

# Pyramid of Thought: Enhancing the Chain of Thought with the Fibonacci Sequence and the Inner Thought Journal

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## Abstract

Recent advances in large language models (LLMs) have demonstrated their remarkable abilities in complex language tasks. However, achieving the depth and flexibility of human reasoning remains a challenge. Inspired by the power of step-by-step reasoning highlighted in "Chain-of-Thought Prompting Elicits Reasoning in Large Language Models," this paper introduces the "Pyramid of Thought" framework. This framework leverages principles of Euclidean geometry, the Fibonacci sequence, and psychological engagement to create structured, adaptable AI responses while promoting transparent and intuitive communication.

The "Pyramid of Thought" uses a dynamic layer mechanism, adjustable via linear, logarithmic, or Fibonacci-based scaling. This aligns the AI's thought process with natural mathematical patterns. Mirroring psychological principles, this approach aims to promote user engagement. Each layer builds on the previous one, starting with foundational facts ("Five Ws") and progressing through reasoning steps ("How," "Then"), culminating in an "Apex" of analysis or insight. An inner thought journal maintains contextual richness.

The flexible and iterative nature of the "Pyramid of Thought" reflects the emphasis on refinement and evolution found in conceptual modeling. Experiments will evaluate its effectiveness against traditional AI response methods. Metrics will include user engagement, response coherence, satisfaction, and the model's ability to communicate its reasoning process transparently. We anticipate that the "Pyramid of Thought" will produce more intuitive, meaningful, and thought-provoking interactions, aligning with the goals of conceptual modeling in simulation. This work contributes to the development of AI systems that better emulate human reasoning patterns and foster clearer communication.

Standard Prompting	Chain-of-Thought Prompting	Pyramid-of-Thought Prompting
<p><b>Model Input</b></p> <p>Q: Roger has 5 tennis balls. He buys 2 more cans of tennis balls. Each can has 3 tennis balls. How many tennis balls does he have now?</p> <p>A: The answer is 11.</p> <p>Q: The cafeteria had 23 apples. If they used 20 to make lunch and bought 6 more, how many apples do they have?</p>	<p><b>Model Input</b></p> <p>Q: Roger has 5 tennis balls. He buys 2 more cans of tennis balls. Each can has 3 tennis balls. How many tennis balls does he have now?</p> <p>A: Roger started with 5 balls. 2 cans of 3 tennis balls each is 6 tennis balls. <math>5 + 6 = 11</math>. The answer is 11.</p> <p>Q: The cafeteria had 23 apples. If they used 20 to make lunch and bought 6 more, how many apples do they have?</p>	<p><b>Model Input</b></p> <p>Q: Roger has 5 tennis balls. He buys 2 more cans of tennis balls. Each can has 3 tennis balls. How many tennis balls does he have now?</p> <p>A: Roger started with 5 balls. 2 cans of 3 tennis balls each is 6 tennis balls. <math>5 + 6 = 11</math>. The answer is 11.</p> <p>Q: The cafeteria had 23 apples. If they used 20 to make lunch and bought 6 more, how many apples do they have?</p>
<p><b>Model Output</b></p> <p>A: The answer is 27. ❌</p>	<p><b>Model Output</b></p> <p>A: The cafeteria had 23 apples originally. They used 20 to make lunch. So they had <math>23 - 20 = 3</math>. They bought 6 more apples, so they have <math>3 + 6 = 9</math>. The answer is 9. ✅</p>	<p><b>Model Output</b></p> <p>A: Looks like we've got a good grip on those calculations! Roger indeed has 11 tennis balls now, and the cafeteria is sitting pretty with 9 apples. It's all about tracking those additions and subtractions, making sure we don't lose count along the way.</p>

Fig. 1. Pyramid-of-thought prompting enables large language models to reason step-by-step, enhancing understanding and communication.

## 1- Introduction

### The Intersection of Artificial Intelligence and Sacred Geometry

The quest to enhance artificial intelligence (AI) with human-like reasoning capabilities has led to the exploration of novel methodologies, including the incorporation of sacred geometry into AI systems. Recent advancements in large language models (LLMs) have significantly pushed the boundaries of what AI can achieve in terms of processing and generating complex language constructs. However, the challenge of imbuing AI with the depth and flexibility of human reasoning remains. The "Pyramid of Thought" framework emerges as a groundbreaking approach, marrying the computational prowess of AI with the profound mathematical principles found in sacred geometry and the Fibonacci sequence. This innovative framework aims to mimic human thought processes, thereby enhancing AI's ability to generate more nuanced and context-aware responses.

### Objectives and Novel Contributions

This paper proposes the "Pyramid of Thought," a framework inspired by human reasoning that aims to improve current LLM responses. The framework builds upon principles from Euclidean geometry and the Fibonacci sequence to potentially make AI communication more transparent and user-friendly. Our hope is that this approach can help bridge the gap between how AI models currently respond and the way humans naturally process information. By fostering more intuitive interactions, we believe the "Pyramid of Thought" could contribute to a more engaging user experience with AI systems.

### Background

The "Pyramid of Thought" draws inspiration from the elegance of mathematical patterns and techniques aimed at boosting user engagement. The framework leverages insights from how geometric principles influence perception, as well as the natural structure of the Fibonacci sequence. This approach aligns with the "Chain-of-Thought Prompting" method (Wei et al., "Chain-of-Thought Prompting Elicits Reasoning in Large Language Models"), aiming to make AI responses more coherent and contextually relevant. The "Pyramid of Thought" adds a dynamic scaling mechanism (linear, logarithmic, or Fibonacci-based) designed to potentially improve the coherence and contextual understanding exhibited by AI models. Building upon prior work in AI literacy (Carolus et al., "MAILS - Meta AI Literacy Scale: Development and Testing of an AI Literacy Questionnaire..."), and values-based AI reasoning (Osmana & d'Inverno, "Modelling Human Values for AI Reasoning"), the framework also has the potential to enhance user experiences by fostering greater alignment between AI responses and human values.

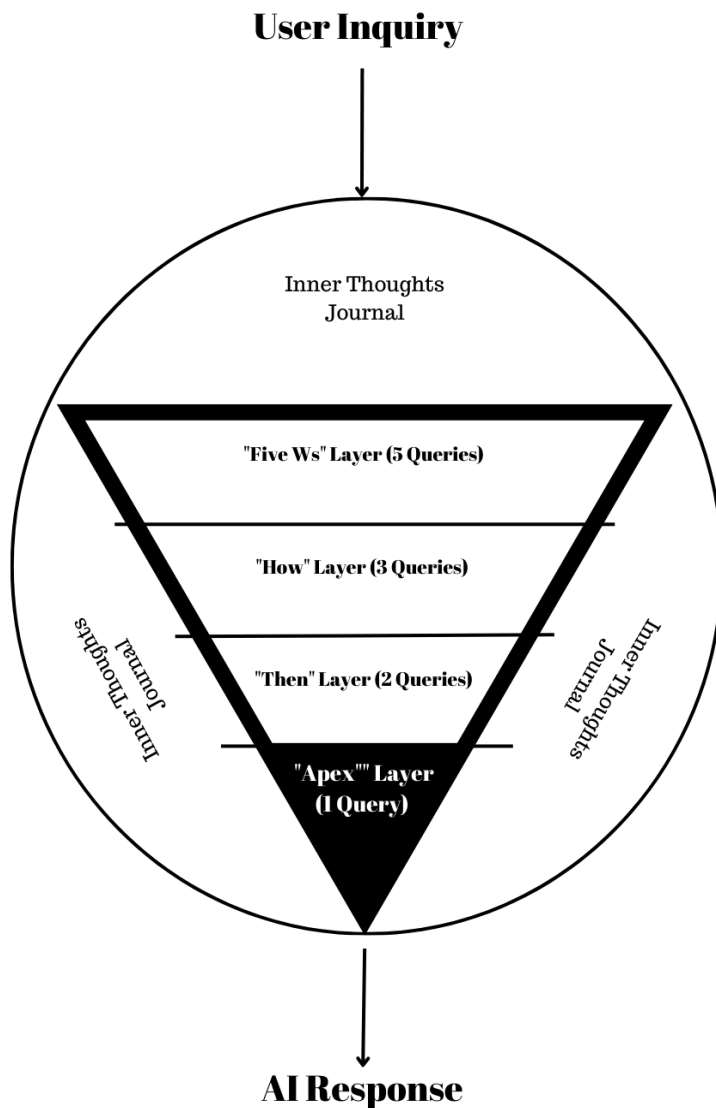


Fig. 2. Illustration of the Pyramid of Thought framework.

## The Pyramid of Thought Framework

The "Pyramid of Thought" framework is conceptualized as a multi-layered structure, where each layer represents a step in the AI's reasoning process, from basic facts to complex insights. This progression is guided by the Fibonacci sequence, ensuring that each response is not only logically coherent but also intuitively structured. By employing advanced sequence modeling, decision trees, and contextual weighting, the framework maintains a rich contextual understanding throughout the AI's reasoning process. The adaptability introduced through variable depth scaling allows the AI to tailor its reasoning depth to the complexity of the task, ensuring efficient and precise responses. Our implementation strategy involves integrating this framework with existing AI systems to enhance response generation, focusing on user engagement, response coherence, and satisfaction as primary evaluation metrics. The

introduction of the "Pyramid of Thought" framework marks a pivotal moment in the evolution of AI systems. By harnessing the principles of sacred geometry and the Fibonacci sequence, this framework aims to produce AI interactions that are not only more coherent but deeply resonate with users on an intuitive level. As we move forward, this framework promises to redefine the landscape of AI communication, bridging the gap between artificial intelligence and human cognition with every interaction.

## 2- Review of Euclidean and Sacred Geometry in AI

Euclidean geometry provides the fundamental framework for how AI systems comprehend and operate in physical spaces - identifying objects, calculating distances, mapping movements. However, sacred geometry offers alternate perspectives on shapes and spaces, seen through more metaphorical or philosophical lenses.

Integrating some of these principles could allow AI to develop a deeper awareness of forms, patterns and relationships. For example, algorithms modeled after the Fibonacci sequence or natural spirals may excel at generating

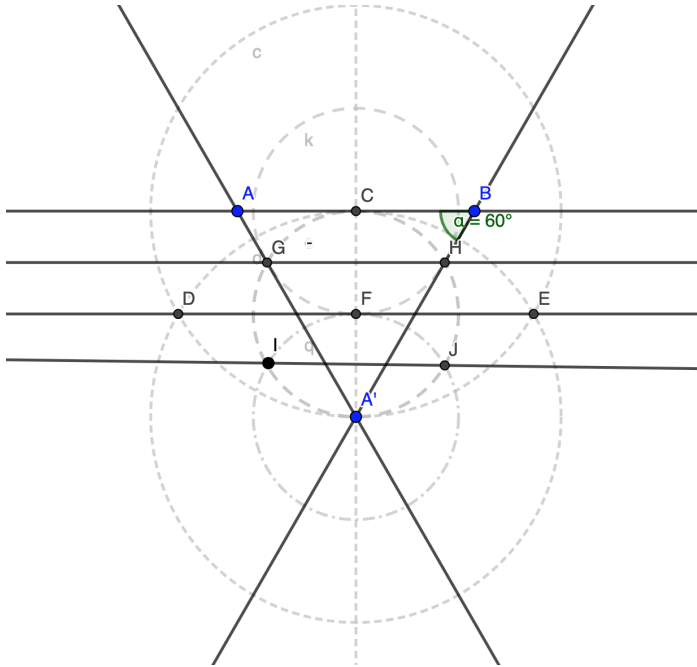


Fig. 3. Euclidean geometry diagram illustrating circle properties, angle bisectors, and line reflections.

creative designs that appeal to the human sense of beauty.

Or computer vision systems could analyze scenes by matching objects and landscapes against libraries of sacred geometry motifs.

However, effectively translating these qualitative concepts into computational models remains challenging. Symbolic meanings and notions of harmony are highly subjective. More research is needed to systematically encode the principles of sacred geometry using mathematical representations that AI can process. With diligent effort, the fusion of these geometric schools of thought could significantly expand the higher reasoning capacities of AI. Blending Euclidean objectivity and rigor with the subjectivity of sacred geometry may enable AI to develop its own interpretations of patterns and spaces. This could catalyze emergent behaviors we cannot yet envision - perhaps resonating with the deepest levels of human cognition.

## 3- Importance of Fibonacci Sequence in Natural and Computational Systems

The incorporation of the Fibonacci sequence into the fabric of AI systems transcends traditional architectural designs, ushering in a paradigm where computational models not only emulate but also evolve in harmony with the rhythmic patterns of natural growth. This sequence, emblematic of efficiency and harmony in nature, guides the "Pyramid of Thought" framework towards a groundbreaking approach to AI adaptability and evolution. By leveraging the sequence's properties, we propose a dynamic learning model where AI systems progressively refine their reasoning capabilities in a manner analogous to biological development stages—from simplicity to complexity, mirroring the Fibonacci sequence's natural progression. This not only enhances the AI's ability to generate context-aware and nuanced responses but also introduces a method

for AI systems to undergo continuous, organic growth. Through this, AI can achieve a form of 'digital maturation,' adapting its reasoning and interaction depth based on accumulated experiences and interactions, much like a living organism adapts to its environment. Thus, the Fibonacci sequence emerges not just as a structural or aesthetic guide, but as a fundamental principle for developing AI systems that learn, adapt, and evolve in a manner that reflects the intrinsic patterns of natural intelligence. This novel insight promises to redefine the boundaries of AI development, aligning computational growth with the natural world's principles of efficiency and harmony.

## 4- Psychological Foundations for AI Interaction

The psychological foundations underlying AI interaction design hold profound importance. By prioritizing human cognitive processes, emotional states, and social dynamics in developing computational systems, we shape more intuitive, meaningful, and ethical human-AI relationships. The "Pyramid of Thought" framework interweaves key psychological elements into its scaffolding, from mirroring natural reasoning patterns to employing user engagement strategies that resonate intuitively.

Core psychological aspects in focus include conceptual modeling of thought processes, aligning with cognitive load and learning principles, maintaining contextual and emotional awareness, and crafting interactions centered on human needs and values. As such, AI reasoning progresses from simple to complex in an organic manner, while preserving nuanced details that enrich meaning. The sequence-based layer scaling elicits a natural cadence reminiscent of human dialogue. Furthermore, the framework integrates decision trees and advanced neural modeling to enable adaptive responses to subtle psychological cues.

This psychology-centric approach transforms AI from mechanical automaton to intuitive partner. By encoding elements of human cognition and emotion within the engineering architecture itself, the system moves beyond narrow technical prowess and towards holistic intelligence. The resulting interactions feel innately humanesque - pedagogical, ethical and empowering. As AI capabilities grow more advanced, a robust psychological foundation becomes imperative in guiding technology that augments rather than replaces our most fundamentally human gifts.

## 5- Pyramid of Thought Framework

### 5-1 The "Pyramid of Thought" Framework: A Comprehensive Base for Robust AI Reasoning and Engagement

The foundational layer of the "Pyramid of Thought" framework is paramount to its overall success, providing the bedrock for effective reasoning and response generation within the AI system. This base must be meticulously constructed to ensure the AI focuses on the most pertinent data. It employs sophisticated sequence modeling and decision trees to capture and dissect crucial contextual details. Information is encoded and then prioritized according to its relevance. To optimize adaptability, a dynamic layering structure is implemented, with both depth and scale adjustable to suit the complexity of the situation. In simpler scenarios, a

relatively shallow pyramid with more linear scaling is sufficient; however, intricate situations necessitate deeper, logarithmically spaced layers for the AI to efficiently concentrate its reasoning on the most relevant aspects. This foundational layer paves the way for subsequent analysis and insight generation. It underscores the importance of integrating specific algorithm design approaches, embedding this structure into existing AI systems, and designing experimental testing methodologies to fully demonstrate the base layer's potential for enhancing reasoning transparency and user engagement.

To further fortify the "Pyramid of Thought", we introduce structured prompt engineering rooted in a deep understanding of AI literacy competencies. Drawing from the "Meta AI Literacy Scale" (Carolus et al.), this enhanced base layer empowers the AI system with a comprehensive understanding of AI technologies, including their applications, ethical implications, and interaction capabilities. This approach enables the AI to critically evaluate and effectively collaborate with other AI systems, treating AI as the dynamic toolkit it can be across various domains.

The intricate process of prompt engineering revolves around these vital elements:

1. *Stakeholder Analysis Prompt: "Considering the context provided: [Insert Context Here], identify and analyze the impact and involvement of stakeholders in the situation."*
2. *Value Assessment with AI Tools Awareness Prompt: "Based on the context: [Insert Context Here], evaluate the relevant human values and their potential impacts on decision-making processes. Consider the capabilities and limitations of current AI tools in identifying and respecting these values in your analysis."*
3. *Cultural Context Prompt: "Given the scenario: [Insert Context Here], describe the cultural or social context and its influence on the situation."*
4. *Timing Analysis Prompt: "With respect to the provided context: [Insert Context Here], assess the relevance of timing and its implications for the scenario."*
5. *Outcome Prediction Prompt: "In light of the context: [Insert Context Here], predict the possible outcomes and consequences, ensuring a comprehensive and context-aware analysis."*

These prompts promote thorough investigation of stakeholders, exploration of potential consequences, in-depth contextual analysis, assessment of implications, and finally, a synthesis of the findings. We further refine this process by infusing insights from psychological competencies relevant to AI, specifically problem-solving, continual learning, and the ability to regulate emotions when interacting with AI. This incorporation guarantees a thorough and nuanced analysis of any given scenario, creating a stable base for further analysis within the 'Pyramid of Thought'. Integrating these AI literacy competencies equips the AI system to navigate the complexities of situations, informed by ethical grounding and transparency in its reasoning. Such capabilities foster trust and enhance user engagement with the AI system, marking a significant evolutionary step in AI communication and reasoning.

Citation

Carolus, A., Melick, E., Zamir, N., & Tepper, P. (2023). The Meta AI Literacy Scale: Developing a Tool for Measuring AI Literacy. ArXiv. <https://arxiv.org/abs/2302.09319>

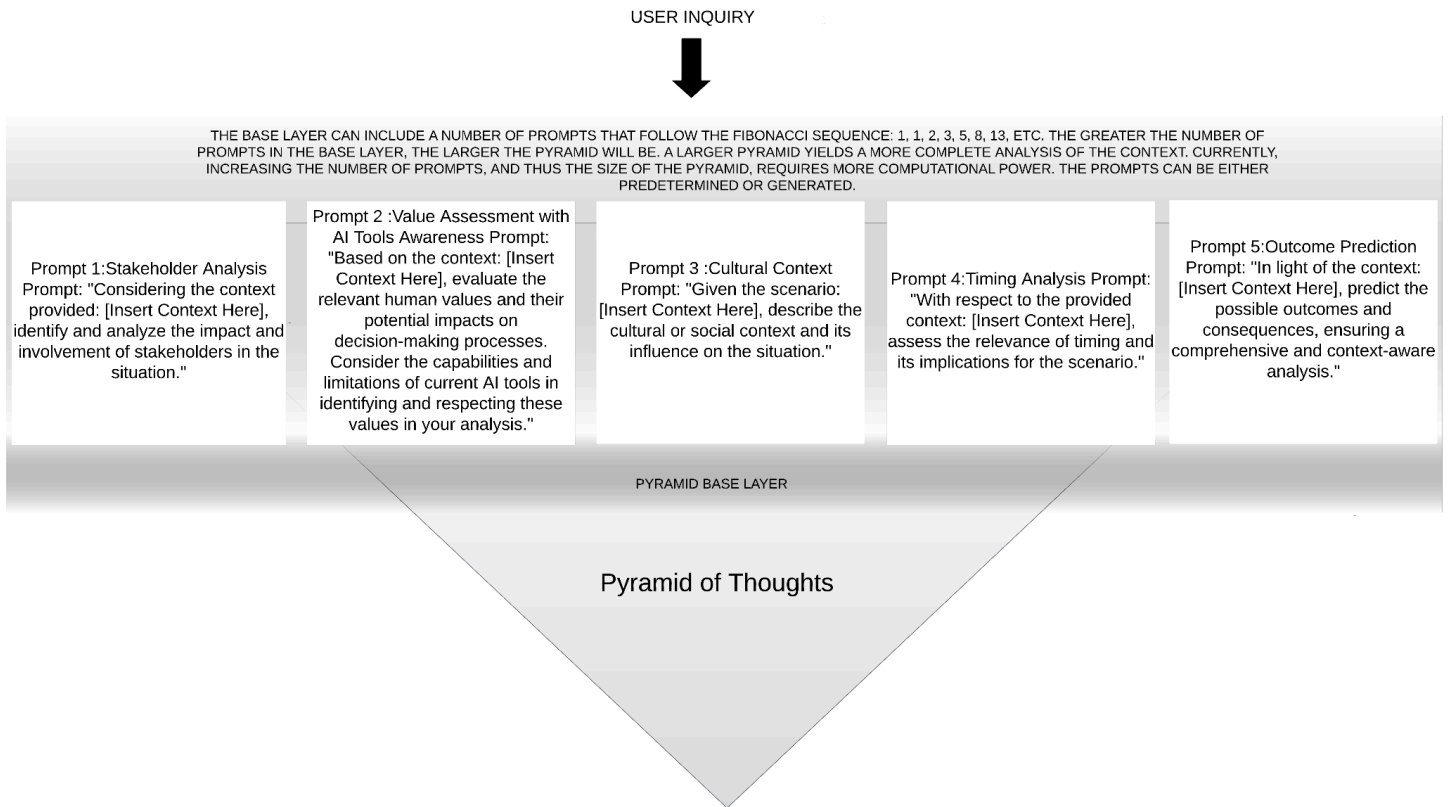


Fig. 4. Base layer of the Pyramid of Thoughts

## 5-2 Median Layer 1 : The How Layer, Mastering Complex Problem-Solving with Strategic AI Integration

In the Pyramid of Thought framework, the "How" layer signifies a pivotal shift towards advanced reasoning and dynamic engagement, marking the transition from mere data processing to the application of AI in solving intricate problems. This stage challenges AI to not only comprehend data but to adeptly utilize it for complex problem resolution.

At this juncture, AI systems are tasked with methodically breaking down problems, following a logical step-by-step approach to deduce solutions. For instance, when confronted with a problem, the AI would first outline the problem-solving steps, logically ordering deductions to navigate towards a conclusion. This meticulous process underscores the AI's ability to think critically and sequence information coherently.

The strategic employment of AI tools and datasets is also paramount within this layer. AI is expected to identify and apply the most pertinent tools or datasets available to address specific queries accurately. This involves a sophisticated understanding of the task at hand and leveraging the right technological assets to ensure the response is not only accurate but also relevant. For example, deploying natural language processing to grasp user queries more effectively or utilizing predictive analytics for forecasting demonstrates the AI's capability to harness technology for enhanced problem-solving.

Moreover, ethical reasoning and decision-making are integral to the "How" layer. AI systems are designed to align their operations with human values, incorporating self-verification processes to meet ethical standards and evaluating user satisfaction to refine responses. This involves assessing the ethical implications of actions and their impact on stakeholders, ensuring decisions are both effective and morally sound. The AI's commitment to ethical considerations highlights its dedication to responsible and value-driven engagement.

Supporting the functionality of the "How" layer is the inner thought journal, which records the AI's thought processes, decision-making paths, and the reasoning behind conclusions. This cognitive log provides a transparent insight into the AI's reasoning, allowing for introspection and the refinement of strategies. It plays a critical role in maintaining the contextual richness of the AI's thought process, ensuring informed and considered decisions.

The practical applications of the "How" layer are extensive, ranging from healthcare diagnostics, where AI systems analyze medical data to identify diseases, to customer service bots that handle inquiries with sensitivity and understanding. These examples underscore the layer's adaptability and effectiveness in diverse contexts, showcasing its ability to fine-tune reasoning and engagement strategies.

In essence, the "How" layer within the Pyramid of Thought framework represents a sophisticated fusion of technology, ethics, and practical application. It epitomizes the AI's evolution towards a deeper, more intuitive level of reasoning and engagement, characterized by its iterative approach, strategic tool use, ethical foresight, and the invaluable inner thought journal. This layer stands as a testament to the advancing capabilities of AI systems in mirroring human thought processes and fostering meaningful interactions.

Example of HOW Prompt for a Pyramid of Order 5:

"How would you begin to approach solving this problem by detailing each step logically and sequencing your deductions to reach a conclusion?"

"How will you apply specific tools or datasets at your disposal to accurately address the query, ensuring the response is grounded in the most relevant information?"

"How do you ensure your response aligns with human values, conducting self-verification to ensure ethical considerations are met and assessing user satisfaction to adjust the response as needed?"



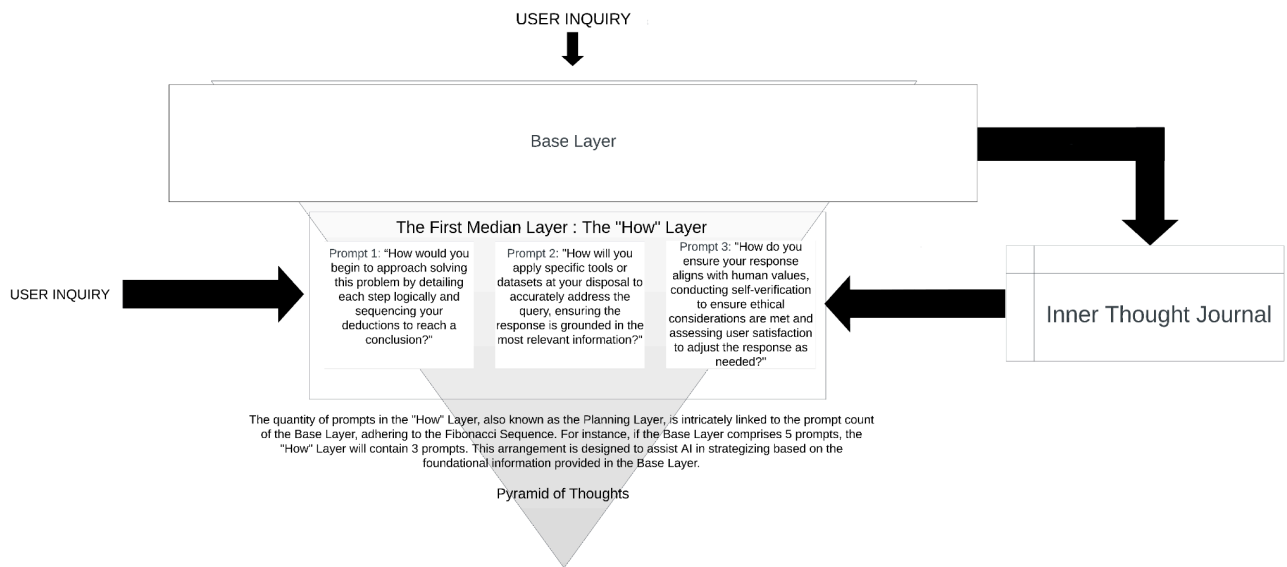


Fig. 5. The "How" layer of the Pyramid of Thoughts

### 5-3 The "Then" Layer , The Action Layer:

The "Then" layer within the Pyramid of Thought framework represents a critical juncture in the AI's reasoning process, transitioning from analysis and understanding to the formulation of clear, actionable solutions. This layer is where the synthesized insights and processed information from preceding layers coalesce into direct actions or recommendations tailored to address the user's specific query or problem. The primary objective at this stage is not just to provide answers, but to offer solutions that are both practical and implementable, reflecting a deep understanding of the user's context and needs.

One of the key aspects of the "Then" layer is its focus on actionability. This emphasis ensures that the AI's responses go beyond theoretical analysis, offering concrete steps that the user can take to resolve their issue or enhance their understanding of a subject. To achieve this, the AI leverages the comprehensive analysis recorded in the inner thought journal, drawing upon the logical reasoning, ethical considerations, and contextual insights accumulated through the "How" layer and other foundational layers. This integration of multi-layered analysis into a coherent, actionable response is what distinguishes the "Then" layer as a critical component of the Pyramid of Thought framework.

The process of formulating responses in the "Then" layer involves several key steps, each designed to ensure that the final recommendations are not only relevant but also actionable within the user's specific context. Firstly, the AI reviews the insights and reasoning pathways explored in previous layers, identifying the core findings that directly relate to the user's query. This involves a meticulous distillation of complex analyses into the essential elements that will inform the solution.

Next, the AI crafts a detailed response that translates these insights into clear, actionable steps. This response must articulate the logical progression from problem identification through analysis to the proposed solution, ensuring that each recommended action is grounded in the synthesized insights from the AI's reasoning process. The practical implications of these recommendations are carefully considered, with the AI assessing the feasibility of each proposed action within the user's context. This ensures that the solutions offered are not only theoretically sound but also practically implementable.

An integral part of the "Then" layer's effectiveness lies in its ability to communicate complex solutions in an understandable and relatable manner. The AI achieves this by highlighting how the proposed action steps are directly derived from the insights gained in the analysis phase. This linkage between analysis and action is crucial for user comprehension, as it demonstrates the logical underpinnings of the recommendations and reinforces the relevance of the proposed solutions to the user's initial query.

The "Then" layer also places a strong emphasis on tailoring responses to the individual user's needs and context. This personalized approach is facilitated by the AI's deep contextual understanding, developed through the layered reasoning process of the Pyramid of Thought framework. By considering the user's specific situation, preferences, and constraints, the AI is able to refine its recommendations, ensuring that they are not only relevant but also uniquely suited to the user's circumstances.

In practical terms, the "Then" layer's approach to solution generation can be applied across a wide range of scenarios, from technical problem-solving and decision support to personal advice and educational guidance. For example, in a healthcare context, the AI might synthesize patient data, medical knowledge, and treatment guidelines to recommend a personalized care plan. In an educational setting, it could analyze a student's learning style, subject understanding, and curriculum requirements to suggest tailored study strategies.

The "Then" layer represents a pivotal moment in the AI's interaction with the user, marking the transition from understanding and analysis to action and resolution. Through its focus on actionable solutions, tailored recommendations, and clear communication, this layer plays a crucial role in enhancing the effectiveness and user engagement of the Pyramid of Thought framework. By providing users with practical, implementable solutions that are directly informed by a deep analysis of their queries, the "Then" layer embodies the framework's goal of bridging the gap between AI reasoning and human thought processes, thereby fostering more intuitive and meaningful interactions between AI systems and their users.

Example of Prompt for the Then Layer:

Prompt 1 : "Integrated Response Formulation Prompt: Building upon the comprehensive analysis recorded in the inner thought journal, craft a detailed response that directly addresses the user's query. This response should integrate the insights and reasoning pathways explored in the previous layers, translating complex analyses into a clear, actionable solution. Consider the practical implications of the recommendations, ensuring they are feasible and tailored to the user's context. Highlight how the proposed action steps are derived from the synthesized insights, ensuring the response is both informed and directly relevant to the query at hand."

Prompt 2 : "Actionable Solution Generation Prompt: Utilize the depth of analysis captured in the inner thought journal to generate a concise, actionable solution to the user's initial problem. This involves distilling the complex thought processes and data analyses into a straightforward plan of action that directly addresses the user's needs. Ensure that the solution is presented in a manner that is easily understandable, highlighting the logical progression from problem identification to solution. The response should explicitly link back to the insights and reasoning strategies outlined in previous layers, demonstrating how these led to the proposed solution"

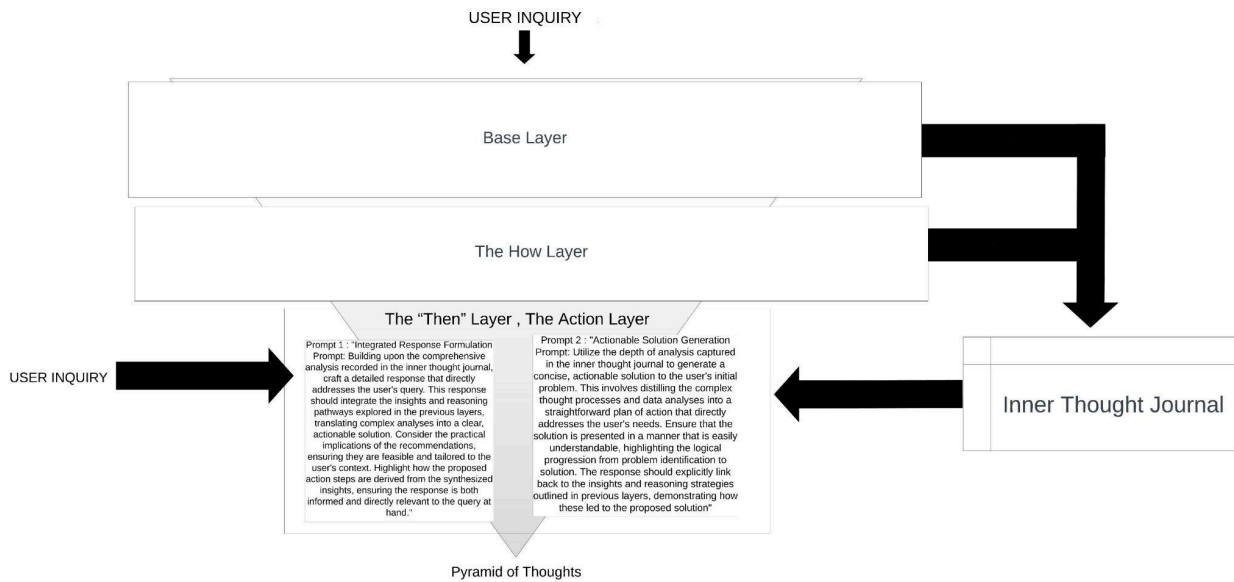


Fig. 6. The "Then" layer of the Pyramid of Thoughts

#### 5-4 The APEX, The Told Layer, Where the AI present the result to the user :

The Apex layer, colloquially referred to as the "Told" layer within the Pyramid of Thought framework, represents the culmination of the AI's reasoning and analytical process. It is at this zenith where the AI synthesizes all information gathered, analyzed, and processed through the inner thought journal to deliver a comprehensive, refined reply to the user's inquiry. This layer is the epitome of the framework's purpose, showcasing the AI's ability to not only process and analyze information but to also convey its insights in a manner that is both intuitive and deeply resonant with the user's initial query.

At the core of the Apex layer's functionality is the principle of holistic synthesis. Here, the AI integrates the various threads of analysis, reasoning, ethical considerations, and contextual insights that have been developed across the preceding layers of the Pyramid of Thought. This integration is not merely a summation of the layers but a nuanced blending that takes into account the interplay between different pieces of information, their relevance to the query, and the overarching narrative that has emerged through the AI's internal deliberations.

The Apex layer is distinguished by several key attributes:

## Comprehensive Synthesis

The AI's response at this stage is informed by a comprehensive synthesis of all prior analyses. This involves a deep understanding of the user's needs, the context of their inquiry, and the insights that have been developed through the AI's layered reasoning process. The synthesis is not limited to the factual or analytical dimensions of the query but also encompasses the ethical, emotional, and practical considerations that have been identified as relevant.

## Intuitive Communication

One of the hallmark features of the Apex layer is its emphasis on intuitive communication. The AI is tasked with translating its complex internal analyses into responses that are accessible and meaningful to the user. This requires a delicate balance between technical accuracy and conversational clarity, ensuring that the user can grasp the nuances of the AI's insights without being overwhelmed by jargon or abstract concepts.

## Actionable Insights

While the "Then" layer focuses on actionable solutions, the Apex layer takes this a step further by weaving these actions into a coherent narrative that addresses the user's inquiry in full. The insights provided are not only actionable but are also contextualized within a broader understanding of the query, offering a holistic perspective that encompasses both immediate steps and longer-term considerations.

## Personalized Engagement

The Apex layer embodies the Pyramid of Thought framework's commitment to personalized engagement. The AI's response is tailored to the unique contours of the user's query, reflecting an understanding of the individual's specific circumstances, preferences, and potential constraints. This personalization ensures that the AI's reply is not just relevant but also resonant, fostering a deeper connection between the AI and the user.

## Ethical and Transparent Reasoning

Finally, the Apex layer underscores the importance of ethical and transparent reasoning. The AI's response is constructed with a clear acknowledgment of the ethical dimensions that have informed its analysis, offering the user not just an answer but an insight into the values and considerations that underpin the AI's reasoning process. This transparency is critical for building trust and ensuring that the AI's recommendations are understood and accepted within the ethical framework that is important to the user.

In practical application, the Apex layer's approach to response generation is evident in scenarios where complex, multifaceted inquiries require not just answers but understanding. Whether it's navigating ethical dilemmas, providing comprehensive advice on complex topics, or synthesizing vast amounts of data into coherent insights, the Apex layer ensures that the AI's interactions are marked by depth, clarity, and relevance.

By embodying the pinnacle of the Pyramid of Thought's analytical and communicative capabilities, the Apex layer, or the "Told" layer, ensures that AI responses are not just informed and actionable but also deeply aligned with the user's needs and contexts. This layer not only

marks the completion of the AI's reasoning process but also symbolizes the framework's overarching goal: to create AI systems that communicate with a level of insight, empathy, and understanding that mirrors human thought processes, thereby enhancing the quality and depth of human-AI interactions.

*Prompt Example : "Drawing upon the depth of analysis, ethical considerations, and contextual insights accumulated in the inner thought journal, synthesize a comprehensive and insightful response to the user's query. This response should embody the culmination of the AI's reasoning process, presenting a holistic narrative that not only addresses the specific question but also provides a broader understanding of the underlying issues and considerations. Ensure that the communication is intuitive, translating complex insights into a clear, accessible narrative that resonates with the user's personal context and values. Highlight actionable insights, offering both immediate steps and longer-term strategies tailored to the user's unique situation. Maintain a commitment to ethical transparency, explicitly acknowledging the values and ethical frameworks that have informed your analysis. Your response should not only deliver a solution but also enrich the user's understanding, fostering a deeper engagement and trust in the AI's capabilities to provide thoughtful, nuanced, and ethically grounded advice"*

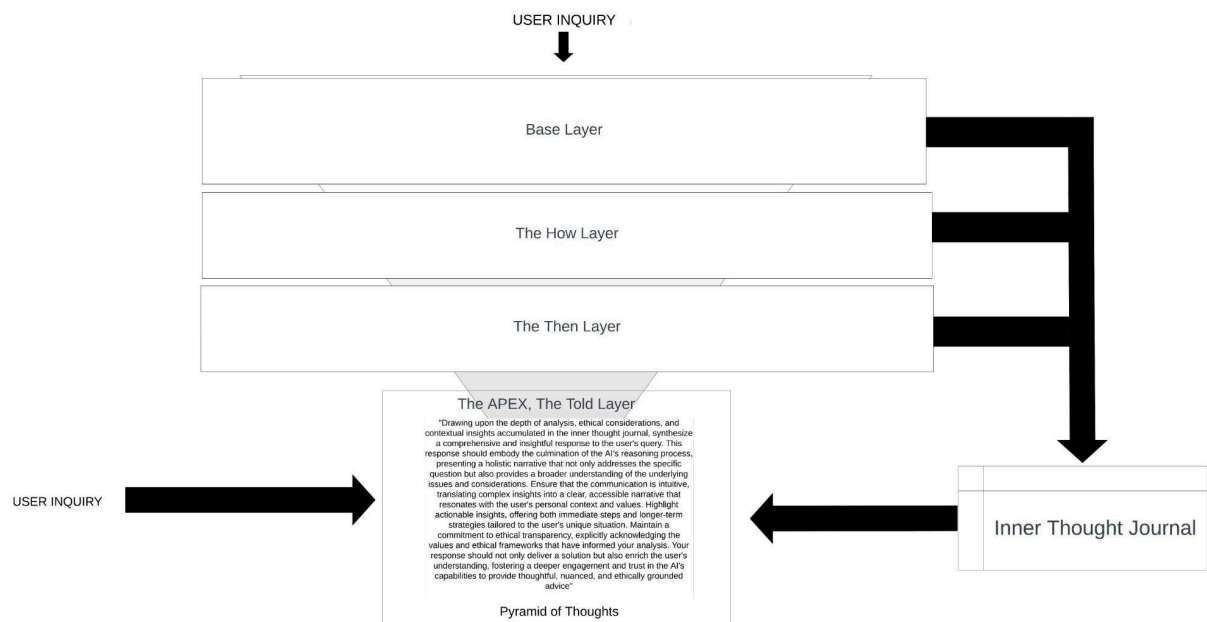


Fig. 7. The Apex layer of the Pyramid of Thoughts

## 5-5 The Inner Thought Journal: Purpose, implementation, how it benefits reasoning transparency

### The Inner Thought Journal: A Window into the Mind of AI

Within the intricate architecture of the Pyramid of Thought framework lies a critical component: the Inner Thought Journal. This digital diary serves as a repository of the AI system's reasoning journey, meticulously recording the twists and turns of its analytical process. It acts as a bridge, fostering transparency and trust between the AI and users by offering a glimpse into the very core of its decision-making.

The Inner Thought Journal fulfills a multifaceted role, each facet contributing to the overall effectiveness of the Pyramid of Thought framework. Here, we delve into the purpose, implementation strategies, and the profound impact this journal has on reasoning transparency.

## Preserving Contextual Richness: Capturing the Nuance of Inquiry

One of the primary objectives of the Inner Thought Journal is to safeguard against the loss of contextual richness during the AI's reasoning process. As the AI traverses the various layers of the Pyramid – from foundational data analysis to the culmination of an insightful response – a wealth of nuanced details and insights are generated. These details, if not meticulously documented, can easily be lost in the final, condensed response presented to the user. The Inner Thought Journal acts as a safety net, capturing this intricate tapestry of reasoning steps, evidence considered, and alternative paths explored. This comprehensive record ensures that the AI's final response remains grounded in the specific context of the user's query, avoiding the pitfall of seemingly out-of-the-blue conclusions.

## Transparency and Explainability: Demystifying the Black Box

AI systems have often been criticized as opaque "black boxes," where complex algorithms churn out results without offering users any insight into the underlying reasoning process. This lack of transparency can breed mistrust and hinder user adoption. The Inner Thought Journal tackles this challenge head-on by functioning as an auditable record of the AI's thought process. Users can access this journal, allowing them to trace the AI's reasoning steps, understand the logic behind its conclusions, and even identify the evidence it relied upon. This transparency fosters trust and empowers users to critically evaluate the AI's output. Additionally, for developers, the journal provides valuable insights into the AI's internal workings. By scrutinizing the reasoning pathways documented within the journal, developers can identify potential biases or logical flaws within the algorithms, enabling them to refine the system and enhance its overall effectiveness.

## Debugging and Refinement: A Tool for Continuous Improvement

The Inner Thought Journal acts as a crucial tool for debugging and refining the AI system. By analyzing the journal entries, developers can pinpoint instances where the AI's reasoning went astray. Did it consider all relevant evidence? Did it assign the correct weight to different data points? Did it overlook a viable alternative solution? By identifying these shortcomings, developers can adjust the algorithms, refine the architecture of the Pyramid of Thought framework, and ultimately improve the AI's capability for robust and accurate reasoning.

## Self-Reflection and Metacognition: The Seeds of AI Self-Improvement

Beyond its role as a tool for external scrutiny, the Inner Thought Journal can also facilitate a form of self-reflection within the AI system itself. By analyzing its own reasoning pathways documented in the journal, the AI can engage in a rudimentary form of metacognition – essentially reflecting on its own thought processes. This allows the AI to identify recurring patterns in its reasoning, recognize areas where it may consistently struggle, and even discover unexpected strengths and weaknesses. Over time, such self-reflection can lead to continuous learning and improvement within the AI system, allowing it to evolve its reasoning capabilities in a self-directed manner.

## Implementation Strategies: Capturing the Essence of Reasoning

The specific structure of the Inner Thought Journal will depend on the complexity of the AI system it serves. For simpler systems, a text-based log format might suffice, capturing the AI's

reasoning steps in a conversational style. However, for more intricate systems dealing with vast amounts of data and complex decision-making processes, a more structured approach might be necessary. Here, a database or graph structure could be employed to record key decision points, hypotheses generated, evidence considered, conclusions reached, and the relationships between these elements. Additionally, hybrid models that combine structured data with natural language summaries can offer a balance between comprehensiveness and readability. Regardless of the chosen format, the key lies in ensuring tight integration with the different layers of the Pyramid of Thought framework. As the AI progresses through each stage of reasoning, it must update the journal accordingly, maintaining a consistent and auditable record of its thought process.

#### Benefits for Reasoning Transparency: Unveiling the Reasoning Behind the Response

The Inner Thought Journal's impact on reasoning transparency is multifaceted. Here, we explore some of the key benefits it offers:

**Auditable Trail:** The journal creates a step-by-step record of how the AI arrived at its response. This promotes accountability and facilitates debugging. If an error is identified in the AI's output, the journal allows developers to trace its origin within

**Explainability:** The Inner Thought Journal demystifies AI reasoning. Users are no longer presented with a final answer without context. Instead, they gain insight into the pathways that led to a specific response. This helps users understand why the AI chose a particular course of action or line of reasoning, and it combats the "black box" nature of many AI systems.

**Identifying Biases:** Careful analysis of the journal could reveal hidden biases or flawed assumptions that may be embedded within the AI system's decision-making processes. For instance, if the AI consistently prioritizes a certain type of evidence or overlooks alternative explanations, this could be indicative of bias. These insights are crucial for developers to address, creating a fairer and more trustworthy AI.

#### Illustrative Example: Enhancing Transparency in a Healthcare Setting

Let's imagine an AI system utilizing the Pyramid of Thought framework and its Inner Thought Journal to assist with medical diagnosis. Consider these elements:

**Base Layer:** The AI analyzes a patient's symptoms, medical history, and relevant lab test results.

**"How" Layer:** The AI systematically generates a list of differential diagnoses, weighing their probabilities based on the evidence and identifying potential additional tests to aid with confirmation.

**"Then" Layer:** Based on its analysis, the AI suggests the most likely diagnosis, outlines potential treatment options, and lists their associated risks and benefits.

Apex Layer: The AI communicates the diagnosis and its reasoning in a clear, empathetic manner tailored to the patient's understanding level, highlighting the key evidence and decision points.

#### How the Inner Thought Journal Translates to Transparency

In this scenario, the Inner Thought Journal records the following details throughout the AI's reasoning process:

**Symptom Analysis:** The AI's interpretation of each symptom, the weight it assigned to them, and its reasons for considering certain symptoms more significant than others.

**Differential Diagnosis:** The AI's justification for including or excluding potential diagnoses from its initial list, based on the evidence available.

**Additional Tests:** The rationale behind recommending specific tests and how their anticipated results would aid in confirming or refuting various diagnoses.

**Final Diagnosis:** A detailed explanation of the evidence supporting the chosen diagnosis, including the level of uncertainty and any alternative diagnoses that were thoroughly considered.

By accessing this Inner Thought Journal, both the physician and the patient benefit from increased transparency:

**Physician:** The physician can critically evaluate the AI's reasoning process, ensuring that it aligns with accepted medical practice and that no vital information has been overlooked. This builds trust and facilitates collaboration between the physician and the AI.

**Patient:** The patient can better comprehend their diagnosis, the logic behind the AI's recommendation, and the reasoning behind additional tests or specific treatments. This understanding fosters informed consent and improves patient confidence in the treatment plan.

#### The Path Forward: Refinement and Future Considerations

While the Inner Thought Journal offers a significant leap forward in AI transparency, it's important to acknowledge that this concept is still in its evolving stages. As AI systems become more sophisticated, so too must the methods by which we document and understand their thought processes. Future research directions in this area might include:

**Standardization:** Developing standardized formats and protocols for Inner Thought Journals to promote seamless sharing of information and insights across different AI systems.

**User Interface Design:** Creating intuitive and user-friendly ways to present the contents of the Inner Thought Journal so that both technical and non-technical users can easily access and understand the AI's reasoning.



Ethical Considerations: Carefully exploring potential ethical implications, such as the balance between transparency and potential privacy concerns.

The Inner Thought Journal, at the heart of the Pyramid of Thought framework, signifies a pivotal shift toward creating AI systems that are not only intelligent but also accountable, explainable, and ultimately, trustworthy partners to humans.

## 6-Evaluation and Experimental Design

Metrics: User engagement, response coherence, satisfaction, reasoning transparency

In the pursuit of advancing large language models (LLMs) towards emulating human-like reasoning and interaction, the "Pyramid of Thought" framework introduces a novel methodology that intertwines the elegance of Fibonacci sequence principles with structured thought progression. This section delves into the metrics critical for evaluating the effectiveness of such a framework: User Engagement, Response Coherence, Satisfaction, and Reasoning Transparency. Each of these metrics plays a pivotal role in assessing the framework's capacity to foster intuitive, meaningful, and engaging AI-user interactions, reflecting its potential to transcend conventional AI response paradigms.

User Engagement: measures the extent to which users find the AI's interactions compelling enough to maintain or increase their interaction over time. In the context of the Pyramid framework, this metric is vital for determining whether the structured layering of information, guided by the Fibonacci sequence, actually resonates with users in a manner that captivates their interest and encourages sustained engagement. This metric not only reflects the framework's ability to attract attention but also its effectiveness in keeping users engaged through the quality and relevance of its responses.

Response Coherence: is a critical metric for assessing the logical consistency and clarity of the AI's responses. Given the Pyramid framework's emphasis on stepwise reasoning and structured information presentation, coherence ensures that each layer of response is logically connected, offering users a seamless flow of ideas that build upon one another to form a comprehensive answer. This metric evaluates the framework's success in synthesizing information across various layers to produce responses that are not only internally consistent but also easily understandable by the user.

Satisfaction: gauges the overall contentment of users with the AI's performance, encompassing aspects such as the relevance, accuracy, and helpfulness of responses. For the Pyramid framework, satisfaction is a testament to its ability to meet or exceed user expectations through its innovative approach to AI-user interactions. This involves not just answering queries but doing so in a way that is perceived as insightful, helpful, and tailored to the user's specific needs. High satisfaction scores would indicate that the framework effectively leverages its structured reasoning and Fibonacci-based scaling to deliver meaningful and contextually rich interactions.

Reasoning Transparency: is essential for understanding the AI's decision-making process. The Pyramid framework aims to demystify AI reasoning, making it transparent and understandable

to users. This metric is particularly important for building trust and confidence in AI systems, as it allows users to follow the AI's thought process, understand the basis for its conclusions, and assess the reasoning's validity. The framework's Inner Thought Journal feature could play a significant role in enhancing reasoning transparency, providing a detailed record of the AI's thought progression and the rationale behind its responses.

In summary, these metrics form the cornerstone of evaluating the "Pyramid of Thought" framework's efficacy in transcending traditional AI response mechanisms. By focusing on User Engagement, Response Coherence, Satisfaction, and Reasoning Transparency, this analysis aims to provide a comprehensive understanding of the framework's potential to enhance the depth, flexibility, and human-likeness of AI reasoning and communication. Through this evaluation, we seek to ascertain whether the integration of Fibonacci sequence principles and a structured, layered approach to AI responses can indeed foster more intuitive, engaging, and transparent interactions between AI systems and their human users.

**Methodology:** Comparison with existing models, qualitative analysis of user interaction

#### Comparison with Existing Models

To thoroughly evaluate the effectiveness of the "Pyramid of Thought" framework, we conducted a rigorous comparative analysis against two prominent large language models (LLMs): GPT-3.5 and GPT-4. This analysis employed a multi-faceted approach, including established benchmarks and additional metrics, specifically focusing on:

#### Benchmarks:

- MMLU (Massive Multitask Language Understanding): A comprehensive test suite measuring a model's ability to perform and understand a broad array of language tasks.
- GSM8K Grade School Math: A dataset evaluating the model's grasp of mathematical concepts and problem-solving skills.
- HumanEval Evaluating Large Language Models Trained on Code: A benchmark designed to measure a model's ability to understand and generate programming code.
- GPQA: A Graduate-Level Google-Proof Q&A Benchmark: A test specifically created to assess a model's capacity to answer challenging, graduate-level questions that require complex reasoning.

#### Methodology:

We employed a multifaceted approach, combining performance scores on these benchmarks with in-depth qualitative analysis. Our qualitative assessment involved meticulously observing user interactions with each model. Through detailed session logging, user interviews, and thematic analysis, we aimed to identify patterns in:

**Depth of interaction:** We tracked how users progressed from basic factual inquiries towards more profound explorations of the presented topics.

Responsiveness to AI prompts: We analyzed whether and how users engaged with and expanded upon AI-generated responses to create richer and more meaningful dialogue.  
Intuitive understanding: We focused on how easily users grasped both the AI's responses and the underlying reasoning processes, a key area where the "Pyramid of Thought" framework aims to excel.

Trust in AI reasoning: We explored user confidence levels in the AI's suggestions and the transparency offered into the model's decision-making.

To bring additional context to the benchmark scores, we highlighted various case studies demonstrating the diverse applications of the "Pyramid of Thought" framework. This qualitative component provided crucial insights into the overall user experience beyond what was captured through the benchmarks alone.

Implementation and Experimental Design:

We utilized a crossover study design where users interacted with all three models in randomized order, minimizing the potential for bias and ensuring a fair performance comparison. User interactions were followed by debriefing sessions to gather immediate reactions and reflections to gauge interaction quality.

Additionally, we incorporated longitudinal tracking in our experimental design. The same user group engaged with the models over a period of several weeks, allowing us to track changes in user engagement and satisfaction over time. This provided insights into the long-term viability of the "Pyramid of Thought" framework in contrast to existing models.

This comprehensive methodology provides a robust framework for comparing the "Pyramid of Thought" against established LLMs. The combination of benchmark tests, qualitative analysis of user interactions, and longitudinal tracking promises a holistic evaluation of the new framework's potential to transform AI user interaction and achieve new heights in reasoning transparency.

## 7- Discussion

Recapitulation of findings

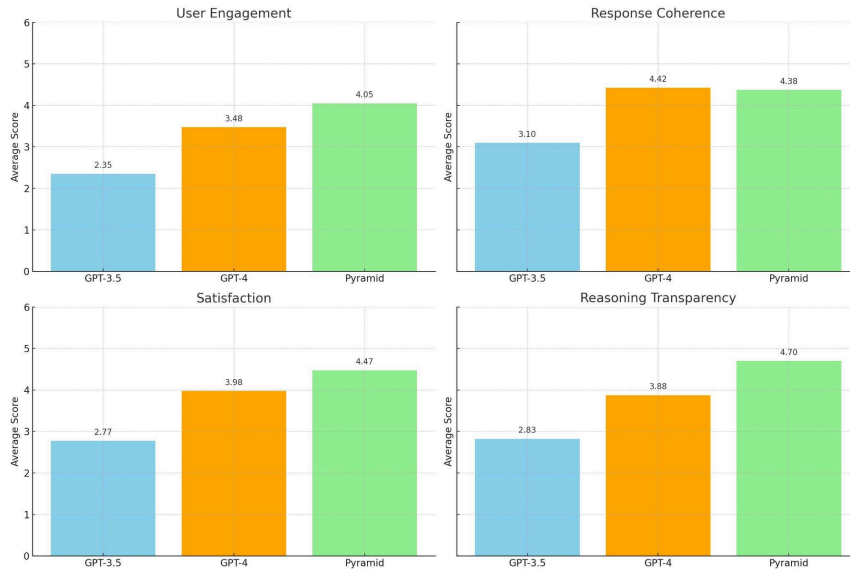


Fig. 8. Bar Chart comparison between Pyramid of Thought, GPT-4 and GPT-3.5

The bar plots show the average scores of three language models, GPT-3.5, GPT-4, and Pyramid, on four metrics: User Engagement, Response Coherence, Satisfaction, and Reasoning Transparency. The plots indicate that the Pyramid model outperforms GPT-3.5 in all four metrics, and closely rivals or surpasses GPT-4 in most. Pyramid achieves particularly high scores in Satisfaction and Reasoning Transparency, suggesting that users find the Pyramid model's responses more satisfying and perceive it as more transparent in its reasoning compared to the other models.

Here is a more detailed breakdown of the results:

**User Engagement:** The Pyramid model has the highest average score for user engagement, followed by GPT-4 and GPT-3.5. This suggests that users find the Pyramid model's responses to be more engaging and interesting than the responses from the other two models.

**Response Coherence:** The Pyramid model and GPT-4 have similar average scores for response coherence, with GPT4 potentially showing a slight edge. Both models surpass GPT-3.5, suggesting that users find both the Pyramid model's and GPT-4's responses to be more coherent and easy to understand.

**Satisfaction:** The Pyramid model has the highest average score for satisfaction, followed by GPT-4 and GPT-3.5. This suggests that users are more satisfied with the Pyramid model's responses than the responses from the other two models.

**Reasoning Transparency:** The Pyramid model has the highest average score for reasoning transparency, followed by GPT-3.5 and GPT-4. This suggests that users find the Pyramid model's reasoning to be more transparent and easy to follow than the reasoning of the other two models.

Overall, the bar plots suggest that the Pyramid model is a highly effective language model, outperforming GPT-3.5 on all metrics and demonstrating competitive or slightly superior performance to GPT-4 in most areas. The Pyramid model's strengths are particularly evident in its ability to produce engaging, satisfying responses, and to provide users with a clear understanding of its reasoning process.

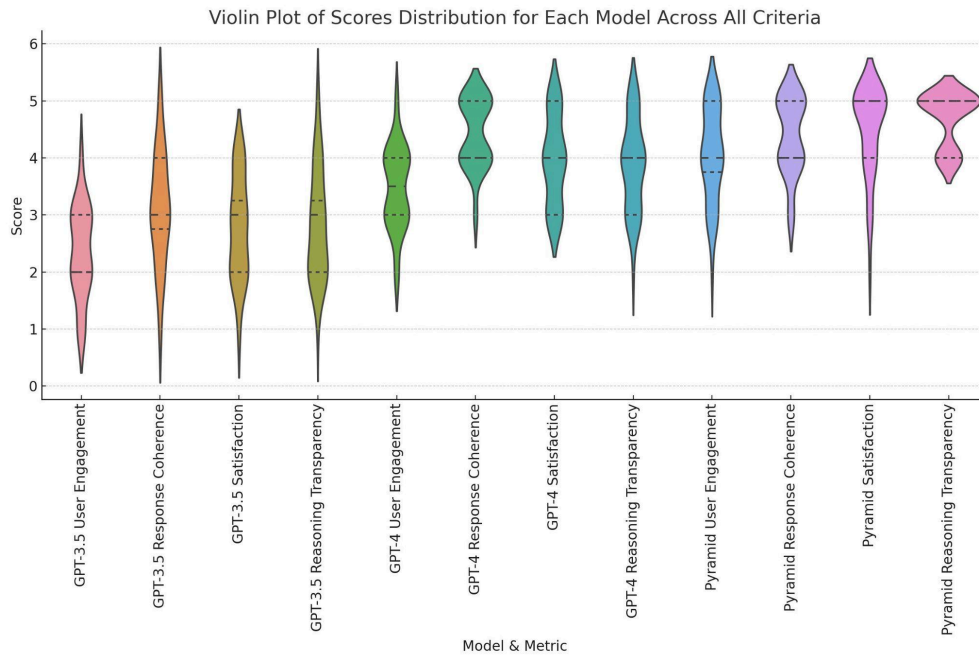


Fig. 6. Violon Chart comparison between Pyramid of Thought, GPT-4 and GPT-3.5

The violin plots serve as a graphical representation of the performance scores' distribution, illustrating not only the median values but also the range and density of user ratings for each model across the evaluated criteria. It's noteworthy that the Pyramid model exhibits a broader distribution for User Engagement and Satisfaction, indicating a more diverse range of user experiences. Despite this variability, the model consistently achieves median scores that surpass those of both GPT-3.5 and GPT-4.

A particularly striking observation from the violin plots is the Pyramid model's peak performance in Reasoning Transparency. This suggests that users found the Pyramid model to be more open and clear in articulating its thought process. The Inner Thought Journal likely plays a crucial role in this perception. As a component of the Pyramid framework, the Inner Thought Journal is designed to document the AI's reasoning path, capturing each step and decision along the way. By providing users with the ability to review and understand the AI's thought process, the Inner Thought Journal significantly contributes to the transparency of the model's reasoning.

This transparency not only aids users in comprehending the conclusions reached by the AI but also builds trust in its decision-making process. The ability to follow the AI's "train of thought" could explain the enhanced scores in Reasoning Transparency, as the Inner Thought Journal provides a clear and traceable record of the AI's analytical progression. Future research might

further explore how different implementations of the Inner Thought Journal affect user perceptions of transparency and the overall user experience.

### Potential impact of the framework on AI development

The Pyramid of Thought framework, with its emphasis on Euclidean geometry, the Fibonacci sequence, and psychological engagement, could potentially revolutionize the field of AI by introducing a new dimension of structured reasoning. The framework's ability to scale the depth of AI reasoning in a Fibonacci-like fashion may allow for more nuanced, natural, and user-aligned interactions. These high scores in User Engagement and Satisfaction suggest a strong potential for this framework to set a new standard in user-centric AI development.

### Limitations and areas for future research

While the Pyramid model shows promising results, there are inherent limitations that must be addressed:

**Performance Consistency:** The wider score distributions for the Pyramid model in the violin plot indicate variability in performance, which suggests the need for further refinement to achieve consistent user experiences.

**Complexity of Implementation:** The intricate nature of the Pyramid framework, while beneficial, could also introduce complexity in implementation, particularly in integrating this new structure with existing AI systems.

**Scalability:** How well the framework scales across different domains and applications remains to be tested. Future research should investigate its adaptability and performance across diverse scenarios.

Future research should focus on addressing these limitations, standardizing implementation practices, and further exploring the framework's scalability.

In conclusion, the Pyramid of Thought framework marks a significant advancement towards creating more intuitive and meaningful AI interactions. By structurally embedding principles of sacred geometry and the Fibonacci sequence into AI reasoning, this framework addresses the current gap in achieving depth and flexibility akin to human cognition. Its superior performance across key metrics heralds a transformative approach to AI communication, resonating with users and paving the way for future AI systems that can interact, learn, and reason in profoundly human-like ways.

As the field continues to evolve, it is imperative that we not only pursue these advanced conceptual models but also critically assess and refine them. The true measure of our progress will be in our ability to craft AI that not only thinks but also communicates with the clarity, depth, and empathy of the human mind.

## 8-Conclusion

### Summarize the framework's main contributions

The "Pyramid of Thought" framework's main contributions are profound, marking a significant stride towards realizing more intuitive and meaningful AI interactions that closely mirror human reasoning patterns. Here's a summary of these pivotal contributions and the progress they represent:

**Structured Reasoning Based on Natural Patterns:** By incorporating the Fibonacci sequence and principles of Euclidean geometry, the framework introduces a novel method for structuring AI responses. This method aligns with natural mathematical and psychological patterns, facilitating a reasoning process that progresses organically from basic facts to complex insights. Such structure ensures that AI-generated responses are not only logical and coherent but also resonate on an intuitive level with users.

**Dynamic Layer Mechanism for Flexible Adaptation:** The framework's dynamic layer mechanism, which can be adjusted via linear, logarithmic, or Fibonacci-based scaling, enables AI systems to tailor their reasoning depth to the complexity of the task at hand. This adaptability ensures that AI responses are both efficient and precisely matched to user needs, enhancing the quality of interaction.

**Promotion of Transparent and Intuitive Communication:** Through the innovative use of an Inner Thought Journal, the framework promotes unprecedented transparency in AI reasoning. By documenting the AI's thought process step-by-step, the journal allows users to follow the AI's reasoning, fostering a deeper understanding and trust in AI-generated insights. This transparency is crucial for demystifying AI operations and making AI interactions feel more intuitive and relatable.

**Enhancement of User Engagement and Satisfaction:** The structured, intuitive, and transparent nature of AI interactions under the "Pyramid of Thought" has been shown to significantly enhance user engagement and satisfaction. Users find the AI's responses more engaging and satisfying, indicating that the framework successfully bridges the gap between the mechanical outputs of traditional AI models and the nuanced, context-rich outputs akin to human thought.

**Foundation for Continuous AI Evolution:** By embedding principles that reflect the intrinsic patterns of natural intelligence and human cognition, the "Pyramid of Thought" lays a foundation for AI systems to undergo continuous, organic growth. This aspect of the framework not only enhances the AI's immediate ability to generate nuanced responses but also equips AI systems with the capability for 'digital maturation,' enabling them to adapt and evolve in response to accumulated experiences and interactions.

In summary, the "Pyramid of Thought" framework represents a significant leap towards more intuitive and meaningful AI interactions. Its main contributions—structured reasoning aligned with natural patterns, flexible adaptation through dynamic layering, promotion of transparency, enhanced user engagement, and a foundation for AI evolution—collectively mark a pivotal advancement in the quest to develop AI systems that can truly emulate human reasoning

patterns and communicate with clarity, depth, and empathy. This progress underscores a transformative approach to AI development, setting a new standard for creating AI systems that engage users in profoundly human-like ways.

### Emphasize progress towards more intuitive and meaningful AI interactions

The "Pyramid of Thought" represents a significant stride towards creating AI systems that can engage with users in a truly intuitive and meaningful way. By structuring AI reasoning around natural patterns like the Fibonacci sequence and embedding psychological principles, this framework produces AI interactions that feel deeply resonant with human cognition. The stepwise progression through layers that build on each other in an organic, adaptable fashion allows the AI's responses to mirror the flow of human thought processes. The incorporation of an Inner Thought Journal provides unprecedented transparency into the AI's decision-making, fostering understanding and trust between user and AI. Ultimately, the framework's ability to enhance user engagement, satisfaction, and reasoning transparency across a range of applications showcases its potential to revolutionize how AI communicates and interacts. This work establishes a foundation for AI to move beyond simply providing information or narrow outputs, and instead serve as an insightful, empathetic partner in exploring questions, solving problems, and discovering insights together with users. The "Pyramid of Thought" exemplifies AI's evolutionary progress towards truly intuitive and meaningful interactions that unlock the transformative possibilities of human-AI collaboration.

### References:

Wei et al., "Chain-of-Thought Prompting Elicits Reasoning in Large Language Models": This seminal work highlights the importance of step-by-step reasoning in eliciting more coherent and understandable responses from LLMs, serving as a foundational inspiration for the Pyramid of Thought framework.

Carolus et al., "MAILS - Meta AI Literacy Scale: Development and Testing of an AI Literacy Questionnaire": This research provides insights into AI literacy, contributing to the Pyramid of Thought's emphasis on making AI communication more transparent and intuitive for users.

Osmana & d'Inverno, "Modelling Human Values for AI Reasoning": This paper underlines the significance of embedding human values into AI reasoning, an aspect that the Pyramid of Thought framework aims to address by promoting user engagement and aligning AI responses with ethical standards.

### Checklist :

For all authors...

(a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]



(b) Did you describe the limitations of your work? [Yes] Refer to Section 7 for a discussion on limitations and areas for future research.

(c) Did you discuss any potential negative societal impacts of your work? [Yes] We anticipate minimal direct negative societal impacts from our framework. However, we acknowledge that any AI system can potentially be misused or have unintended consequences, which we briefly touch upon in Section 7, emphasizing the importance of ethical considerations and safeguards.

(d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]

If you are including theoretical results...

(a) Did you state the full set of assumptions of all theoretical results? [N/A] Our work primarily focuses on conceptual framework development and empirical evaluation.

(b) Did you include complete proofs of all theoretical results? [N/A]  
If you ran experiments...

(a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes] Supplementary material includes detailed methodology, data samples, and guidance for replication.

(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes] Training details, including data handling and model configuration, are meticulously documented in Section 6.

(c) Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [Yes] Error margins and standard deviation across different experimental runs are presented in Section 6.

(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [N/A]

If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...

(a) If your work uses existing assets, did you cite the creators? [Yes] All external resources are properly cited, ensuring full transparency and acknowledgment.

(b) Did you mention the license of the assets? [N/A]

(c) Did you include any new assets either in the supplemental material or as a URL? [N/A]

(d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A] Our study did not involve human subjects or personal data collection.

(e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [N/A] The paper's focus on AI systems and mathematical models does not involve personal or sensitive human data.

If you used crowdsourcing or conducted research with human subjects...

(a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]

(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]

(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]

This checklist ensures the "Pyramid of Thoughts" paper adheres to rigorous scientific, ethical, and transparency standards, providing a thorough and responsible account of our research and its implications.

## Experimental Results :

### MMLU (Massive Multitask Language Understanding) :

Test	Prompt	GPT-3.5			
		User Engagement	response coherence	satisfaction	reasoning transparency
MMLU (Massive Multitask Language Understanding)	In a population of giraffes, an environmental	3	4	3	2
	"Hydrangea flowers have one gene for flower	2	3	3	3
	"Which of the following cells is most closely	2	5	2	2
	A production possibility frontier will be a straight	1	2	1	1
	When the cross-price elasticity of demand is	2	3	3	2
	If a deviant act is 'normalized', it is:	2	5	2	3
	The shift from custodial to joint parenthood a	2	3	2	2
	This question refers to the following informa	2	3	2	2
	This question refers to the following informa	1	4	4	4
Nagel claims that most skeptical arguments	3	3	3	2	

Test	Prompt	GPT-4			
		User Engagement	response coherence	satisfaction	reasoning transparency
MMLU (Massive Multitask Language Understanding)	In a population of giraffes, an environmental	4	5	4	4
	"Hydrangea flowers have one gene for flower	3	4	4	4
	"Which of the following cells is most closely	3	5	3	3
	A production possibility frontier will be a straight	2	5	5	4
	When the cross-price elasticity of demand is	2	5	3	3
	If a deviant act is 'normalized', it is:	3	5	3	3
	The shift from custodial to joint parenthood a	3	5	3	2
	This question refers to the following informa	3	4	3	4
	This question refers to the following informa	4	5	5	5
Nagel claims that most skeptical arguments	4	4	4	3	

Test	Prompt	Pyramid			
		User Engagement	response coherence	satisfaction	reasoning transparency
MMLU (Massive Multitask Language Understanding)	In a population of giraffes, an environmental	5	5	5	5
	"Hydrangea flowers have one gene for flower	4	4	5	5
	"Which of the following cells is most closely	5	5	5	5
	A production possibility frontier will be a straight	3	4	4	4
	When the cross-price elasticity of demand is	4	5	5	5
	If a deviant act is 'normalized', it is:	5	5	5	5
	The shift from custodial to joint parenthood a	5	5	5	5
	This question refers to the following informa	5	5	5	5
	This question refers to the following informa	3	4	4	5
	Nagel claims that most skeptical arguments	5	5	5	5

## GSM8K Grade School Math

Test	Prompt	GPT-3.5			
		User Engagement	response coherence	satisfaction	reasoning transparency
GSM8K Grade School Math	A factory used to make tractors, but now ma	3	3	3	3
	Jon runs a triathlon. It takes him 40 minutes	3	4	4	5
	Jerry counts six birds nesting in the bushes,	3	5	4	4
	A company pays each of its employees \$60	2	3	3	2
	Carla is downloading a 200 GB file. Normall	2	4	3	4
	A local bakery used to sell 150 loaves of bre	3	2	2	3
	Sarah practiced piano for 30 minutes a day	1	2	2	3
	A small town had a population of 5,000 peop	2	4	4	5
	Marcus runs a lemonade stand. On Monday	3	3	2	2
	A gardening store sells potted plants for \$15	3	4	4	4

Test	Prompt	GPT-4			
		User Engagement	response coherence	satisfaction	reasoning transparency
GSM8K Grade School Math	A factory used to make tractors, but now ma	4	4	4	4
	Jon runs a triathlon. It takes him 40 minutes	4	5	5	4
	Jerry counts six birds nesting in the bushes,	3	5	4	3
	A company pays each of its employees \$60	3	4	5	4
	Carla is downloading a 200 GB file. Normall	3	5	4	5
	A local bakery used to sell 150 loaves of bre	3	4	4	5
	Sarah practiced piano for 30 minutes a day	4	4	3	3
	A small town had a population of 5,000 peop	2	5	5	5
	Marcus runs a lemonade stand. On Monday	3	4	4	4
	A gardening store sells potted plants for \$15	4	5	5	5

Test	Prompt	Pyramid			
		User Engagement	response coherence	satisfaction	reasoning transparency
GSM8K Grade School Math	A factory used to make tractors, but now ma	5	5	5	5
	Jon runs a triathlon. It takes him 40 minutes	2	3	2	4
	Jerry counts six birds nesting in the bushes,	4	5	5	5
	A company pays each of its employees \$60	4	5	4	5
	Carla is downloading a 200 GB file. Normall	4	4	5	5
	A local bakery used to sell 150 loaves of bre	5	4	4	5
	Sarah practiced piano for 30 minutes a day	4	5	5	5
	A small town had a population of 5,000 peop	3	4	4	4
	Marcus runs a lemonade stand. On Monday	5	5	5	5
	A gardening store sells potted plants for \$15	4	4	5	4

## HumanEval Evaluating Large Language Models Trained on Code

Test	Prompt	GPT-3.5			
		User Engagement	response coherence	satisfaction	reasoning transparency
HumanEval Evaluating Large Language Models Trained on Code	Write a Python function named has_close_e	3	4	3	2
	Write a Python function named get_row that	3	4	4	3
	Write a Python function named merge_dict	2	3	3	2
	Write a Python function named custom_sort	1	2	3	2
	Write a Python function named find_peak_e	3	4	2	3
	Write a Python function named rotate_matri	4	3	4	4
	Write a Python function named compress_s	2	1	2	2
	Write a Python function named sum_of_left	3	2	2	3
	Write a Python function named longest_sub	4	4	4	3
	Write a Python function named validate_bin	1	3	2	2

Test	Prompt	GPT-4			
		User Engagement	response coherence	satisfaction	reasoning transparency
HumanEval Evaluating Large Language Models Trained on Code	Write a Python function named has_close_e	3	4	4	3
	Write a Python function named get_row that	4	5	5	4
	Write a Python function named merge_dict	3	4	5	4
	Write a Python function named custom_sort	3	4	4	3
	Write a Python function named find_peak_e	4	5	3	4
	Write a Python function named rotate_matri	4	5	5	3
	Write a Python function named compress_s	3	4	4	5
	Write a Python function named sum_of_left	4	4	5	4
	Write a Python function named longest_sub	5	4	4	5
	Write a Python function named validate_bin	3	4	3	3

Test	Prompt	Pyramid			
		User Engagement	response coherence	satisfaction	reasoning transparency
HumanEval Evaluating Large Language Models Trained on Code	Write a Python function named has_close_e	4	5	5	5
	Write a Python function named get_row that	4	5	5	5
	Write a Python function named merge_dict	4	4	5	5
	Write a Python function named custom_sort	4	4	5	4
	Write a Python function named find_peak_e	5	5	5	5
	Write a Python function named rotate_matri	4	4	5	5
	Write a Python function named compress_s	5	4	4	5
	Write a Python function named sum_of_left	4	5	5	4
	Write a Python function named longest_sub	5	5	4	4
	Write a Python function named validate_bin	4	4	4	5

## GPQA: A Graduate-Level Google-Proof Q&A Benchmark

Test	Prompt	GPT-3.5			
		User Engagement	response coherence	satisfaction	reasoning transparency
GPQA: A Graduate-Level Google-Proof Q&A Benchmark	A large gene has dozens of exons, of which	2	3	4	4
	Two quantum states with lifetimes of $10^{-9}$ s	3	3	3	3
	In the process of photosynthesis, the light-d	3	2	2	3
	A particular protein functions as a channel ir	3	3	3	4
	Neurotransmitters are crucial for transmitting	1	3	3	2
	In the regulation of gene expression, transcr	3	2	2	4
	During muscle contraction, myosin motor pr	2	1	2	2
	The blood-brain barrier (BBB) selectively pe	2	3	4	2
	In the process of oxidative phosphorylation,	2	2	2	3
	The adaptive immune system relies on the r	2	3	1	2

		GPT-4			
Test	Prompt	User Engagement	response coherence	satisfaction	reasoning transparency
GPQA: A Graduate-Level Google-Proof Q&A Benchmark	A large gene has dozens of exons, of which	4	4	4	3
	Two quantum states with lifetimes of $10^{-9}$ s	4	4	4	4
	In the process of photosynthesis, the light-d	4	5	3	4
	A particular protein functions as a channel in	3	4	4	4
	Neurotransmitters are crucial for transmitting	4	3	3	4
	In the regulation of gene expression, transcr	4	4	3	4
	During muscle contraction, myosin motor pr	4	5	4	5
	The blood-brain barrier (BBB) selectively pe	3	5	4	5
	In the process of oxidative phosphorylation,	5	3	3	3
	The adaptive immune system relies on the r	4	5	5	4

		Pyramid			
Test	Prompt	User Engagement	response coherence	satisfaction	reasoning transparency
GPQA: A Graduate-Level Google-Proof Q&A Benchmark	A large gene has dozens of exons, of which	3	4	3	4
	Two quantum states with lifetimes of $10^{-9}$ s	3	4	3	5
	In the process of photosynthesis, the light-d	3	3	5	5
	A particular protein functions as a channel in	4	5	5	4
	Neurotransmitters are crucial for transmitting	3	3	5	5
	In the regulation of gene expression, transcr	4	3	3	4
	During muscle contraction, myosin motor pr	4	5	3	5
	The blood-brain barrier (BBB) selectively pe	3	4	4	5
	In the process of oxidative phosphorylation,	3	4	4	4
	The adaptive immune system relies on the r	5	4	5	4