. 2022; Kim et al. 2021; Zhang et al. 2020). However, there is no similar research in the literature
87 for selection of hurricane wind records. There are two instances of prior research that consider uncertainties
88 in hurricane wind hazards using a set of wind records, but they do not use a selection procedure. Vickery
89 et al. (2006) studied hurricane fragility curves for building envelope components that were developed in
90 the Hazus-MH software by comparing the wind pressure demand and the capacity of the envelope
91 components. The record-to-record uncertainties of hurricane wind speeds were accounted for through the
92 use of a 20,000-year simulation of hurricanes created by employing the hurricane model described by
93 Vickery et al. (2000a) and Vickery et al. (2000b). The simulated hurricanes inherently incorporated many
94 of the duration effects associated with the changes in wind speed and direction which accompany hurricane
95 winds. Joyner and Sasani (2018) developed fragility curves for the windborne debris damage of building
96 glazing, where eight hurricanes that made landfall in the U.S. in the last 10 years were adopted.
97 Uncertainties in the record-to-record variability for different hurricanes were accounted for by employing

98 the eight hurricane records in the damage analysis. Vickery et al. (2006) used all hurricanes in the 20,000-
99 year simulation, which may address the uncertainties in hurricanes, but is not suitable for nonlinear dynamic
100 analysis considering the computational demand. On the contrary, Joyner and Sasani (2018) only used eight
101 hurricanes without an analysis of the hazard uncertainties, which may not be able to represent the
102 uncertainties in hurricanes for a specific location.

103 This paper proposes a procedure to select a suite of hurricane wind records that can be used for performance-
104 based design and fragility analysis. The wind speed and direction records for a location are collected from
105 a synthetic hurricane catalog (Liu 2014) with some preprocessing, after which the collected wind records
106 have durations that are short enough to make a nonlinear time history analysis feasible. The collected wind
107 records are then compressed into low-dimensional latent feature vectors using a neural network designated
108 as an autoencoder (Aggarwal 2018), so that it is easier to measure similarity of different wind records and
109 apply the standard clustering algorithms such as the k-means algorithm (Aggarwal et al. 2001; Shalev-
110 Shwartz and Ben-David 2014). Autoencoder is an artificial neural network in which the input and output
111 layers have the same number of neurons, while the number of neurons in the middle is constricted. The
112 training algorithm tries to reconstruct the input data in the output layer; however, this reconstruction is not
113 exact because the neurons in the middle only carry a reduced representation of the input data. The data held
114 by the neurons in the middle (i.e., the low dimensional vectors compared to the input and output layer) are
115 called latent features, to which the clustering algorithm is applied. This means that only important
116 information in the wind records is preserved for clustering. The latent features representing hurricane wind
117 records are then clustered into several groups using the conventional k-means algorithm (Shalev-Shwartz
118 and Ben-David 2014). Finally, only a few hurricane wind records are selected from each cluster for fragility
119 development or design checks, which significantly reduces the number of required time history analyses,
120 while still ensuring that the uncertainties of different hurricanes are covered with a limited number of wind
121 records. Since the properties of hurricanes for different locations have significant differences, a hazard map
122 can be developed for hurricane wind records so that users are able to choose appropriate records for their

123 locations of interest. As an example, the Commonwealth of Massachusetts has been divided into 92 grids
124 and a suite of hurricane wind records has been selected for each grid using the proposed hurricane selection
125 approach. To demonstrate the usefulness and effectiveness of the selected wind records, they have been
126 adopted to develop fragility curves for electrical transmissions towers in Massachusetts, which can be found
127 in Du et al. (2022) and Du and Hajjar (2022).

128 **Hurricane simulation**

129 Synthetic hurricanes are widely used for risk analysis and structural design in wind engineering, which
130 evolved from the single site probabilistic model (Russell 1971) to Vickery's hurricane track model (Vickery
131 et al. 2000a). For example, ASCE 7 has adopted the hurricane track model when generating the wind hazard
132 maps (ASCE 2016b). This research also uses a 10,000 year synthetic hurricane catalog developed by Liu
133 (2014) for the Atlantic basin based on Vickery's hurricane track model, which consists of a hurricane
134 genesis model, a track model, an central pressure model, a decay model and a boundary layer model. The
135 temporal and spatial evolution of thousands of hurricanes from emergence to dissipation was modeled using
136 the Monte Carlo method. The HURDAT database (Jarvinen et al. 1984) for historical storms was adopted
137 for building the hurricane model through regression and calibrating the simulated results. In this simulation,
138 the state of a hurricane can be determined with 7 parameters: the hurricane eye's latitude and longitude,
139 storm translation speed, storm heading angle, storm central pressure, radius to maximum winds (describing
140 storm size), and Holland's radial pressure profile parameter (i.e., the Holland B parameter (Holland 1980)).
141 These parameters are updated at each 6-hour point. As suggested by Vickery et al. (2000a), linear
142 interpolation is performed within each 6-hour interval, which results in 10-min updates of the parameters
143 as used in Vickery et al. (2009c). Examples of the simulated hurricane tracks are shown in Fig. 1. In this
144 research, the gradient wind speeds are calculated by employing Georgiou's model (Georgiou 1985), which
145 gives the 10-min sustained wind speeds at 500 m to 2000 m above the ground surface (Cui and Caracoglia
146 2019; Pei et al. 2014, 2018). An example of the calculated gradient wind field is shown in Fig. 2.

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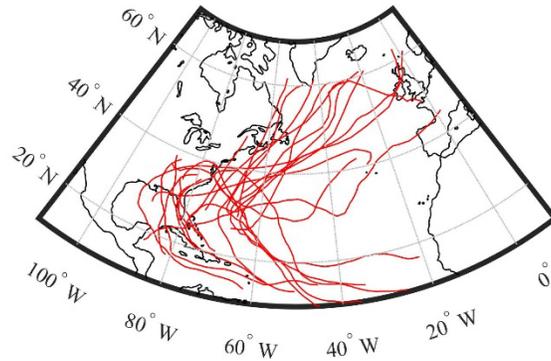


Fig. 1. Examples of the simulated hurricane tracks

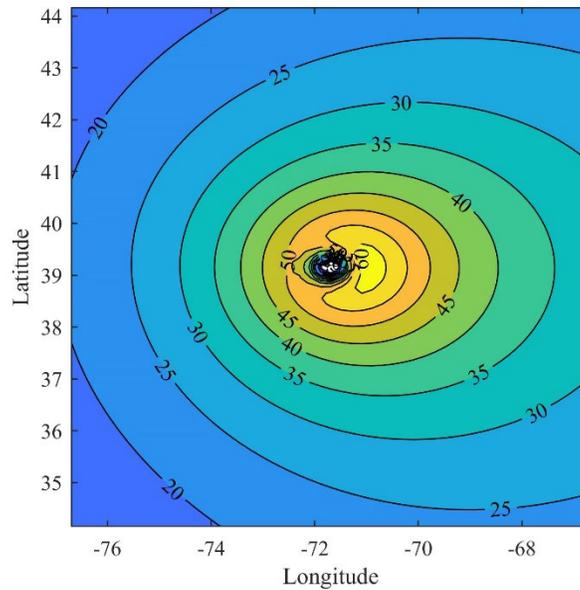


Fig. 2. Example of hurricane gradient wind field (m/s)

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151 The obtained hurricane gradient wind speeds V_g need to be converted to surface wind speeds V_{10} (10 m
152 above the ground or water) for wind force calculation on structures. The reduction factor V_g/V_{10} over water
153 proposed by Batts et al. is used in this research (Batts et al. 1980; Vickery et al. 2009a). A sea-land transition
154 factor obtained from the model given in Simiu and Scanlan (1996) is then utilized to calculate the surface
155 wind over land (open terrain with surface roughness $z_0 = 0.03 \text{ m}$) from the surface wind over water ($z_0 =$
156 0.0013 m). In addition, the surface wind speed over land approaches the fully transitioned value
157 asymptotically over a fetch distance as the wind moves from sea to land; therefore, the transition function
158 proposed in Vickery et al. (2009b) is employed here, which defines the percentage of the sea-land transition

159 as a function of the fetch distance. With the methods discussed in this section, the time series of the 10-min
160 sustained wind speeds at 10 m height and the corresponding wind directions at a location of interest
161 (assuming open terrain) during a hurricane may be obtained.

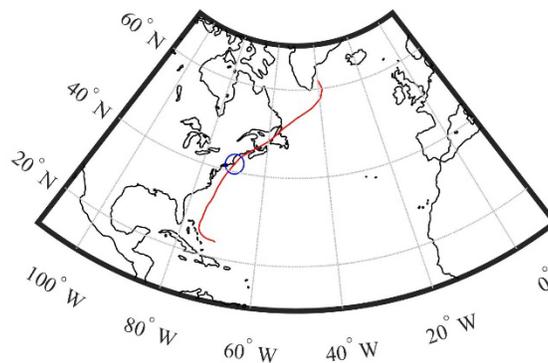
162 **Hurricane wind records collection and preprocess**

163 ASCE 7 wind hazard maps display wind speeds with a certain mean recurrence interval (MRI) for the entire
164 U.S., including hurricane prone regions (ASCE 2016b). However, much information regarding hurricane
165 winds is omitted in the ASCE 7 wind hazard maps, such as the variation of wind speeds and directions
166 during a hurricane, and the durations of hurricane winds. This kind of information, which are contained in
167 the time series of hurricane wind speeds and directions, are critical for structural response estimation and
168 risk analysis. Thus, in this section, a number of hurricane wind speed and direction records are collected
169 for a location of interest. In order to collect hurricane wind records for a region, the region is first discretized
170 into a series of grids and then hurricane wind records are collected for each grid.

171 ***Wind records for a location of interest***

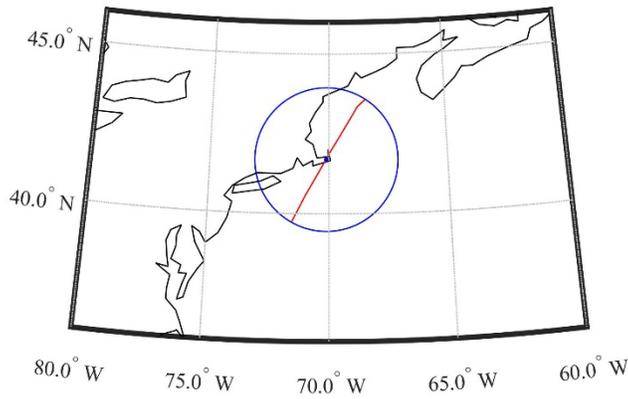
172 A location in Massachusetts with latitude 41.7 and longitude -70.1 is used as an example in this section.
173 Wind records are collected for this specific location from 10,000-year synthetic hurricanes developed by
174 Liu (2014). Examples of the collected 10-min sustained wind speed and wind direction records at the
175 location of interest are shown in Fig. 3 to Fig. 5 with the corresponding hurricane tracks. It is seen in Fig.
176 3(a), Fig. 4(a) and Fig. 5(a) that the hurricane eye usually moves thousands of miles from a hurricane's
177 genesis to dissipation. It is reasonable to assume that the wind speed induced by a hurricane that is very far
178 away is relatively small and can be neglected. Therefore, as suggested by Vickery et al. (2009c), hurricane
179 winds are considered only when the location of interest is within 250 km of the hurricane eye (see the blue
180 circles in Fig. 3 to Fig. 5). This limit on distance also provides a limit for the durations of the hurricane
181 wind records. Figure 3(c), Fig. 4(c) and Fig. 5(c) illustrate the absolute values of the wind speeds and the
182 wind directions in a polar coordinate system, while Fig. 3(d), Fig. 4(d) and Fig. 5(d) illustrate the hurricane
183 wind speeds in the North and East directions in a Cartesian coordinate system. Note that the wind direction

184 in the polar coordinate system is clockwise positive from the North direction. It is seen that the pattern of
185 wind speed and direction records are different for different hurricanes, which depends on a number of
186 factors, including the 7 parameters defining the hurricane eye tracks and wind fields. While the impacts of
187 the hurricane wind field as shown in Fig. 2 on the wind records is complex, a qualitative analysis of the
188 impact of hurricane eye tracks on the wind records provides examples of the range of loading developed
189 during hurricanes. Specifically, when the location of interest is very close to the hurricane eye track, the
190 record of the absolute values of the wind speeds usually has two peaks and the drop of the wind speed in
191 the middle is due to the near zero wind speed in the hurricane eye (see Fig. 3(c)). On the contrary, if the
192 location of interest is further from the hurricane eye track, the record of the absolute values of the wind
193 speeds will typically only have one peak (see Fig. 4(c) and Fig. 5(c)). The difference between Fig. 4 and
194 Fig. 5 is that the hurricane eye passes by the West or East side of the location of interest, which dominates
195 the variation of the wind directions as presented in these two figures.



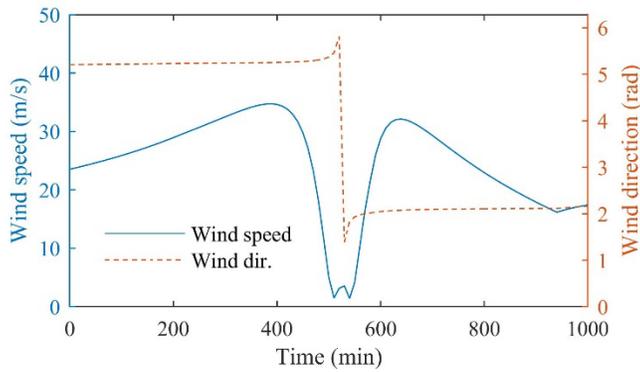
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(a) The whole hurricane track (the blue circle represents the 250 km limit)



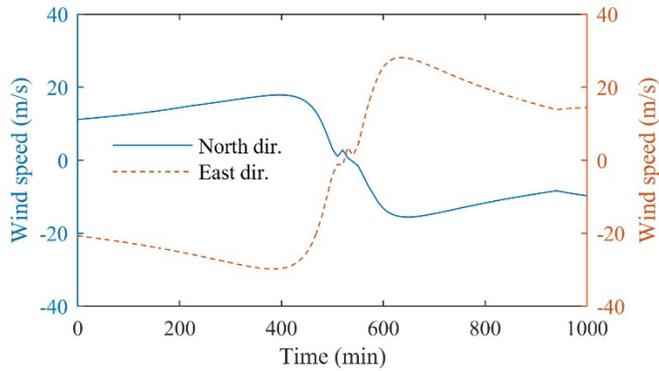
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(b) The hurricane track within the 250 km limit (blue circle) of the location of interest (blue dot)



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(c) Wind speed and direction records

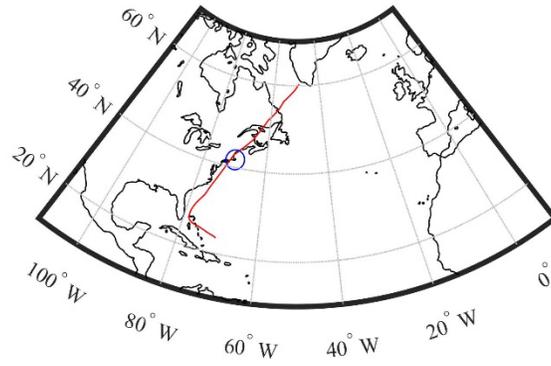


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(d) Wind speed records in the North and East directions

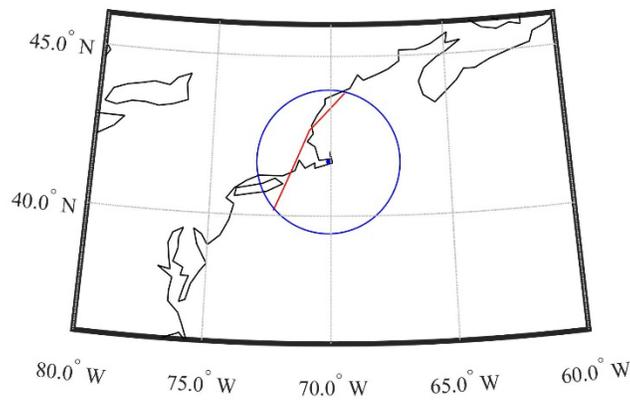
Fig. 3. An example of hurricanes going through the location of interest

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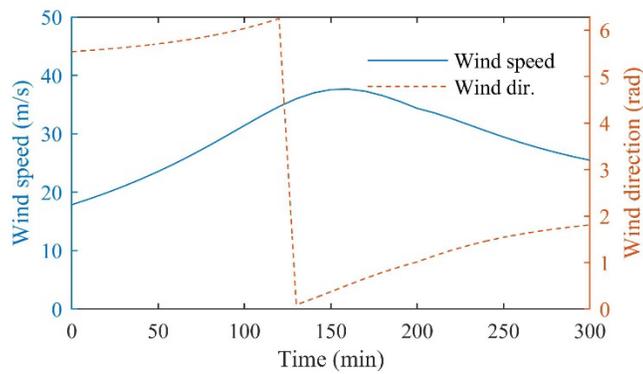
(a) The whole hurricane track (the blue circle represents the 250 km limit)

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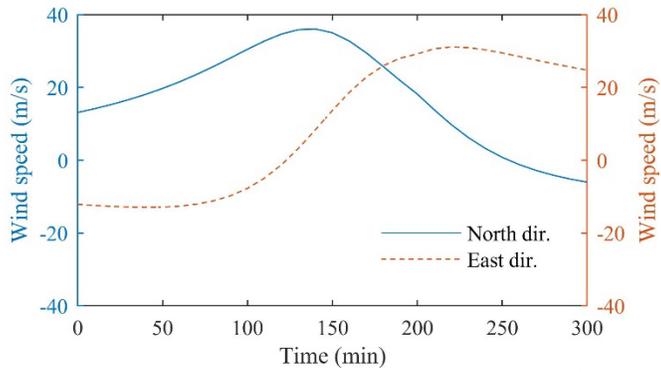


(b) The hurricane track within the 250 km limit (blue circle) of the location of interest (blue dot)

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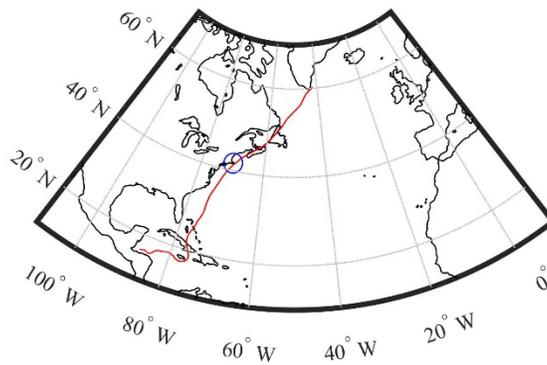


(c) Wind speed and direction records

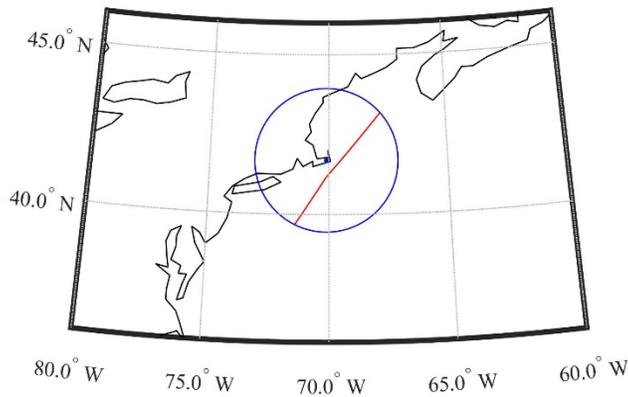


(d) Wind speed records in the North and East directions

Fig. 4. An example of hurricanes passing by the West side of the location of interest



(a) The whole hurricane track (the blue circle represents the 250 km limit)



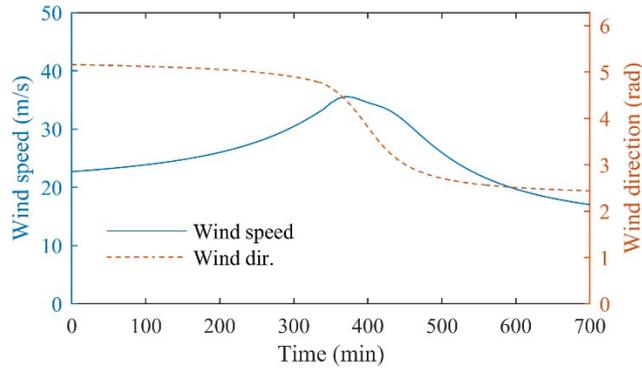
(b) The hurricane track within the 250 km limit (blue circle) of the location of interest (blue dot)

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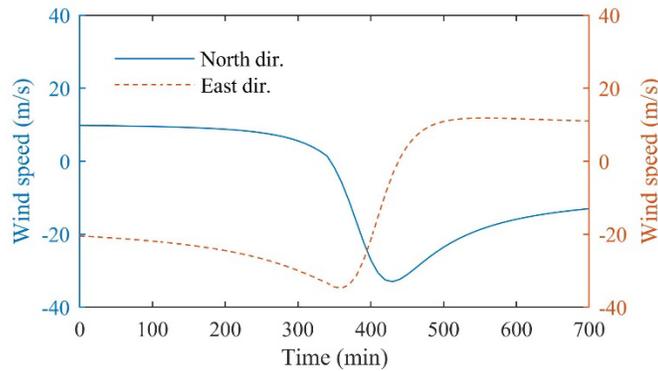
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(c) Wind speed and direction records



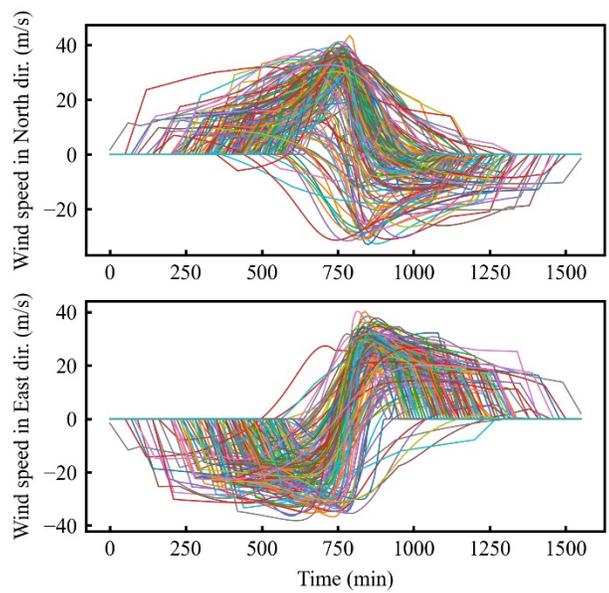
(d) Wind speed records in the North and East directions

Fig. 5. An example of hurricanes passing by the East side of the location of interest

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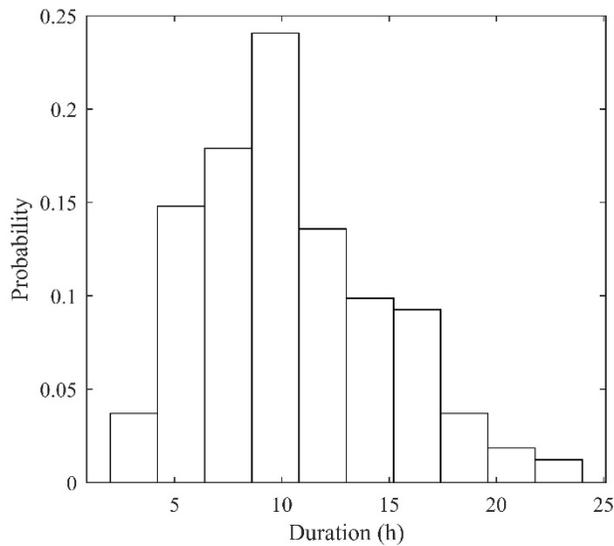
223 Wind records are first collected through applying the 250 km distance limit between the hurricane eye and
224 the location of interest. Hurricanes with very low wind speeds are then filtered out through a strategy that
225 only hurricanes whose maximum wind speeds at the location of interest are greater than the 50-year MRI
226 wind speed at the same location are considered. The 50-year MRI wind speed obtained from the ASCE 7
227 Hazard Tool (ASCE 2016a, b) is a 3-second gust wind speed at 10 m above ground (47 m/s for this location),
228 which is then converted to 10-min sustained wind speed at 10 m above ground (32.4 m/s for this location)
229 following the approach proposed by Simiu and Scanlan (Simiu and Scanlan 1996). This 50-year MRI 10-
230 min sustained wind speed is used as the threshold for comparison with the collected hurricane wind records
231 to get rid of those with small maximum wind speeds. Thus, a total of 162 hurricane wind records are
232 collected from the 10,000-year synthetic hurricanes, of which 160 records are shown in Fig. 6 within a
233 Cartesian coordinate system and are used in the following sections for clustering. Only 160 records are
234 included because 162 cannot be divided by the batch size (i.e., 16) employed in the training process of the

235 autoencoder, as will be introduced in the following sections. In addition, Fig. 7 presents the histogram of
236 the durations of all of the collected hurricanes with a mean duration of 12.4 hours. To avoid the impulse
237 effects, a 1-hour linear ramp-up and a 1-hour linear ramp-down are attached to the beginning and the end
238 of the collected wind records, respectively, as recommended in the Prestandard for Performance-Based
239 Wind Design (ASCE 2019). To be consistent with the hurricane wind records with 10-min intervals, the
240 ramp is added as six 10-min steps with a constant wind direction. Note that the ramps are not included in
241 Fig. 3 to Fig. 5 but included in Fig. 6 and Fig. 7. Moreover, as will be discussed in the following sections,
242 the collected wind records may have different durations, but the autoencoder needs the same size for the
243 input data of each record. Therefore, to facilitate training the autoencoder, zero paddings are added to the
244 beginning and the end of the records that are shorter than the longest one. Consequently, all records after
245 preprocess have the same length as the longest one. For each record, zero paddings at the beginning and the
246 end have the same length, which means all records after preprocessing have a midpoint that is usually
247 recorded when the hurricane eye is closest to the location of interest.



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Fig. 6. The 160 collected hurricane wind records resolved in two directions

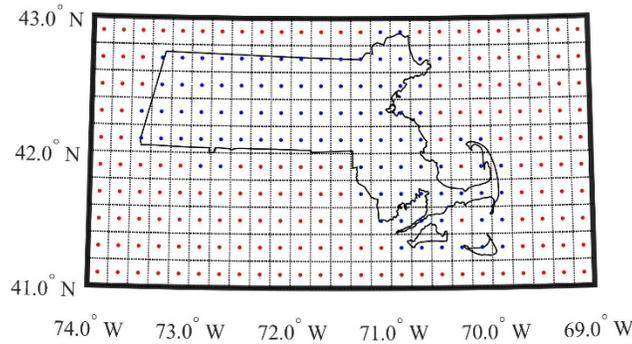


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251 Fig. 7. Histogram of the durations of the collected hurricane wind records

252 ***Wind records for a region***

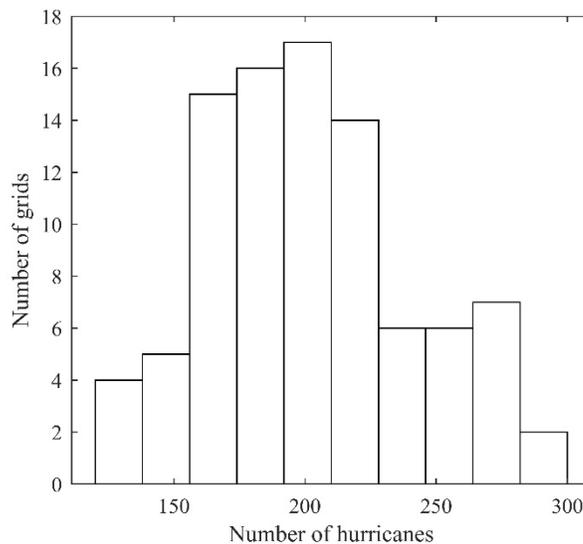
253 Hurricane wind records for different locations have different patterns. Consequently, it is appropriate to
 254 select site-specific wind records instead of generic wind records for all locations. Compared to generic wind
 255 records, site-specific wind records have lower uncertainties and thus can be used to predict responses of
 256 structures at a given location more accurately. To collect and select site-specific hurricane wind records for
 257 a region of interest, this research proposes that this region can be discretized into a set of grids and the
 258 centroid of each grid is used to represent the whole grid for recording wind speeds and directions. Thus,
 259 hurricane wind records can be collected for all centroids of the grids. To demonstrate this idea, Fig. 8 shows
 260 Massachusetts as a testbed, which is divided into 0.2° by 0.2° grids. In Fig. 8, the red dots represent the
 261 centroids of the grids that are not associated with Massachusetts, while the 92 blue dots represent the
 262 centroids of the grids that are associated with Massachusetts. The hurricane wind records collection
 263 procedure proposed in the previous sections is then run for all 92 grids. Note that when generating the wind
 264 records, the percentage of the sea-land transition is calculated for the centroid of each grid based on its fetch
 265 distance. In addition, the 50-year MRI wind speeds for the centroids of some grids cannot be obtained from
 266 the ASCE 7 Hazard Tool because these centroids are over the ocean (see Fig. 8); therefore, for these cases,

267 locations within the same grids but on the land are used to find the 50-year MRI wind speeds. Figure 9
 268 presents the histogram of the number of hurricanes collected for all 92 grids, with a mean value of 202.



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Fig. 8. Massachusetts is discretized into grids



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Fig. 9. Histogram of the number of collected hurricanes for the 92 grids

273 Wind records clustering and selection

274 The approximately 200 collected hurricane wind records for each grid are still too many for design checks
 275 and fragility development, especially considering the long durations of the wind records. Incremental
 276 dynamic analysis (IDA) may be used to estimate collapse probability of structures under hurricanes (Du et
 277 al. 2022; Vamvatsikos and Cornell 2002). This approach is computationally intensive because direct
 278 integration of the nonlinear dynamic governing equations is required over the entire duration of the
 279 hurricane wind records and this nonlinear time history analysis needs to be run multiple times with scaled

280 wind records. As such, it is important to limit the number of records used. Therefore, in this research, the
281 collected wind records for each grid are first clustered using a machine learning approach and then
282 approximately 1/10 of the wind records in each cluster are selected, which are combined together to create
283 approximately 20 selected wind records for each grid. This significantly reduces the number of nonlinear
284 time history analyses required, while still preserving the uncertainties in the collected records. This
285 procedure is similar to stratified sampling in statistics. Sampling is the process of selecting a subset from a
286 population so that the characteristics of the whole population can be estimated using this subset, while
287 stratified sampling is used by dividing the population into subpopulations (i.e., clusters in this paper), where
288 the elements within each subpopulation are similar, and performing sampling on each subpopulation.
289 Stratified sampling may improve the precision of the sample because sampling variability within each
290 subpopulation is smaller than the sampling variability on the entire population (Botev and Ridder 2017;
291 Parsons 2014). Specifically, the selected wind records can cover a spread of properties such as durations,
292 patterns of wind speed records, and patterns of wind direction records, because the collected wind records
293 are divided into clusters based on these properties.

294 ***Fully connected autoencoder***

295 Since the collected hurricane wind records are time series of both wind speed and direction with different
296 durations, it is challenging to cluster the records directly. To facilitate the clustering process, the high
297 dimensional wind records are first transformed into low dimensional latent features using an artificial neural
298 network named autoencoder (Aggarwal 2018; Bond et al. 2022; Tavakoli et al. 2020). The architecture of
299 the autoencoder for wind records at the location of interest given in the previous section is presented in Fig.
300 10. It is seen that the input matrix is the original wind speed records in the Cartesian system, which has two
301 columns with each column representing wind speed time histories in the North and East directions,
302 respectively. The input matrix is first flattened into a vector as the input layer of the fully connected
303 autoencoder and then passed through other hidden layers to reconstruct the data as another vector in the
304 output layer, which is finally reshaped to a matrix as the reconstructed wind speed records in the Cartesian

305 system. Even though the two columns of the input matrix are correlated time series of wind speeds in two
306 directions, this “flatten” and “reshape” process is reasonable because the correlations are considered in the
307 flattened vectors (input and output layers) through the weights of the fully connected layers. In another
308 word, “flatten” and “reshape” only change the appearance of the data while retaining the relationships and
309 correlations of the elements within the data. A fully connected autoencoder means that all the neurons in
310 one layer are connected to all the neurons in the next layer. The autoencoder architecture consists of two
311 parts: the encoder that compresses the high dimensional input data into the small-size latent feature vector,
312 and the decoder that utilizes the latent features to reconstruct the input data. In this example, the flattened
313 wind speeds in the input layer are transformed into 5 latent features through the encoder process, which are
314 then expanded to form the reconstructed but still flattened wind records in the output layer through the
315 decoder process. The hidden layers with a nonlinear activation function (Tanh) are included to enhance the
316 power of this autoencoder so that it can map the input data into much smaller dimensional spaces. Here
317 Tanh is adopted because it has better performance than other activation functions based on numerical tests
318 in this research. This autoencoder architecture requires that all input matrices have the same size; thus, the
319 size of the longest wind record is used as the size of the input matrices and zero padding is added to the
320 beginning and the end of all other shorter wind records. This strategy retains all information in the wind
321 records. In this example, the longest record has 156 data points (including the ramp-up and ramp-down)
322 with 10-min intervals, so the number of rows of the input matrices is 156.

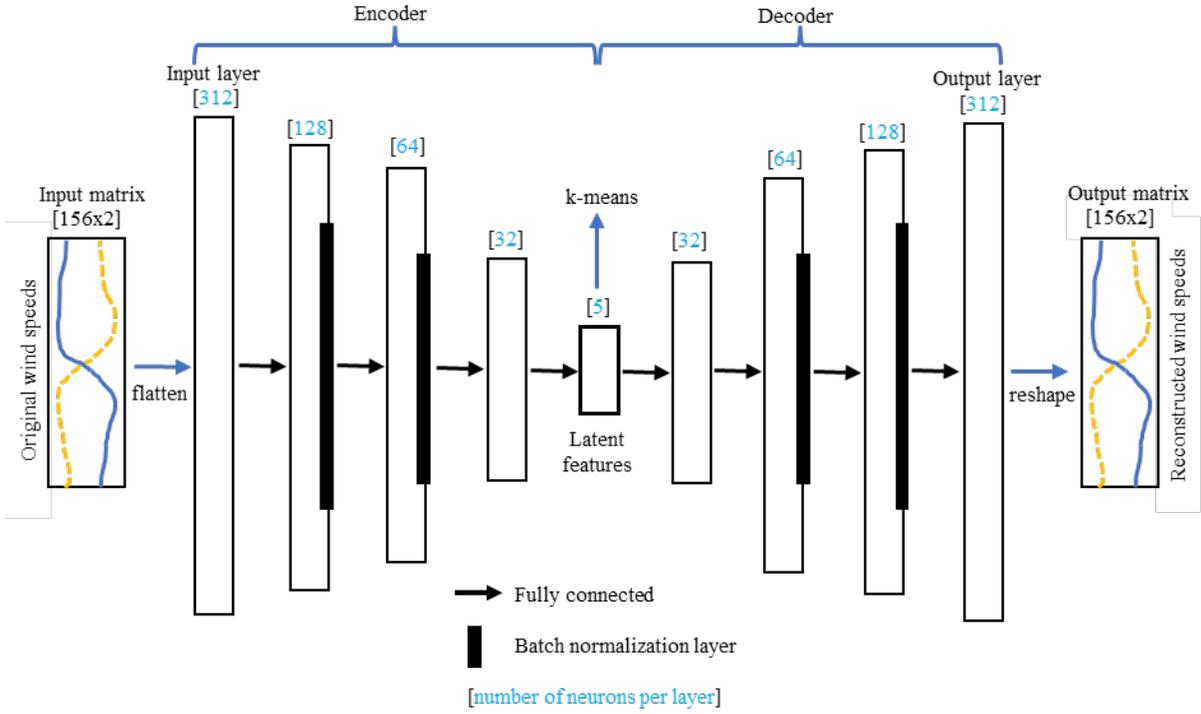
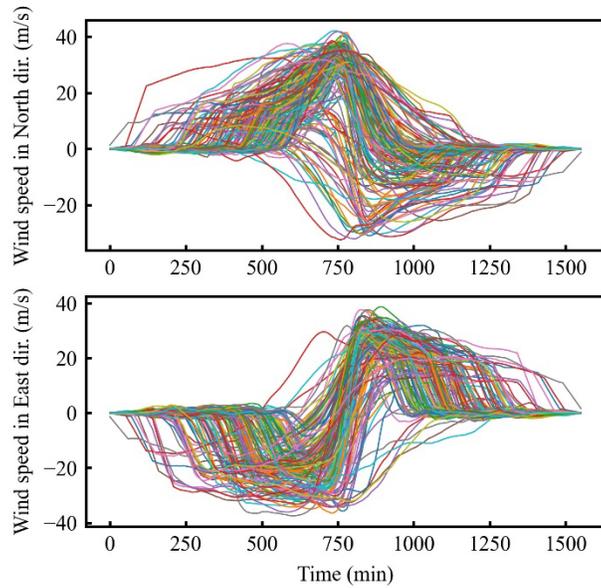


Fig. 10. The proposed autoencoder architecture

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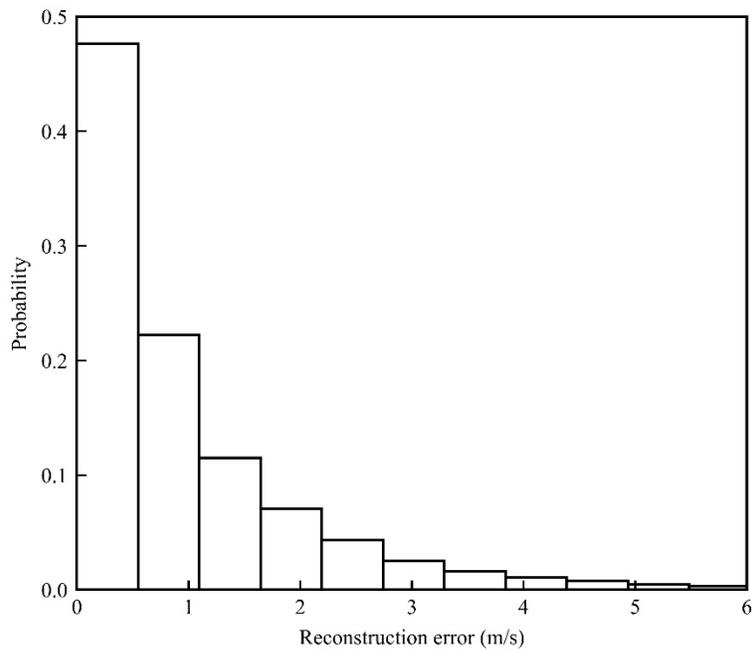
325 The training of this autoencoder is conducted by minimizing the error between the reconstructed data in the
 326 output layer and the input data, which ensures that the latent features can represent the important patterns
 327 of the wind records. The Adaptive Moment Estimation (Adam) algorithm is adopted for stochastic
 328 optimization and batch normalization is added to some hidden layers as shown in Fig. 10 to address the
 329 exploding and vanishing gradient problems (Aggarwal 2018). Since the chosen batch size is 16, only 160
 330 of the collected 162 wind records are used for the training process. In addition, Fig. 11 illustrates the
 331 reconstructed 160 wind records in the North and East directions after training the proposed autoencoder
 332 neural network. The histogram of the reconstruction error between the original and the reconstructed wind
 333 records is shown in Fig. 12, which demonstrates that the reconstructed records match well with the original
 334 ones and the latent features hold the most important characteristics of the wind records. It should be noted
 335 that since the 312 data points in the input layer is compressed into only 5 latent features, there must be some
 336 loss of information in this process and the discrepancies between the original and the reconstructed records
 337 are inevitable. However, these discrepancies are usually induced by noise or other nonsignificant factors;

338 therefore, the low dimensional latent features should be adequate for clustering because the important
339 information has been extracted through the autoencoder.



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Fig. 11. The 160 reconstructed wind records in two directions for the location of interest



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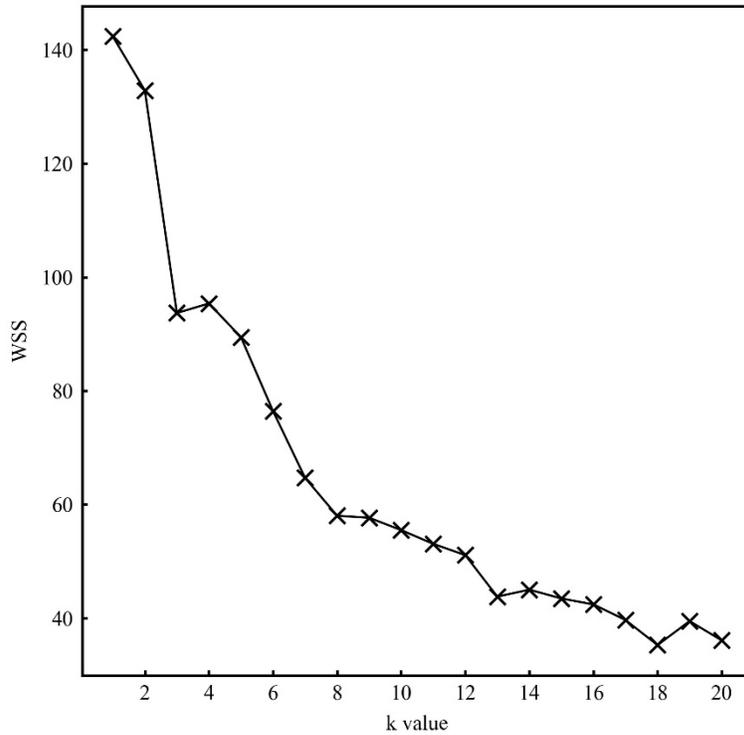
Fig. 12. Histogram of the reconstruction error

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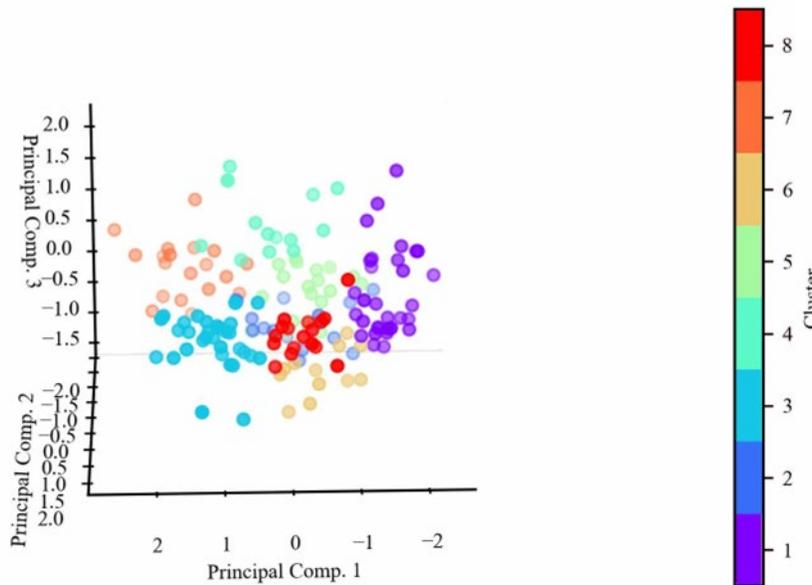
346 ***Clustering and selection based on latent features***

347 The location of interest studied in the previous sections is used here as an example. After the training
348 process, all wind speed time series are converted into latent feature vectors, on which the k-means algorithm
349 is applied for clustering. The goal of clustering is to maximize the similarity of data within each cluster and
350 maximize the dissimilarity of data in distinct clusters. Therefore, one can take a subset of the data in a
351 cluster to represent all data in that cluster, the accuracy of which depends on the number of clusters used.
352 Here, the elbow rule is adopted to find an optimal number of clusters (Thorndike 1953). To do so, the k-
353 means algorithm has been run multiple times on the latent features with different number of clusters ranging
354 from 2 to 20. For this example, when the number of clusters k equals 8, the Within-Cluster-Sum of Squared
355 Errors (WSS) curve reaches its elbow as shown in Fig. 13. Therefore, the 160 hurricane wind records are
356 divided into 8 clusters. Since it is difficult to show the 5 latent features on a 2D or 3D figure, principal
357 component analysis is performed on the latent features and the first 3 principal components are plotted in
358 Fig. 14 to demonstrate the results of the k-means clustering. This is acceptable because the first 3 principal
359 components possess 82% of the variation of the 5 latent features and it is believed that the 5 latent features
360 must show better performance than the 3 principal components if they can be plotted in a figure. In Fig. 14,
361 the first 3 principal components are presented using 8 different colors for the 8 clusters, from which it may
362 be seen that the hurricane wind records are clustered well because the principal components of different
363 clusters have rare overlaps and the principal components of each cluster are gathered closely around their
364 centroid.



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Fig. 13. The WSS for different number of clusters



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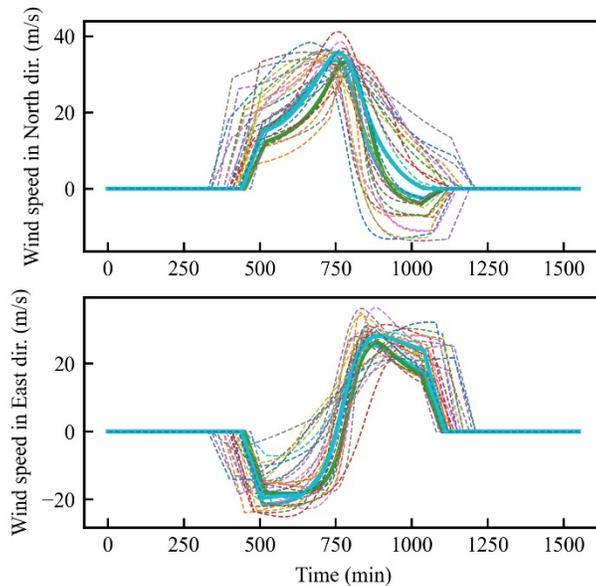
Fig. 14. Principal components of the latent features for the 8 clusters

369 To demonstrate the effectiveness of the proposed clustering approach, Fig. 15 to Fig. 22 illustrate the
 370 hurricane wind speeds and tracks of the 8 clusters. It is seen that the clustering results are successful,
 371 because hurricane wind speeds and durations within each cluster have similar patterns. Specifically,

372 Clusters 2 and 7 have hurricanes whose tracks pass by the East side of the location of interest, while other
373 clusters have hurricanes whose tracks pass by the West side of the location of interest. The number of
374 hurricanes in each cluster from Cluster 1 to Cluster 8 are 31, 17, 31, 13, 20, 12, 19 and 17, respectively. So
375 much more hurricanes pass by the West side of the location of interest than the East side. The main
376 difference between Cluster 2 and Cluster 7 is that the durations of hurricanes in Cluster 7 is longer. For the
377 clusters passing by the West side of the location of interest, Cluster 3 and Cluster 4 has the shortest and the
378 longest durations, respectively, while Clusters 1, 5, 6 and 8 have durations in the middle. Clusters 6 and 8
379 have very similar durations, but they are divided into two clusters because they have different shapes for
380 the profile of the wind speed time histories. There are outliers in some clusters such as the one with abrupt
381 changing of the storm heading direction as seen in the figure of hurricane tracks of Cluster 2. This can be
382 expected because the k-means algorithm cannot eliminate all outliers, but instead assigns outliers to their
383 closest cluster. Usually, outliers are rare and their latent feature points are far from the centroid of all points
384 in a cluster. Therefore, the outlier commonly will not be included to the final suite of wind records
385 considering the selection strategy within a cluster that will be introduced below. The wind field shown in
386 Fig. 2 also has impacts on the clustering results, which cannot be explained explicitly here because its
387 information is included in the latent features through the operations on the wind records during the training
388 of the autoencoder.

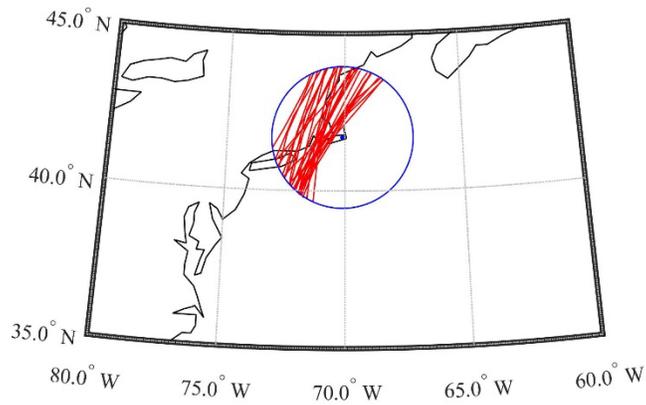
389 Considering the computational demand of nonlinear time-history analyses that these wind records will be
390 used to perform, approximately 1/10 of the hurricanes in each cluster are selected and combined together
391 as the final suite of hurricane wind records. The number of records selected from each cluster is proportional
392 to the total number of records in each cluster, which results in 3, 2, 3, 1, 2, 1, 2 and 2 records from each
393 cluster, respectively. This strategy is used to make sure the proportions of different patterns of wind records
394 are similar in the selected 16 hurricanes and the original 160 ones. It is also reasonable to make sure the
395 selected records from each cluster are the most representative ones. To achieve this goal, the clustering
396 results of the latent features are used, and for each cluster it is recommended to select those records whose

397 latent feature points are the closest to the centroid of all latent feature points in that cluster. The selected
398 records for each cluster are highlighted in bold solid lines as shown in Fig. 15(a) to Fig. 22(a), which is a
399 demonstration of the validity of this selection strategy within a cluster. In Fig. 15(a) to Fig. 22(a), all wind
400 records are shown in different colors and curves resolved from the same record are shown in the same color
401 in the upper subplot and lower subplot. It is seen that the selected records are representative, as they are
402 near the middle of all the records. The total of 16 selected hurricanes can be employed to represent
403 uncertainties in wind loading for design check and fragility development for structures at the location of
404 interest. Note that these selected wind records are only time series of 10-min mean wind speed at 10 meters
405 height. If one wants to use them for structural dynamic analysis, the fluctuating wind speeds and the
406 atmospheric boundary layer should be considered.



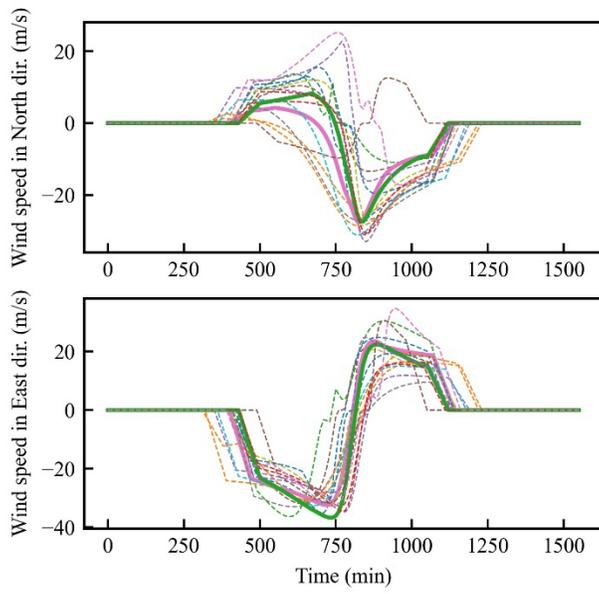
(a) Wind records of Cluster 1

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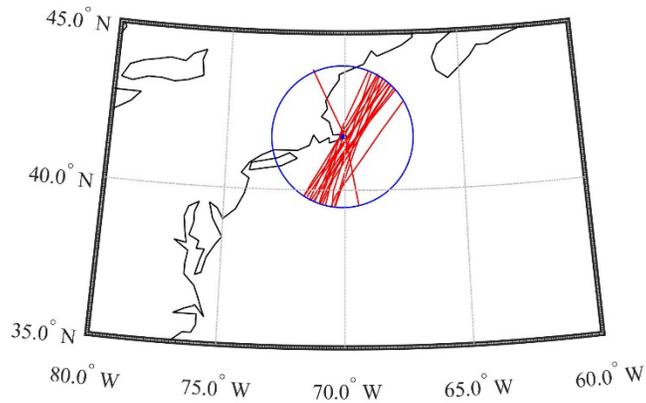
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(b) Hurricane eye tracks of Cluster 1
Fig. 15. Hurricanes in Cluster 1



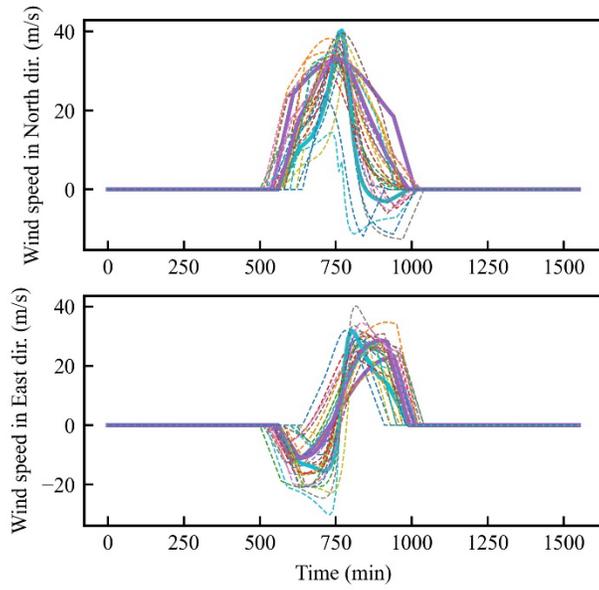
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(a) Wind records of Cluster 2

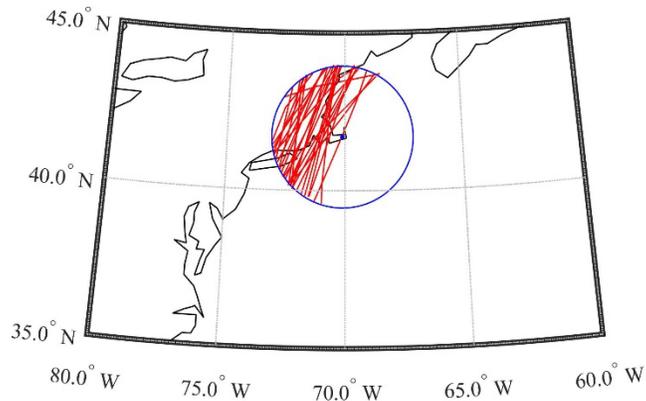


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(b) Hurricane eye tracks of Cluster 2
Fig. 16. Hurricanes in Cluster 2



(a) Wind records of Cluster 3

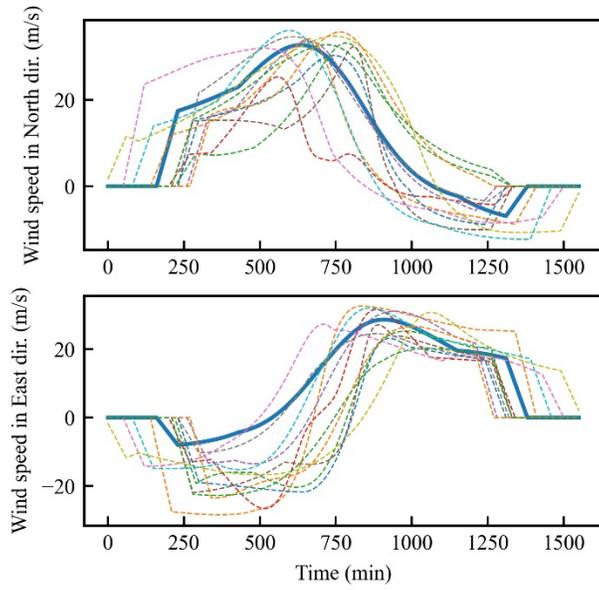


(b) Hurricane eye tracks of Cluster 3

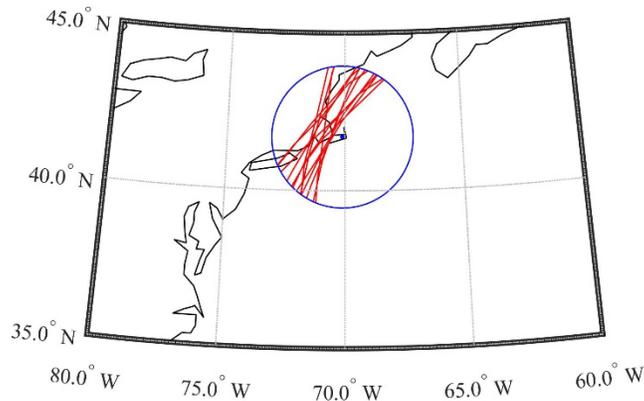
Fig. 17. Hurricanes in Cluster 3

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(a) Wind records of Cluster 4

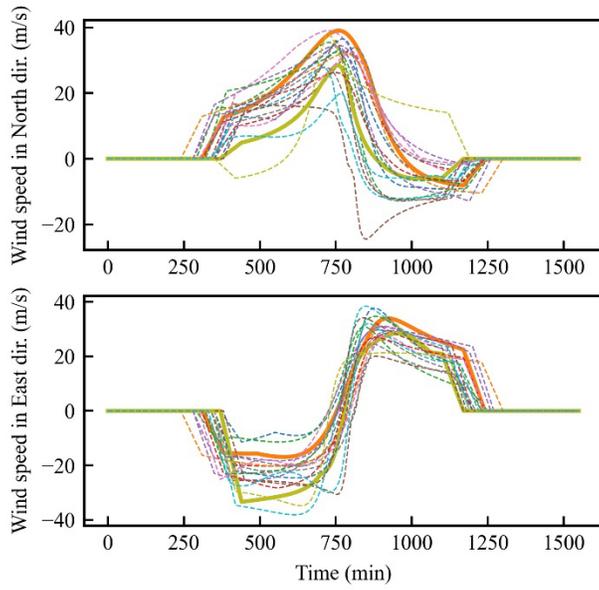


(b) Hurricane eye tracks of Cluster 4

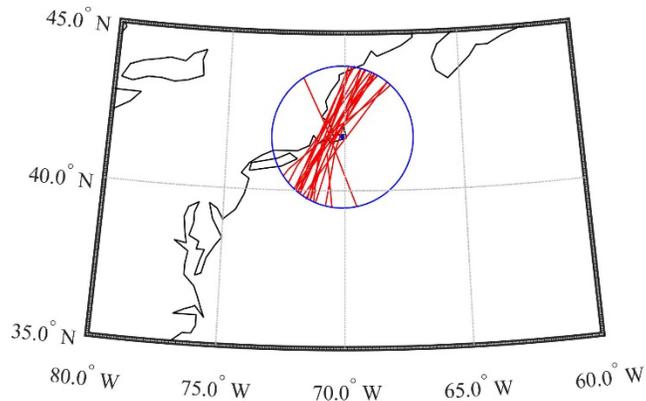
Fig. 18. Hurricanes in Cluster 4

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(a) Wind records of Cluster 5

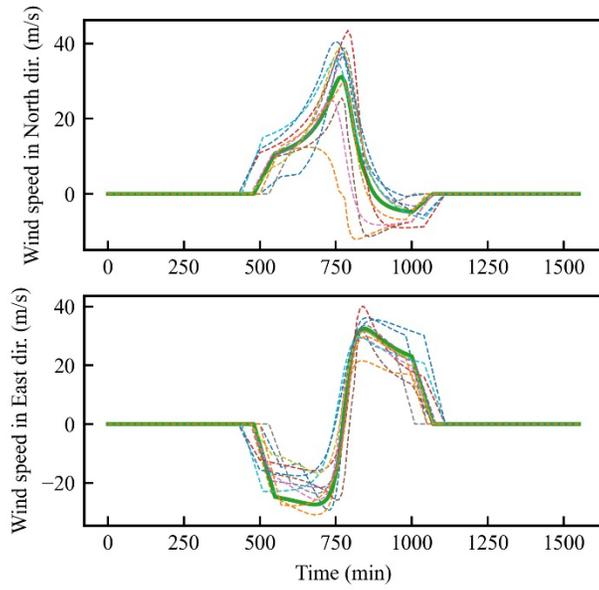


(b) Hurricane eye tracks of Cluster 5

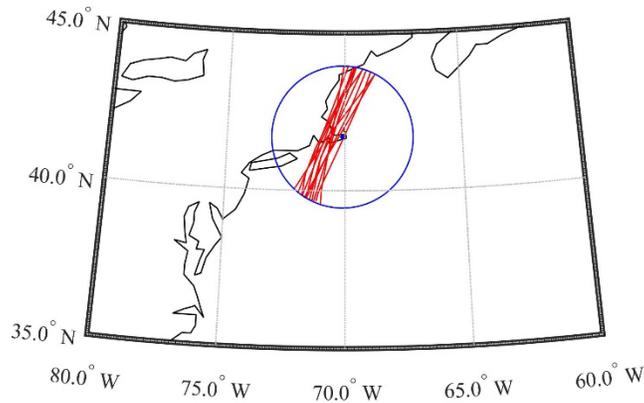
Fig. 19. Hurricanes in Cluster 5

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(a) Wind records of Cluster 6

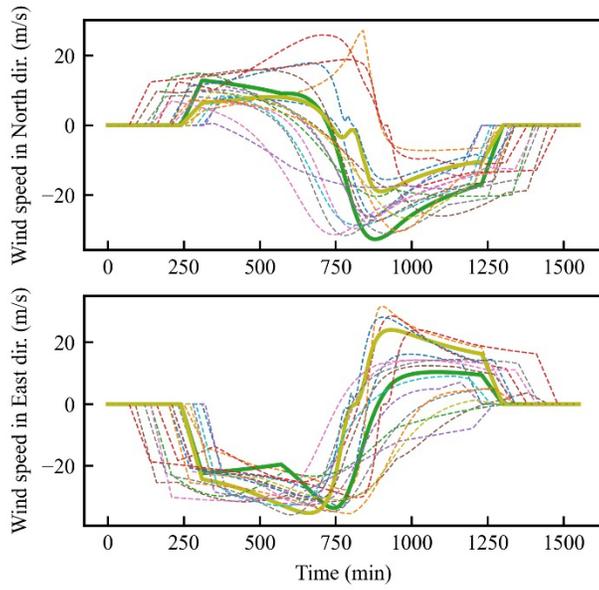


(b) Hurricane eye tracks of Cluster 6

Fig. 20. Hurricanes in Cluster 6

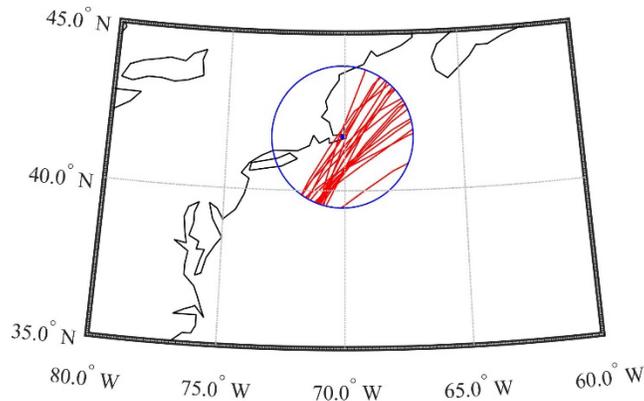
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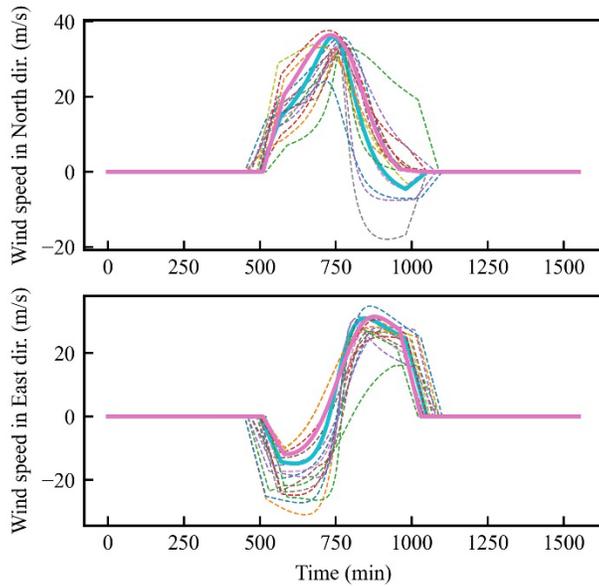
(a) Wind records of Cluster 7



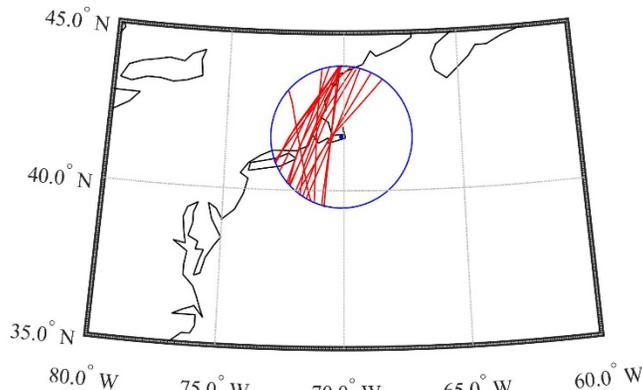
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(b) Hurricane eye tracks of Cluster 7

Fig. 21. Hurricanes in Cluster 7



(a) Wind records of Cluster 8



(b) Hurricane eye tracks of Cluster 8

Fig. 22. Hurricanes in Cluster 8

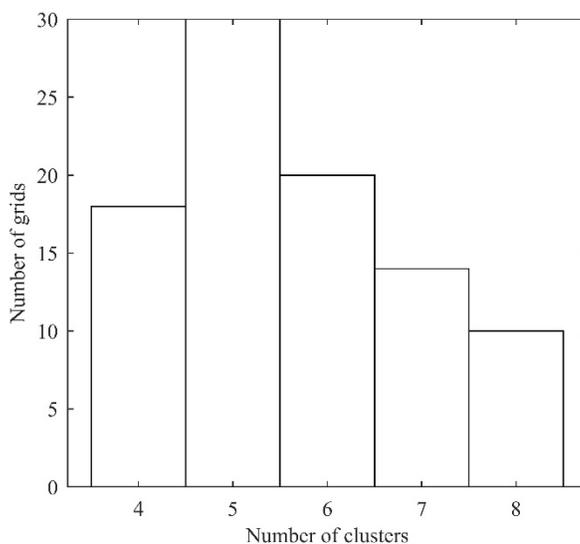
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447 ***Wind records selection for a region***

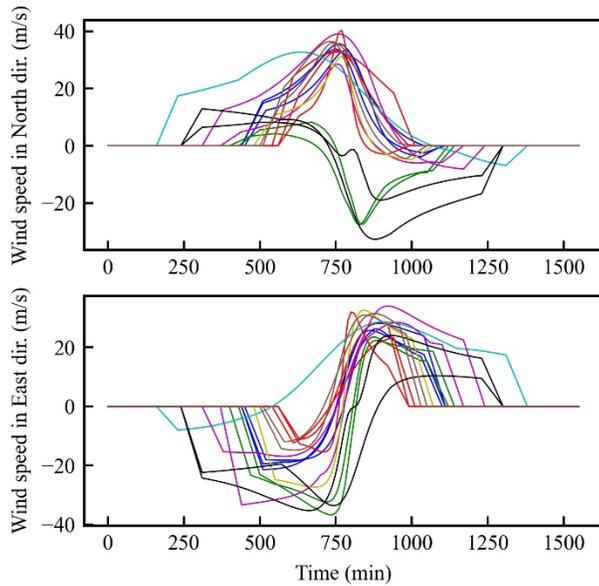
448 As a case study for regional analysis, Massachusetts has been divided into 92 grids and wind records has
 449 been collected for each grid. Here the procedures for wind records clustering and selection introduced in
 450 the previous sections are applied to all 92 grids. The same autoencoder architecture is used for all grids
 451 except for the slightly different sizes of the input vectors for different grids, which is because the maximum
 452 duration of the collected records for different grids may be different. The same k-means algorithm is also
 453 adopted for clustering on the latent features; however, the number of clusters may vary for different grids
 454 because it is dynamically determined using the elbow rule. The histogram of the number of clusters for all

455 grids is presented in Fig. 23 with a mean value of 5.65. Since approximately 200 hurricane wind records
456 are collected for each grid, then approximately 20 records are selected for each grid according to the method
457 introduced in the previous sections. Finally, a wind map is generated so that a suite of hurricane wind speed
458 and direction records can be provided for any locations in Massachusetts. For example, Fig. 24(a) gives 16
459 wind records selected from 8 clusters for a grid whose centroid has a latitude of 41.7 and a longitude of -
460 70.1 (this location is used in the previous sections), while Fig. 24(b) gives 19 wind records selected from 4
461 clusters for a grid whose centroid has a latitude of 42.1 and a longitude of -72.5. Here the wind records
462 selected from the same cluster are shown in the same color, and it is seen that wind records within the same
463 cluster have similar characteristics in terms of wind speeds, directions, and durations. This approach
464 provides an alternative to the ASCE 7 wind map. The ASCE 7 wind map can only provide a wind speed
465 without any information of variation of the wind speed and direction during a hurricane. This methodology
466 can be generalized to any other regions besides Massachusetts.

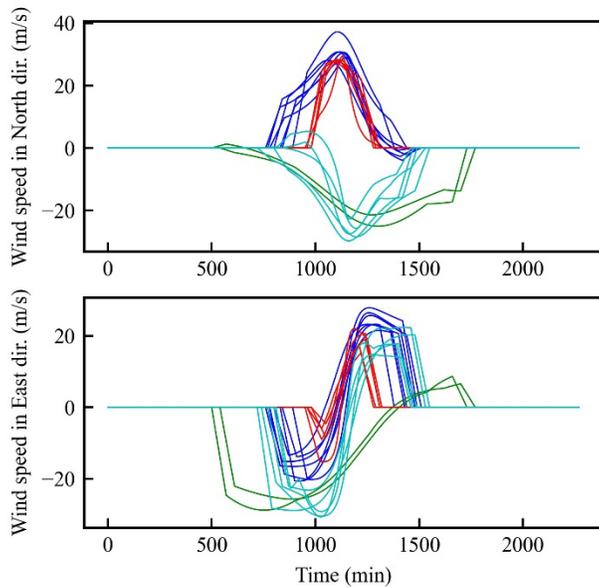


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Fig. 23. Histogram of the number of clusters for all grids



(a) For a grid whose centroid has a latitude of 41.7 and a longitude of -70.1



(b) For a grid whose centroid has a latitude of 42.1 and a longitude of -72.5

Fig. 24. Examples of selected hurricane wind records

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474 Conclusions

475 This paper presents a machine learning approach for collecting and selecting hurricane wind speed and
 476 direction records for a location and a region, which can be used for efficiently developing fragility curves
 477 or assessing probabilistic behaviors of structures considering uncertainties in hurricanes. The selected
 478 hurricane wind records are supposed to address the uncertainties in hurricanes because 1) they are selected

479 from 10,000-year synthetic hurricanes and 2) the collected records with similar properties are first divided
480 into clusters and then the most representative ones are selected from each cluster. The preprocess of the
481 wind records is also important since it can remove hurricanes with very small wind speeds and limit the
482 durations of the records to a relatively short time. The proposed autoencoder architecture is shown to be
483 able to reconstruct the wind speed time series and compress them into low dimensional latent features. The
484 clustering results based on the latent features using the k-means algorithm are successful, because the points
485 in the latent space are divided clearly into several clusters, and the wind records in the same cluster exhibit
486 similar properties in duration, hurricane track, and changing of wind speed and directions. A method is also
487 proposed to select the most representative records from each cluster based on the clustering results of latent
488 features. This hurricane selection procedure is demonstrated using wind records from both a location and a
489 region. For the regional hurricane selection, Massachusetts is used as a testbed, and it is discretized into a
490 set of grids with performing the proposed hurricane selection procedure on each grid. Usually, approximate
491 20 wind records are selected for a location, which make the nonlinear structural analysis feasible for
492 uncertainty propagation simulation under hurricanes.

493 **Data availability**

494 Some or all data, models, or code that support the findings of this study are available from the corresponding
495 author upon reasonable request. Some or all data, models, or code used during the study were provided by
496 a third party. Direct requests for these materials may be made to the provider as indicated in the
497 Acknowledgements.

498 **Acknowledgement**

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