

*The Computation of
Natural Circulation
in Large Boilers*

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To

MY LOVING PARENTS

this work is respectfully dedicated

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Introduction

At present, many large capacity boilers are being built or are in the preliminary stages of design. At some phase of the design stage, the circulation characteristics of the unit must be determined in order to properly apportion riser and downcomer circuits. The simplest method of doing this would be to extrapolate the existing experimental data on similar units. However, boilers are usually built to a customer's specifications and in general no two units are made identical for the same set of operating conditions. Thus, in extrapolating, it is very possible to introduce serious faults in design because of the inapplicability of the extrapolated data. The technical data available in the literature contains many cases of overheating and subsequent failure of boiler tubes due to faulty and inadequate circulation.^{(47,60,61)*}

The work of Munzinger⁽⁷⁾ in 1922 has been the basis of many papers written on the subject of the circulation of steam and water in natural circulation boilers. In order to obtain a workable solution, various assumptions as to the rate of heat absorption, friction coefficients, and the state of the mixture of steam and water were made. Since the appearance of this work, many excellent papers have been published on the mechanism of heat transfer and the mechanics of boiling. While much work has been done and is being done on this subject, it is still not fully understood and remains a fertile field for further investigation. In order to fully develop the subject, this work has been divided into the following three sections:—

1. A qualitative description of the mechanics of boiling, *i.e.*, the change of water to steam in a vertical tube according to the latest available data.
2. The mathematical development of all the necessary equations needed to compute the circulation characteristics of a natural circulation boiler. This section also includes curves that have been developed to facilitate circulation computations.
3. A large "Twin Furnace" unit on which circulation tests were made is completely analyzed by means of both the equations and curves of Section II. In addition, two topics of interest are discussed in this section.

A comprehensive bibliography is to be found at the end of this work. It is hoped that this bibliography will be of use for further investigation in this field.

* Numbers in parentheses refer to the bibliography at the end of this work.

I *Analysis of the Change from Water to Steam in a Vertical Tube*

In this section, a description of the phenomena that occur in a vertical tube in which the liquid flows upward and is simultaneously being heated and evaporated is given. Most of the experimental work on this subject has been performed at or near atmospheric pressure, and very little data is available at the pressures and rates of heating usually found in large modern boilers. The analysis given here follows closely that given in the paper by Lewis and Robertson.⁽⁶²⁾ Fig. 1 shows the findings of these authors and others. The vertical scale on this figure has been very much reduced in comparison to the horizontal scale. All reference to sections *A, B, C, etc.*, will be taken as meaning those sections which have been correspondingly marked on Fig. 1.

If the water is assumed to enter the downcomer system feeding this tube at saturation conditions, then it will be sub-cooled an amount corresponding to the increase in pressure due to the weight of the column of liquid above it, upon entering the tube. Thus, up to section *A*, heat must be added to bring this liquid to saturation conditions, and up to this section there will only be liquid in the tube. At the average entrance velocity usually found in large boilers, the Reynolds Number will be greater than 2100 and the flow will be turbulent.⁽³³⁾

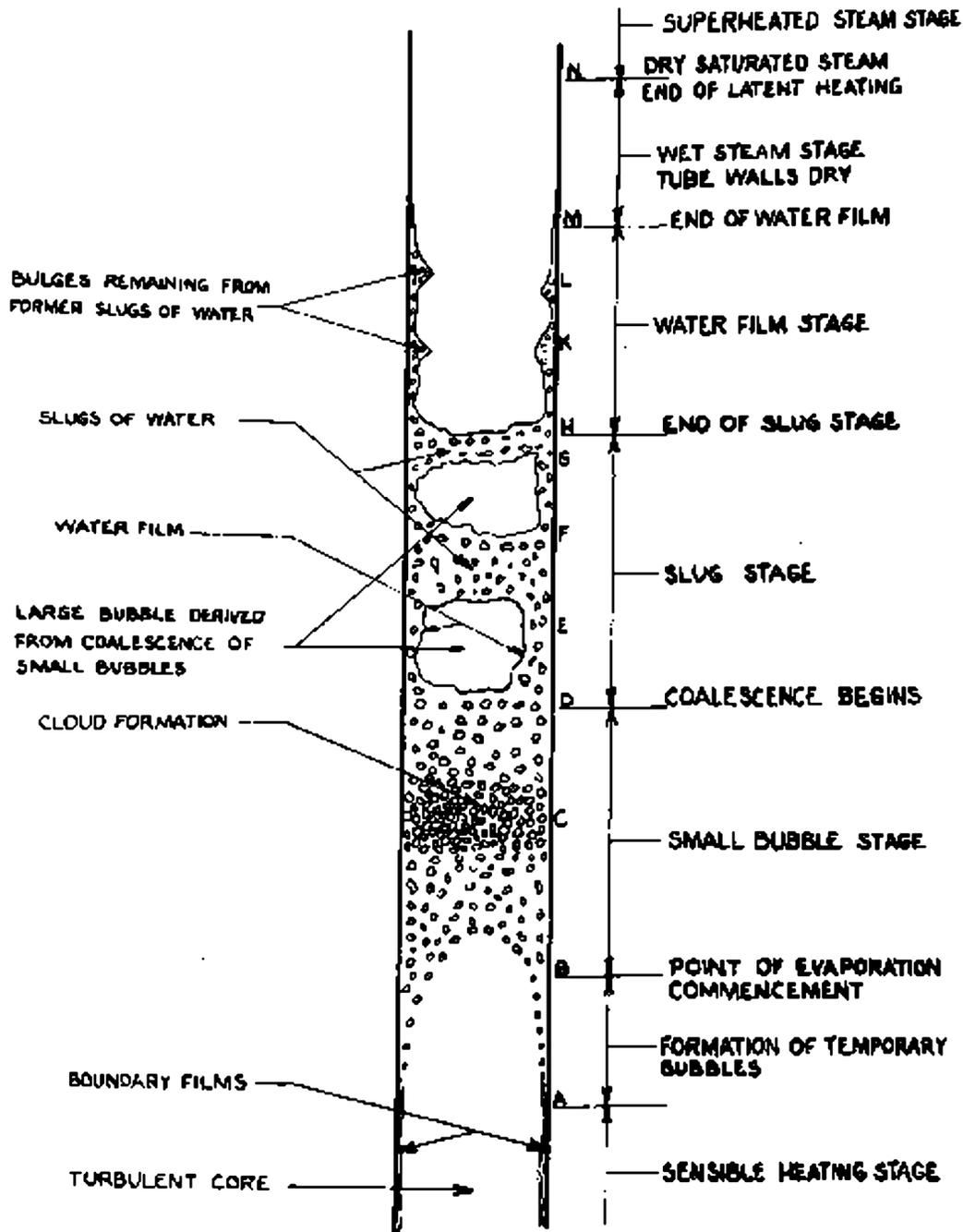


FIG. 1 CHANGE FROM WATER TO STEAM IN VERTICAL TUBE
VERTICAL SCALE DECREASED

For this condition, any cross-section through the tube up to section A will indicate the following: next to the tube wall, there exists a thin layer of fluid moving with laminar or viscous motion, then a transition zone between laminar and turbulent motion, and finally the turbulent core of the main body of the liquid. The existence of these various states of flow has been thoroughly investigated and found to be essentially correct by many investigations.^(33, 49, 66, 70, 71, 87) According to McAdams,⁽³³⁾ heat is first transferred from the wall of the tube to and through the laminar film by conduction. Between the laminar and buffer layers, heat is transferred by mechanical mixing due to the eddy formation and also by conduction due to the existence of a radial temperature gradient. The transference of this heat to the turbulent core is accomplished by the mechanisms of turbulent mixing and conduction. In this latter process, the greater portion of the heat transfer is accomplished by the mixing and eddies that occur in the turbulent zone.

Due to the continued heating in the section from A to B, small bubbles of superheated steam will start to form in the water that is in immediate contact with the tube wall. It has been shown in Keenan's work⁽³⁾ that surface tension causes the pressure in a spherical bubble to be in excess of the pressure of the surrounding liquid and inversely proportional to the radius of the sphere. Thus, a bubble of infinitely small radius would have to have an infinite pressure within it in order to remain in equilibrium. The formation of these bubbles usually starts on the many small curved surfaces of the tube wall or around nuclei of air particles or other impurities in the liquid. Before such bubble formation occurs, it is necessary that the temperature of the fluid adjacent to the wall be considerably above that of saturation conditions.⁽⁴⁴⁾ Once the bubble has formed, it is highly unstable, for, as the radius of the bubble increases, the tension in the enveloping sphere becomes unable to balance the excess of pressure within it.

The bubble, once formed on the tube wall or nuclei present, will continue to grow larger in diameter until it either bursts through its enveloping film or is swept off the wall of the tube by the liquid moving past the wall. These bubbles then travel inward toward the center of the tube and the turbulent core that exists there. Because of the radial temperature gradients that exist in any cross-section of the tube, the bubbles then collapse, since the temperature in the core is sufficiently high to enable the bubbles to exist. This process occurs in the section of the tube from A to B. In the process of collapsing and subsequent condensation of the vapor in the bubble, the latent heat of vaporization of the vapor is given to the turbulent core and raises its temperature to more nearly that of the saturation temperature. When the core temperature becomes sufficiently high (above section B), the bubbles do not collapse. Since the temperature is high enough to maintain the equilibrium of these bubbles, they will be permanent and continue to increase in both size and number. The density of the vapor inside the bubble is less than that of the saturated liquid it displaces and there will be a relative velocity between the bubbles and the main body of the liquid. This relative velocity has been called "slip velocity" by many authors.^(1,41, 65) Fig. 7 of Section II of this work shows the value of this slip velocity as a function of

tube diameter and absolute pressure. This figure is from the work of Nothman⁽¹⁾ who correlated the data of Behringer⁽³⁷⁾ and converted it into English units from the metric units of the original data.

In the section from *B* to *C*, the formation and growth of the bubbles continues and the distribution of the bubbles throughout the liquid in this section is fairly uniform. At some point in the tube, such as *C*, the distribution is no longer uniform but the bubbles tend to crowd together and form what has been termed “clouds”. Interspersed with these clouds are sections in which the number of bubbles in any cross-section of the tube is less than the number in any corresponding section between *B* and *C*. At some point higher in the tube, *D*, the bubbles in these clouds tend to coalesce and form a single large bubble occupying the entire flow area of the tube. This action displaces some of the liquid in the tube and forms a slug of water between any two such bubbles. This slug of water is pushed ahead by the largest steam bubble behind it and in the section between *D* and *H*, the tube is occupied by alternate slugs of water and bubbles of steam. In this section, the velocity of the water slugs and steam bubbles is the same. As they continue to travel upward, there is an added evaporation of the water due to the continued heating and also due to the decrease of pressure due to the weight of the column of liquid.

The evaporation that occurs due to the decrease in the static head has been termed “self-steaming”⁽⁶²⁾ or evaporation intensification.⁽¹⁾ This self-steaming is essentially an adiabatic evaporation⁽⁶²⁾ and the water in the tube loses an amount of heat equal to the latent heat of vaporization at the pressure at which it occurs. Any steam in the tube will also expand adiabatically due to this decrease of pressure. Nothman⁽¹⁾ has computed the effect of this self-steaming at various pressures and found that these effects are usually small and in most cases may be neglected in circulation computations. This is the same conclusion reached by Lewis & Robertson.⁽⁶²⁾

The continued evaporation in the tube causes the water slugs to become smaller and smaller until they finally cease to exist as such in the tube. At all times up to this stage in the tube, there exists a film of water on the tube wall between the wall and the bubbles of steam in the tube. Thus, above *H*, there are no slugs of water in the tube; only the water film on the tube wall. This film persists from *H* to *M*, where continued evaporation causes the vapor to become dry and saturated, and finally the vapor becomes superheated. In the section from *H* to *M*, the film of water on the tube wall travels at a velocity somewhat less than that of the steam in this section. During the breaking up of the steam bubbles and the final evaporation of the water film on the tube wall, particles of water are entrained in the main body of the vapor flowing in the core of the tube. These particles of water continue to flow upward in the tube with the steam. If the section of the tube above *H* is not long enough, or the rate of heating is not intense enough, these particles of water will contribute to carry-over.⁽⁶²⁾

In each of the stages of the process that has been described above, there are various coefficients and rates of heat transfer due to the difference in the properties of the

contents of the tube in various vertical sections of the tube. If the rate of heat transmission and the coefficients of heat transfer are assumed constant throughout the entire length of the tube, the various actions that occur in each section of the tube could be readily calculated. This, however, is not the case, and the analysis of the heat transfer is complex.

In modern boilers, it is common to find that 75% or more of the total steam production is produced in the water walls of the unit. These walls are placed such as to receive the direct radiation from the flame in the furnace. The resistance and temperature of the gas film on the outside of the tubes will be relatively constant along the tube length. The other resistances involved are those of the tube metal, the inside water (or steam) film, and the resistance of the main body of fluid in the tube.

McAdams⁽³³⁾ recommends the following equation for the heat transmitted from the inside tube wall to the contents of the tube:

$$\frac{hD}{K} = 0.032 \left(\frac{DG}{\mu} \right)^{0.8} \left(\frac{c_p \mu}{K} \right)^{0.4} \quad (A)$$

where:

h = Coefficient of heat transfer between fluid and surface— $\frac{\text{Btu}}{\text{hr.}} \times \text{ft.} \times$

D = Inside Tube diameter—ft.

K = Thermal conductivity of fluid— $\frac{\text{Btu}}{\text{hr.}} \times \text{sq.ft.} \times \text{°F per ft.}$

G = Mass velocity— $\frac{\text{lb.}}{\text{hr.}} \text{ per sq.ft. of cross section}$

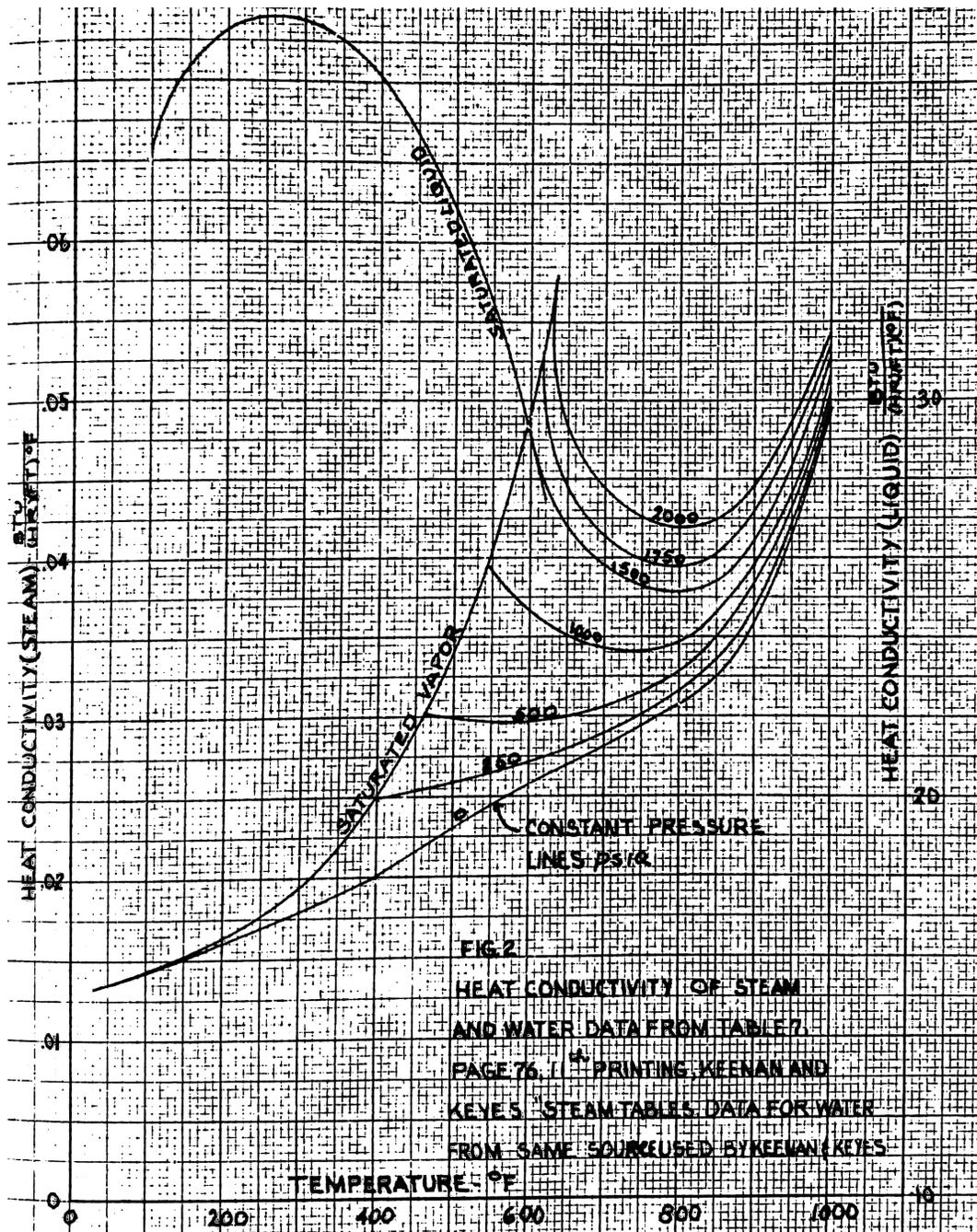
C_p = Specific heat at constant pressure— $\frac{\text{Btu}}{\text{lb. fluid}} \text{ per °F}$

μ = Absolute viscosity of the $\frac{\text{fluid-lb.}}{\text{ft.-hr.}}$

For a velocity of five feet per second and an inside diameter of 0.104 feet, Lewis & Robertson⁽⁶²⁾ have evaluated this expression at various pressures and their results are given in Table A below.

Table A

Pressure psis	100	300	500	1000	2000
Inside tube wall to sat. liquid (h)	1840	1050	2000	1970	1910
Inside tube wall to sat. steam	680	802	915	1170	1670



If equation A is evaluated using the data for the physical properties given in the Appendix for the Lewis & Robertson paper it will be found that the values of h given in Table A for inside tube wall to saturated steam are incorrect.

In addition to this, these authors have used the data for the specific heat and thermal conductivity from the earlier printing of the Keenan and Keyes Tables⁽⁴⁵⁾ and viscosity data from the work of Hawkins, Solberg, & Potter.⁽⁹⁰⁾ Since the appearance of these works, new tests and formulations of these physical properties have been made. The latest and probably most accurate tabulation of these properties appears in the 11th printing of the Keenan & Keyes work, dated 1945. Using this data, the author has plotted Figs. 2 and 5 and recomputed the values in Table A. The results of this computation are given in Table B.

In computing this data, the author used Table 7 of the Keenan & Keyes 11th printing for the thermal conductivity of the steam. Because of what appeared to be a discrepancy in this table, the author communicated with Professor Keyes, and in a letter dated March 11, 1948, Professor Keyes confirmed the fact that three values are incorrect. The corrected values are given below and were used to compute Table B and to plot Fig. 2.

Values for heat conductivity to be corrected in Table 7, Keenan & Keyes 11th printing:

Pressure psis (sat.)	Heat Conductivity (corr.)
0	13.16
500	30.15
1750	53.18

Table B

Pressure psis	100	300	500	1000	2000
Inside tube wall to sat. liquid (h)	1755.00	1855.00	1845.00	1810.00	1675.00
Inside tube wall to sat. steam	8.38	23.30	44.30	95.60	322.00

Since Table B shows that the value of h is less for saturated steam than for the saturated liquid, it follows that the tube wall temperatures in the section containing the saturated steam will be higher than the corresponding wall temperatures in the section carrying saturated liquid. It would therefore be expected that the tube wall temperature in the section above M would increase considerably over that in the sections below this point where a water film is maintained on the tube wall.

In the section from A to B , the conditions are very complex and there is very little data available for these conditions. Various attempts have been made to correlate the heat transfer and pressure drop data by use of the Reynolds Analogy,⁽³³⁾ Prandtl Analogy, and combinations of various dimensionless groups. The data that is available

indicates that there is a definite increase in heat transfer in this section but the data is so sketchy as to make other than qualitative predictions almost useless.

Thus far, only a vertical tube has been considered. In any boiler, the generating tubes will invariably have sections that are inclined to the vertical at various angles depending on the particular design. If the tube is only slightly inclined to the vertical, it would be expected that the description given above for a vertical tube will be essentially the same for this case. However, as the inclination is made still greater, the steam and water tend to separate, with the water flowing along the bottom of the tube and the steam flowing along the top section. If the tube is heated along the entire outside periphery or along the top, the tube metal temperature will increase in the section where there is steam. The heat transfer across this steam blanket (as it has been frequently termed) takes place by the mechanism of conduction and convection and is considerably smaller than in the section where the tube wall is wetted.

The next logical question that arises is what constitutes good circulation. It would appear that whatever the criterion is, it will be a function of the individual design, the saturation pressure and temperature, the physical properties of the mixture of steam and water, the fraction of steam by volume and by weight in any section of the tube, the amount that the tube is inclined to the vertical, the roughness of the tube surfaces, the tube material, and the temperature in the combustion zone of the furnace. Lewis and Robertson⁽⁶²⁾ set as the criterion of good circulation a vapor-by-weight fraction of 0.20 leaving the tube. The fraction of steam by volume would appear to be a better criterion since, as long as the water film on the tube wall is maintained, the harmful effects of steam blanketing will not occur. Partridge and Hall⁽⁶⁰⁾ have shown that the inclination of the tube plays a marked role in determining what the optimum ratio of water to steam in the tube should be and what this ratio should be to avoid tube failure in an inclined tube due to overheating.

The author has compared test data on four Twin Furnace units (similar to the one used in Section III of this work) of different capacities and operating pressures. These units have been in satisfactory operation for a number of years and no trouble has been experienced that could in any way be attributed to faulty circulation. In these units, it was found that the fraction of steam by weight leaving the tubes was always less than the criterion of 0.20 set by Lewis and Robertson, and in all cases, the fraction of steam by volume leaving the tubes was less than 0.85. As has been stated above, there can be no one universal criterion of good circulation. Each individual design would have to be tested and the results completely correlated to find the effect of each of the variables, and only then could such a criterion be established. Such a correlation has not as yet been made or, if it has, the results have not as yet been published. The amount of data on natural circulation test data in actual installations is too small to justify the establishing of any such criterion; it would merely be a guess. Therefore, no such criterion of good circulation will be set up in this work. It is hoped that such a correlation will be made in the near future, since the importance of adequate

circulation in a natural circulation boiler cannot be over-emphasized if trouble-free operation is to be had in these units.

II Derivation of Equations for Natural Circulation Computations

The equations developed in this section follow the method of Munzinger⁽⁷⁾ but have been put in a convenient form advocated by Mr. John Blizard. The following nomenclature will be used throughout except as otherwise noted:

E	= Steam produced— $\frac{\text{lbs.}}{\text{hr.}}$
W	= Weight of water entering tube— $\frac{\text{lbs.}}{\text{hr.}}$
q	= Rate of heat absorption— $\frac{\text{Btu}}{\text{hr.} \times \text{sq.ft.}}$ (total outside surface)
S	= Specific volume of saturated steam— $\frac{\text{cu.ft.}}{\text{lb.}}$
s	= Specific volume of saturated liquid— $\frac{\text{cu.ft.}}{\text{lb.}}$
h	= Latent heat of vaporization— $\frac{\text{Btu}}{\text{lb.}}$
V_o	= Velocity entering tube— $\frac{\text{ft.}}{\text{sec.}}$
$\$$	= Specific volume of mixture at any point in tube— $\frac{\text{cu.ft.}}{\text{lb.}}$
d	= Inside diameter of tube—inches
D	= Outside diameter of tube—inches
g	= Acceleration due to gravity— $\frac{\text{ft.}}{\text{sec.}}$ per sec.
f	= Friction factor
l	= Length of tube to point considered—ft.
L	= Total length of tube—ft.
P	= Density of mixture relative to saturated liquid
P_0	= Density of mixture entering tube relative to saturated liquid
N	= $\frac{Dq(S-s)}{75d^2h} - \frac{1}{\text{sec.}}$
ΔP	= Static head loss—ft. of saturated liquid
B	= Vapor friction by volume
λ	= Vapor fraction by weight
A	= Flow area—sq.ft.
K	= $\frac{\text{Flow area of circuit}}{\text{Flow area of } n\text{th. circuit}}$
X	= $\frac{NL}{KV_o}$
$SPdl$	= Gravity head
\bar{P}	= $\frac{SPdl}{L}$
θ	= Angle circuit makes with horizontal
R_e	= Reynolds number
μ	= Viscosity— $\frac{\text{lb.}}{\text{ft.hr.}}$
K_B	= Bend loss coefficient

Subscript o denotes entering conditions of circuit 1. Subscript on denotes entering conditions of circuit "n". Subscripts $1, 2, \dots, n$ denote properties of circuits 1, 2, \dots , n.

In order to obtain a workable solution the following assumptions will be made:

1. The velocity of the mixture at any section perpendicular to the axis of the tube is constant.
2. The mixture of steam and water is uniform and homogeneous.
3. The velocity of the steam at any point along the tube is equal to the velocity of the water at the same point.
4. The rate of heat absorption along the heated section of the tube is constant and uniform.
5. Saturated liquid enters the tube.

While all of these assumptions are open to question, they serve as a convenient starting point. The equations developed from these assumptions may be modified later to account for any deviations from the assumed conditions. Fig. 3 shows schematically a simple circuit having equal downcomer and riser flow areas. The total amount of steam evaporated per hour is given by:

$$E = \frac{\pi D l q}{12h} = \frac{\pi D L q}{12h} \quad (1)$$

and the weight of water entering the circuit per hour is given by:

$$W = \frac{V_o \pi d l 2 \times 3600}{144 \times 4 \times s} \quad (2)$$

From equations (1) and (2), the specific volume of the mixture at any point along the tube will be given by equation (3) and the velocity of the mixture at the corresponding point is given by equation (4).

$$\$ = \frac{ES + (W - E) s}{W} \quad (3)$$

$$V = \frac{\$}{s} \times V_o \quad (4)$$

By substitution of (1), (2), and (3) into (4), the velocity at any section in the tube can be expressed in terms of the properties of the fluid entering the tube, the rate of heat absorption, the dimensions of the tube, and the velocity entering the tube.

$$V = \left[\frac{\frac{\pi D L q s}{12h} + \left(\frac{V_o \pi d^2 \times 3600}{4 \times 144 \times s} - \frac{\pi D L q}{12h} \right) s}{\frac{s V_o \pi d^2 \times 3600}{4 \times 144 \times s}} \right] V_o \quad (5)$$

Re-arranging equation (5) yields equation (6).

$$V - V_o = \frac{DqL(S - s)}{75d^2h} \quad (6)$$

If we now let the right hand side of equation (6) equal NL , where:

$$N = \frac{Dq(S - s)}{75d^2h} \quad (7)$$

equation (6) becomes:

$$V - V_o = NL \quad (8)$$

The substitution of (8) into (4) yields the following relations:

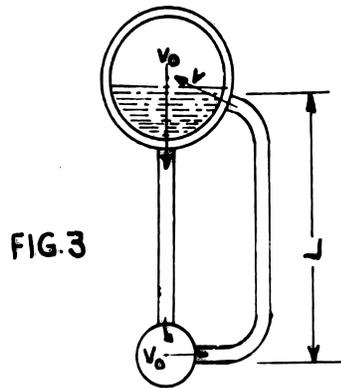
$$\frac{S}{s} = 1 + \frac{NL}{V_o} \propto P = \frac{1}{1 + \frac{NL}{V_o}} \quad (10,10a)$$

From McAdams⁽³³⁾ pages 111 to 125, the static head loss for length dl along a vertical tube can be written as:

$$-dP = \frac{4f}{d} \times \frac{V^2}{2g} \times dl + \frac{V}{g}dV + dl \quad (11)$$

Equation (11) is in terms of feet of mixture and it is more convenient to rewrite it in terms of feet of saturated liquid.

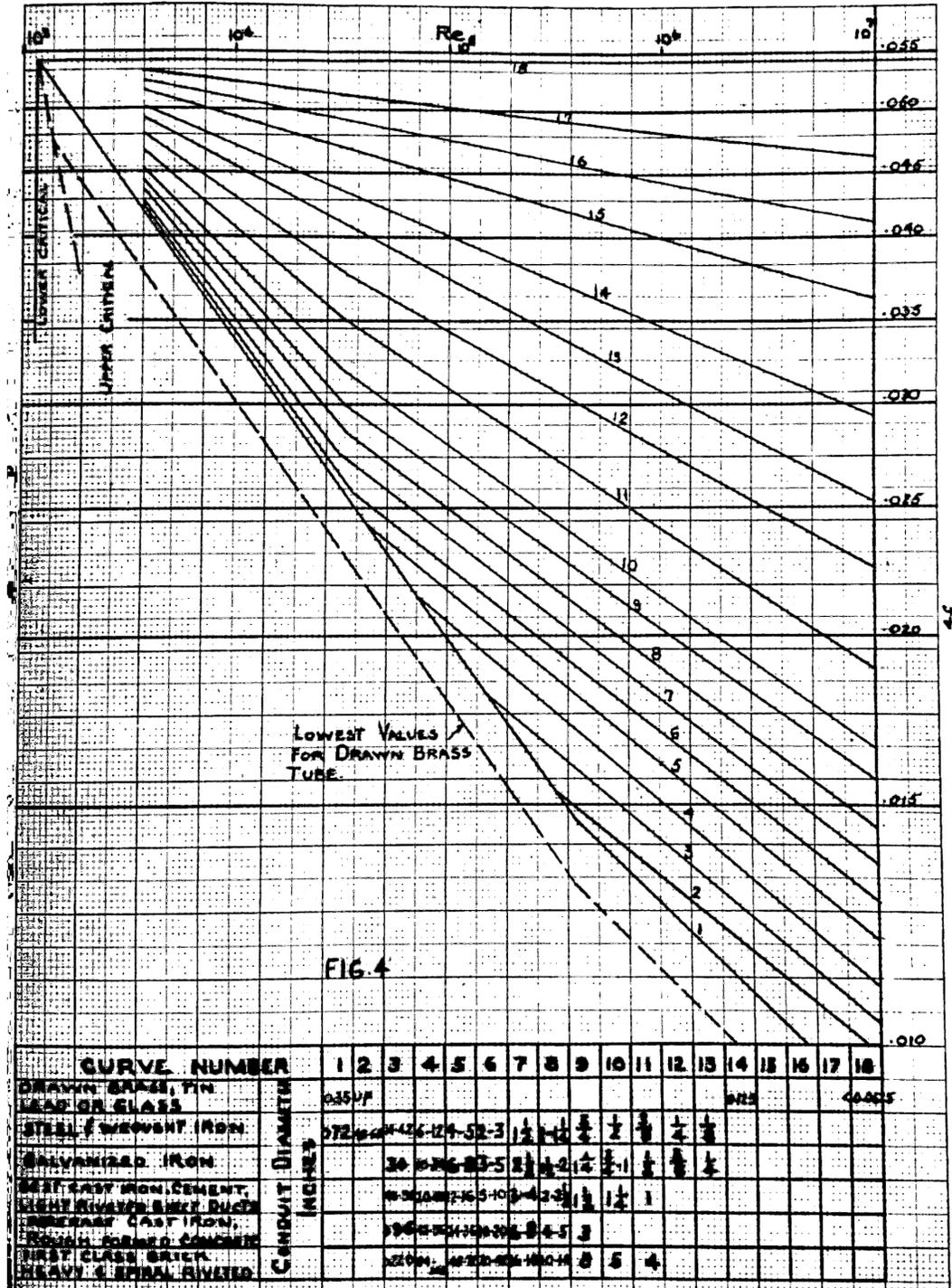
$$-dP = \frac{4f}{d} \frac{P}{2g} \left(\frac{V_o}{P} \right)^2 dl + \frac{V_o}{g}dV + Pdl \quad (12)$$



In equations (11) and (12) the first term on the right-hand side represents a friction loss, the second term the loss due to an increase in momentum, and the third term a loss due to the weight of the column of mixture. In addition to these losses, we must also consider an entrance and exit loss and bend losses.

In order to evaluate equation (12), it will be necessary to determine the relation between f , dv , P , and l . Thus far equations (10) or (10a) give the relation between three of these variables but as yet no relation has been developed giving the friction factor as a function of the other variables.

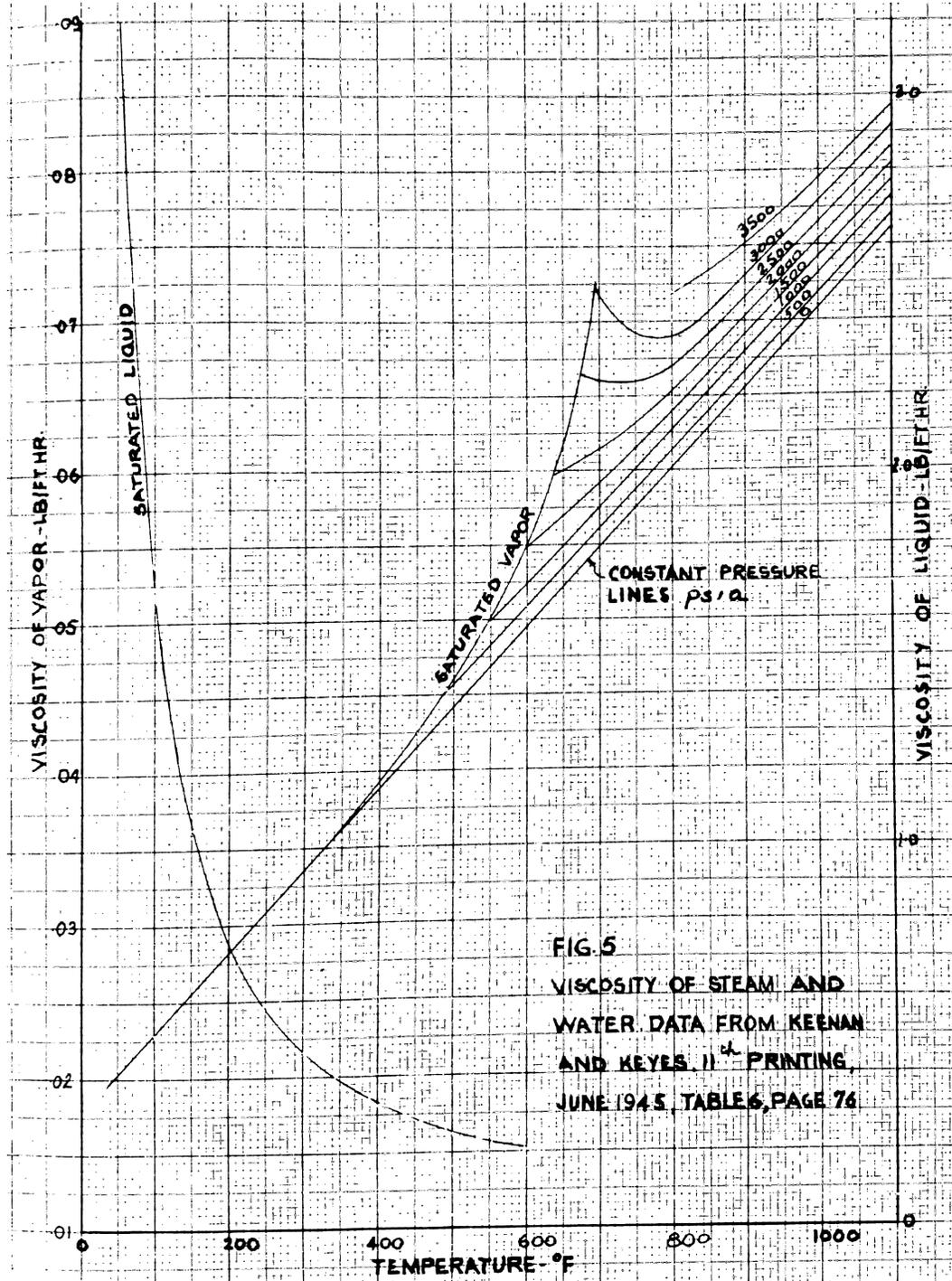
For isothermal flow the friction factor has been found to be a function of the Reynolds Number and the relative roughness of the tube.^(33, 49, 71, 70) Fig. 4 shows a chart based on the work of Pigott⁽⁴⁹⁾ from which the friction factor for isothermal flow can readily be evaluated. For the complex conditions existing when water is being boiled, this relation cannot longer be used since it is not known whether the friction factor remains a function of only the Reynolds Number and the relative roughness of the tube. Even if this functional relation is true under these conditions, it still cannot be used since no data is available to evaluate the viscosity of a mixture of steam and water.



From the data of Boelter & Kepner⁽⁹⁴⁾ and their own tests, Dittus and Hildebrand⁽³⁹⁾ have proposed that Fig. 4 for isothermal flow can be used in the case of two-phase flow if the Reynolds Number is evaluated using the average specific volume of the mixture and the viscosity of the liquid. For the cases that they considered, this method gave an excellent correlation with test data. Martinelli^(55,81) has recently proposed a method of correlating isothermal flow with non-isothermal flow and correlated his method with the test data reported in the paper by Davidson, *et al.*⁽⁶⁶⁾ If either of these methods is used to evaluate the friction factor in terms of the other variables, the expressions become very complex and very difficult to apply.

Nothman⁽¹⁾ has made a correlation of the expressions for friction factor as reported or proposed by various authorities and he found that the expressions have such a wide divergence that it is justifiable to assume as a first approximation that the value is essentially constant and equal to 0.006. The author has checked this value against the methods proposed by Dittus and Hildebrand and Martinelli for various assumed conditions and using Figs. 4 & 5 found that this value agrees with these methods very well.

Throughout this work, a value of friction factor equal to 0.006 will be used. The justification of this rests in what has been said above and the fact that the simplification is considerable in subsequent developments. It must be fully understood this is an assumption and must be changed if further test data show the need of it.



Equation (12) Can now be evaluated term by term as follows:

Friction Loss

$$-dP = \frac{4f}{2gd} \times \frac{V_o^2}{1 + \frac{NL}{V_o}} \left[1 + \frac{NL}{V_o} \right]^2 dl \quad (13)$$

$$\Delta P = \int_0^L \frac{4f}{2gd} \times V_o^2 \left[1 + \frac{NL}{V_o} \right] dl = 4f \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{NL}{2V_o} \right] \quad (14)$$

Acceleration Loss

$$\Delta P = \int_0^L \frac{V_o dv}{g} = \frac{V_o}{g} (V_2 - V_1) = \frac{V_o^2}{zg} \times 2 \frac{NL}{V_o} \quad (15)$$

Bend Loss

The loss in static head due to a bend in a pipe may be written as follows:⁽⁴⁹⁾

$$\Delta P = K_B \frac{Y^2}{2g} \quad (16)$$

where K_B is a bend loss coefficient. Fig. 6, taken from Kent,⁽⁹⁵⁾ allows the easy evaluation of this bend loss coefficient. It must be remembered that this loss is in addition to the loss due to friction.

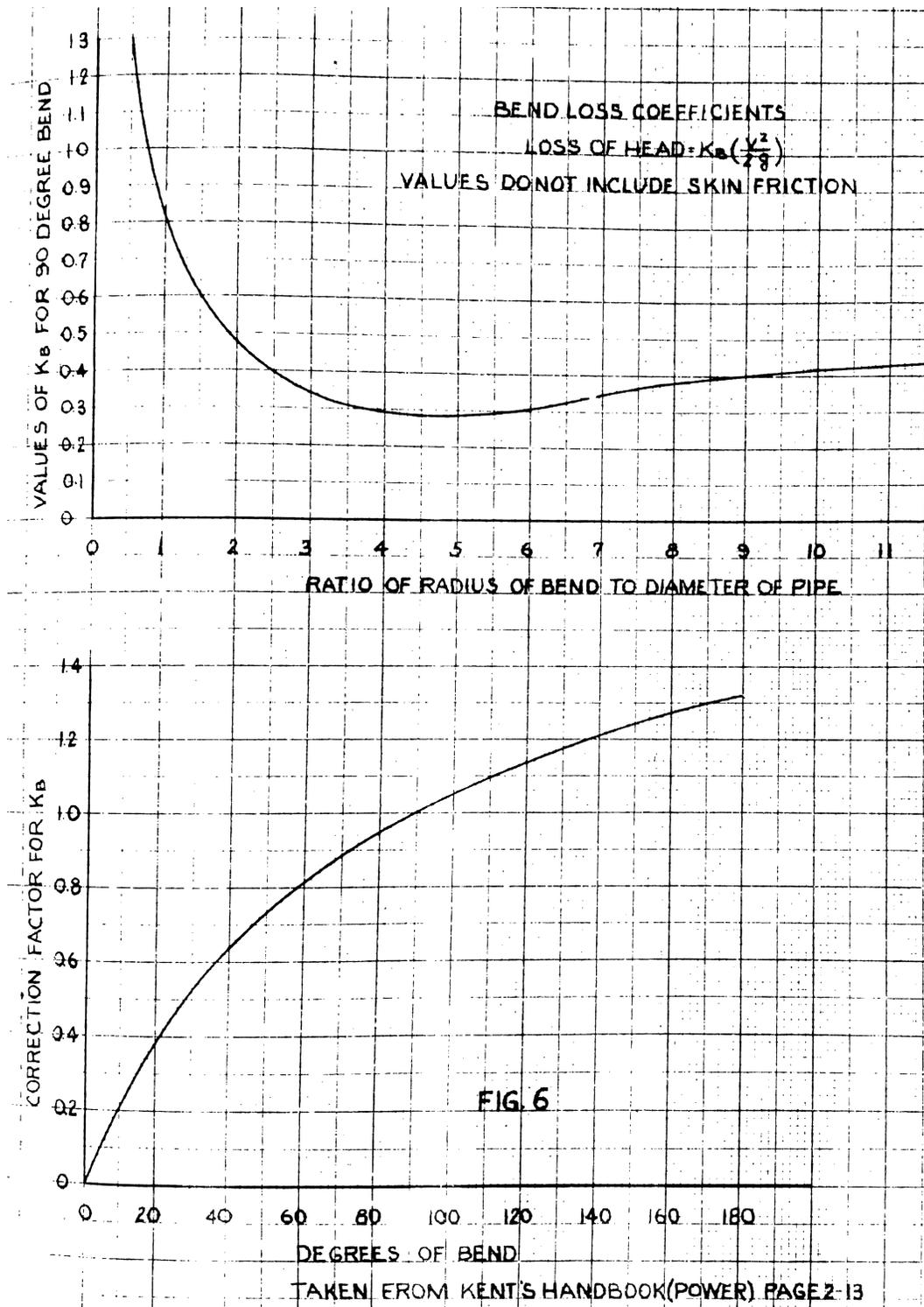
Gravity Head

$$\text{Gravity Head} = \int_0^L \frac{dl}{1 + \frac{NL}{V_o}} = \frac{V + o}{N} \log_e \left[1 + \frac{NL}{V_o} \right] \text{ for a vertical tube} \quad (17)$$

Entrance & Exist Loss

The head available in the downcomer system must also supply the kinetic energy of the liquid entering the riser system, and this is also a loss in available static head. In addition, there is an entrance loss that must be accounted for. The sum of these losses is given by:^(49, 62, 65)

$$\Delta P = 1.5 \frac{V_o^2}{2g} \quad (18)$$



Vapor Fraction by Volume

From equation (10):

$$\frac{s}{S} = \frac{1}{1 + \frac{NL}{V_o}} = \frac{B \frac{1}{S} + (1-B) \frac{1}{s}}{\frac{1}{s}} \quad (19)$$

$$\text{and } B = \left(\frac{1}{1 + \frac{NL}{V_o} - 1} \right) \frac{1}{\frac{s}{S} - 1} = \frac{S}{S-s} \left[\frac{\frac{NL}{V_o}}{1 + \frac{NL}{V_o}} \right]$$

Vapor Fraction by Weight

$$\frac{\$}{s} = 1 + \frac{NL}{V_o} = \frac{\lambda S + (1-\lambda)s}{s} \quad (20)$$

$$\text{and } \lambda = \left(1 + \frac{NL}{V_o} - 1 \right) \frac{s}{S-s} = \frac{s}{S-s} \left[\frac{NL}{V_o} \right]$$

The equations developed thus far are for a single vertical tube based on the assumptions made above. If assumption 4 is not correct; that is, the rate of heat absorption along the heated section of the tube is not uniform, the equations developed above for friction loss and Gravity Head are no longer applicable. However, we may readily obtain expressions for any rate of heat absorption from those that have already been derived.

When the total heat absorbed in the tube is the same for any rate of heat absorption, the acceleration loss, entrance and exit loss, vapor fraction by weight, and vapor fraction by volume may all be properly evaluated from the expressions that have been derived for the case of uniform heat absorption.

If q is expressed as follows:

$$q = \phi(l) + Z \quad (21)$$

where ϕ is a function of length and Z is a constant, Z may be evaluated from equation (22).

$$q_{\mu}^L = \int_0^L [\phi(\lambda) + Z] dl; \quad q_{\mu} = \text{Uniform rate} \quad (22)$$

By substitution of equation (21) into equation (6), the following results:

$$P = \frac{1}{\frac{C(\phi(l)+Z)l}{V_o} + 1} \quad (23)$$

$$\text{Where } C = \frac{D(S-s)}{75d^2h}$$

Friction Loss—variable q

Equation (23) substituted in equation (13) allows us to evaluate the friction loss where the rate of heat absorption is a function of the length of the tube.

$$\Delta P = \frac{4f}{2gd} \times V_o^2 \int_0^L \left[1 + \int_0^l \frac{C(\phi(l) + Z)}{V_o} dl \right] dl \quad (24)$$

Gravity Head—variable q

The substitution of equation (28) into (17) yields the desired expression for Gravity Head when the rate of heat absorption is a function of the length of the tube.

$$\text{Gravity Head} = \int_0^L \frac{dl}{1 + \int_0^l \frac{[C\phi(l)+Z]dl}{V_o}} \quad (25)$$

Mr. John Blizard⁽⁹⁶⁾ has evaluated equation (25) for the case of heat transfer by convection and his development is essentially that given below. In this derivation, the densities are actual and not relative values. It follows from equation (25) that the change of specific volume of the mixture with 1 can be written as follows:

$$d\$ = \left[\frac{c(\phi(l) + Z) dl}{V_o} + 1 \right] s \quad (25a)$$

For convection, the ratio of heat absorption at any point in the tube q to the rate of heat absorption at the entrance to the tube q_1 is given below, where q is the greatest and b is a constant:

a constant: $\frac{q}{q_1} = e^{-bx}$

Let $x = \frac{l}{L}$; $dx = \frac{dl}{L}$

$\therefore d\$ = c'q_1e^{-bx} dx$ where c' is a constant

$$\$ - \$_{\text{ent}} = \int_0^x c'q_1e^{-bx} dx = \frac{c'}{b}q_1 [e^{-bx} + 1] = \frac{c'}{b} [q_1 - q]$$

but $\bar{P} = \int_0^1 P dx$ and $P = \frac{1}{v}$; ent. = entrance

$$\therefore \bar{P} = \int_0^1 \frac{dx}{\$_{\text{ent}} + \frac{c'}{b}q_1 [1 - e^{-bx}]}$$

$$\therefore \bar{P} = P_{\text{ent}} \left[\frac{1}{1 + \frac{c'}{b} \frac{q_1}{\$_{\text{ent}}}} + \frac{1}{b \left(1 + \frac{c'}{b} \frac{q_1}{b}\right)} \log_e \left\{ \frac{c'q_1}{b\$_{\text{ent}}} (1 - e^{-b}) + 1 \right\} \right]$$

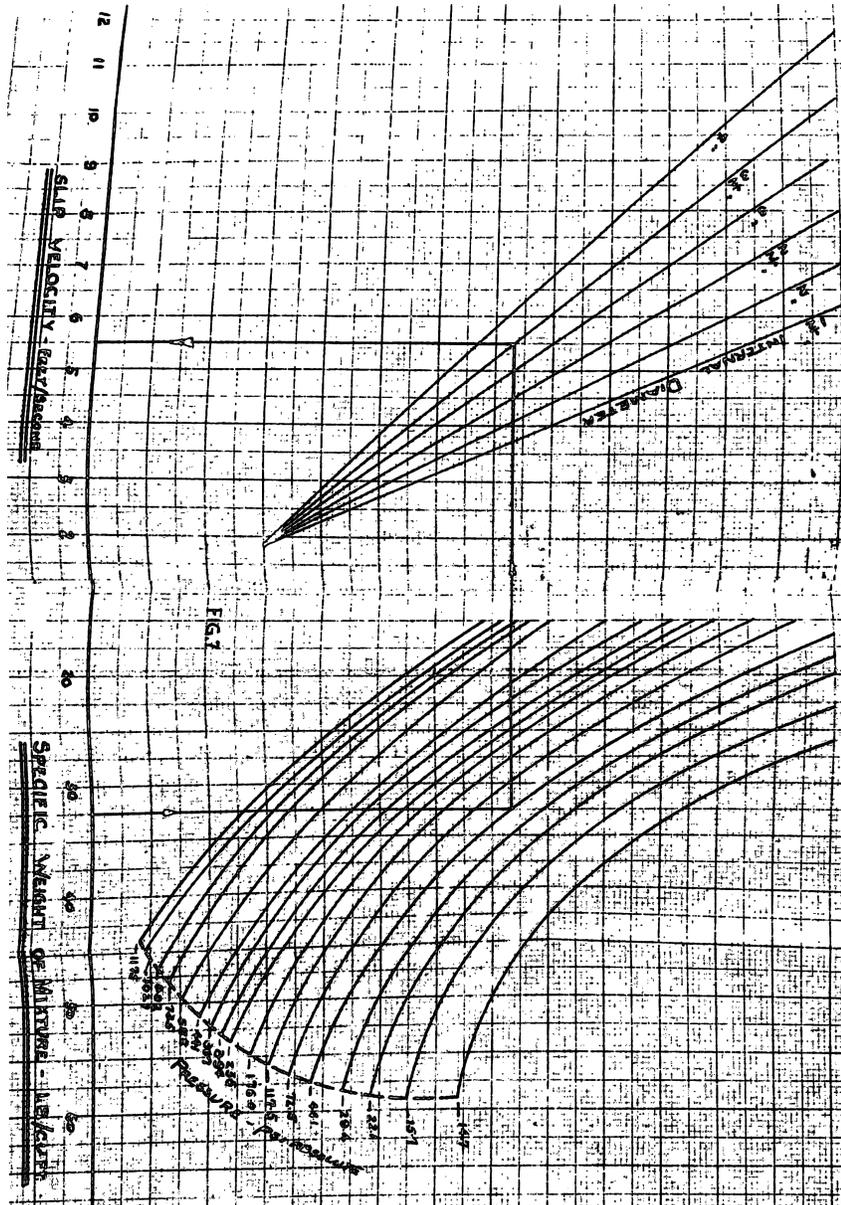
Since $1 - e^{-b} = \frac{q}{q_1} + 1$ and $\frac{c'}{b} = \frac{\$ - \$_{\text{ent}}}{q_1 - q}$

$$\frac{\bar{P}}{P_{\text{ent}}} = \frac{\frac{q_1}{q} - 1}{\log_e \frac{q_1}{q}} \left[\frac{\log_e \left(\frac{q_1}{q} \frac{\$}{\$_{\text{ent}}} \right)}{\frac{q_1}{q} \frac{\$}{\$_{\text{ent}}} - 1} \right] \quad (25b)$$

If q_1 is the least at entrance to the tube, (25b) can be used if the ratios $\frac{q_1}{q}$ and $\frac{\$}{\$_{\text{ent}}}$ are inverted where they appear in equation (25b).

Thus far, the expressions developed have been based upon the assumption that the flow of water and steam is such that there is no relative velocity between the water and the steam. That this is not the case has been shown in Section I of this work. Nothman⁽¹⁾ has derived expressions to account for this effect and, using the data of Behringer,⁽³⁷⁾ has found that an error of as much as 25% in Gravity Head can easily be incurred by neglecting this slip. The data of Behringer is shown in Fig. 7. This data was obtained from tests where the water was stationary and the relative velocity of the steam was measured. This is very different from the conditions that prevail in an actual boiler. Since this is the best test data available, this question of slip velocity will not be treated further here. It must be remembered that this is a fault in the analysis given here and must be taken into account when further data becomes available.

In order to facilitate the computations involved in applying the equations developed, a series of graphs has been developed. Table 1, based on the Keenan & Keyes data,⁽¹⁵⁾ gives the thermodynamic properties needed in circulation computations. Fig. 10 shows the relation of $\frac{s}{s-s}$ pressure to pressure absolute.



Using the data of Table 1, Fig. 11 was plotted giving the value of N as a function of tube dimensions and absolute pressure. This curve is based on a value of a equal to 10,000. For a uniform rate of heat absorption other than 10,000, the value of N read from this curve must be multiplied by the ratio of the actual rate of heat absorption to 10,000.

Figs. 16 to 22 show the total static head loss for a single tube with a uniform rate of heat absorption. The term total static head loss is meant to denote the sum of the Bend loss, Acceleration loss, Friction loss, and Entrance and Exit loss. The assumption was made that there existed one bend in the circuit with a K of 0.3 and that the friction factor is equal to 0.006. With these assumptions, equation (26) is readily arrived at:

$$\Delta P = \frac{V_o^2}{2g} \left[\left(.288 \frac{L}{d} \right) \left(1 + \frac{NL}{2V_o} \right) + \frac{2NL}{V_o} + 1.8 \right] \quad (26)$$

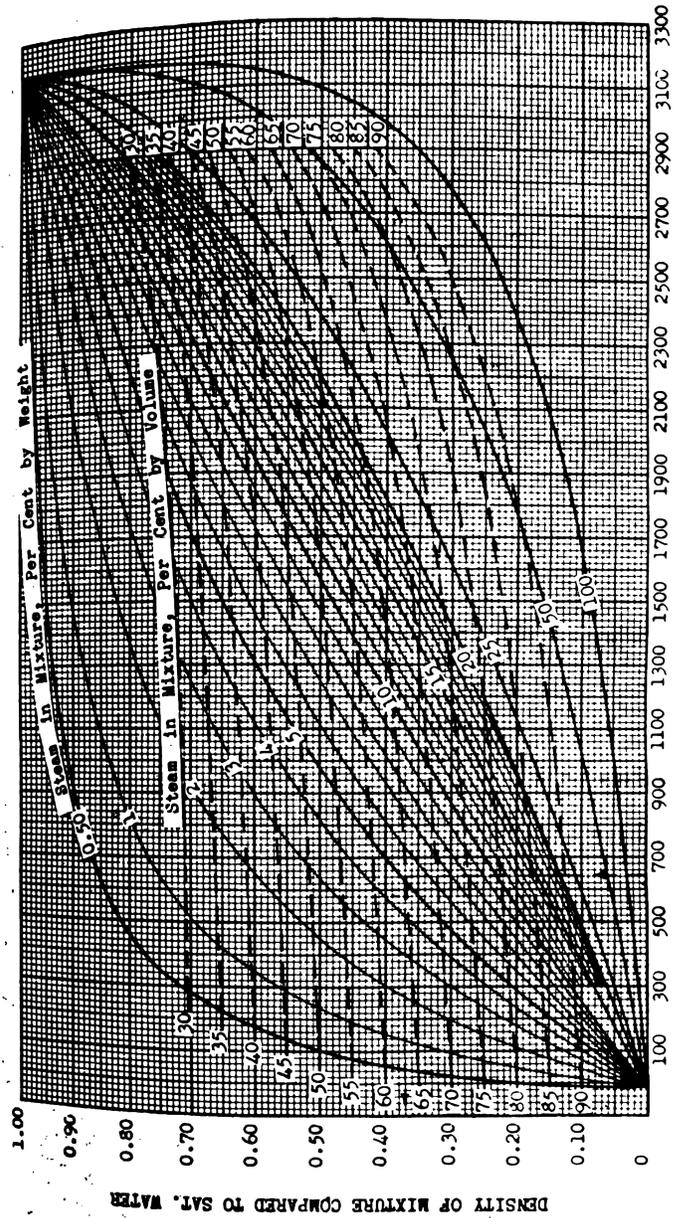
Thus the total static head loss is a function of $\frac{L}{d}$, $\frac{NL}{V_o}$ and the curves were developed on this basis. The further utility of these curves will be shown later in this section and in Section III of this work.

One of the assumptions made thus far was that saturated liquid entered the tube. Actually, it is possible to have sub-cooled liquid or liquid that has been partially vaporized entering. The section on series circuits allows this to be taken into account.

Table 1

Pressure (psis)	h	S	s	$S - s$	$\frac{s}{S-s}$	$\frac{s}{S-s}$	$\frac{S-s}{h}$
100	888.8	4.432	0.01774	4.4143	1.000	0.0040	0.00498
125	875.4	3.587	0.01792	3.5691	1.003	0.0050	0.00407
150	863.6	3.015	0.01809	2.9969	1.005	0.0060	0.00348
175	850.9	2.532	0.01827	2.5137	1.007	0.0073	0.00299
180	843.0	2.288	0.01839	2.2696	1.008	0.0077	0.00270
200	833.8	2.042	0.01852	2.0237	1.009	0.0092	0.00243
225	815.1	1.8436	0.01865	1.8251	1.010	0.0102	0.00221
250	816.9	1.6804	0.01878	1.6616	1.011	0.0120	0.00204
275	809.0	1.5433	0.01890	1.5244	1.013	0.0124	0.00189
300	794.2	1.3260	0.01913	1.3069	1.015	0.0147	0.00165
340	780.5	1.1613	0.0193	1.1420	1.018	0.0169	0.00146
400	767.4	1.032	0.0195	1.0125	1.020	0.0193	0.00132
450	755.0	0.9278	0.0197	0.9081	1.023	0.0217	0.00120
500	731.6	0.7698	0.0201	0.7497	1.029	0.0269	0.00102
600	709.7	0.6554	0.0205	0.6349	1.035	0.0323	0.000895
700	680.5	0.5687	0.0209	0.5478	1.039	0.0382	0.000795
800	668.8	0.5066	0.0212	0.4794	1.045	0.0443	0.000718
900	649.4	0.4456	0.0216	0.4240	1.053	0.0510	0.000654
1000	630.4	0.4001	0.0220	0.3781	1.058	0.0582	0.000601
1100	611.7	0.3619	0.0223	0.3396	1.065	0.0658	0.000555
1200	593.2	0.3293	0.0227	0.3068	1.071	0.0740	0.000517
1300	574.4	0.3012	0.0231	0.2781	1.083	0.0835	0.000484
1400	556.3	0.2765	0.0235	0.2530	1.095	0.0930	0.000455
1500	539.6	0.2551	0.0239	0.2310	1.105	0.1035	0.000430
1600	519.0	0.2354	0.0243	0.2111	1.115	0.1151	0.000405
1700	501.1	0.2197	0.0247	0.1932	1.125	0.1275	0.000385
1800	481.3	0.2021	0.0252	0.1769	1.145	0.1429	0.000366
1900	463.4	0.1878	0.0257	0.1621	1.155	0.1585	0.000350
2000	444.1	0.1746	0.0262	0.1484	1.175	0.1761	0.000335
2100	426.4	0.1625	0.0268	0.1357	1.200	0.1975	0.000320
2200	408.0	0.1513	0.0274	0.1239	1.225	0.2210	0.000307
2300	403.9	0.1415	0.0280	0.1127	1.250	0.2490	0.000294
2400	388.7	0.1407	0.0287	0.1020	1.280	0.2810	0.000283

The data for this table are from the Keenan & Keyes work.⁽⁴⁵⁾



GAGE PRESSURE, LB PER SQ IN.

Chart showing relationships for steam-water mixtures

FIG. 8

Series Circuits

The term “Series Circuits” as used here is meant to distinguish those circuits whose characteristics depend upon what has already happened; *i.e.*, the extent of heating and evaporation that has occurred in the tube. An example of such a circuit is shown schematically in Fig. 9. The tube has a different number of circuits for Gravity Head calculations because a new Gravity Head circuit is created by a change of slope or a change in the intensity of heating along the tube. Notes along the left of Fig. 9 denote circuits and lengths to be used for friction calculations, while notes along the right denote circuits and lengths to be used for Gravity Head circuits.

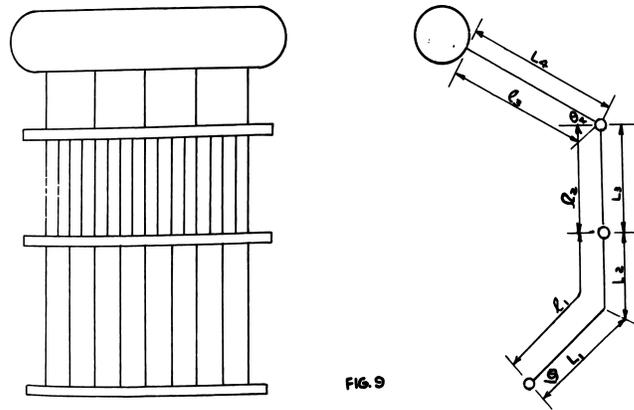


FIG. 9

While all the necessary symbols have already been given, the following symbols will be used in conjunction with the derivations in this section:

Subscript o denotes entering conditions of circuit 1.

Subscript n denotes entering conditions of circuit.

Subscripts 1, 2, . . . , n denote properties of circuits 1, 2, . . . , n.

$$K_n = \frac{\text{Flow area of circuit}}{\text{Flow area of circuit 1}} = \frac{A_1}{A_n}$$

$$X = \frac{NL}{KV_o}; X_1 = \frac{NL}{V_o}; X_o = 0$$

All other symbols are as previously given.

The velocity entering the second circuit is:

$$V_{o2} = \frac{V_o}{P_{o2}} \times \frac{A_1}{A_2} = V_o \left[1 + \frac{N_1 L_1}{V_o} \right] K_2 = K_2 V_o (1 + X_1)$$

and the velocity entering the third circuit is:

$$V_{o3} = \frac{V_{o2}}{P_{o3}} \times \frac{A_2}{a_3} = K_2 V_o [1 + X_1] \left[1 + \frac{N_2 L_2}{K_2 V_o (1 + X_1)} \right] \times \frac{A_2}{A_3}$$

Similarly, the velocity entering the n th. circuit of n circuits in series may be written as:

$$V_{on} = K_n V_o [1 + X_1 + X_2 + \dots + X_{n-1}] \quad (27)$$

$$\text{Let } [1 + X_1 + X_2 + \dots + X_{n-1}] = \sum_1^n X_{n-1}$$

$$\therefore V_{on} = K_n V_o \left[1 + \sum_1^n X_{n-1} \right] \quad (28)$$

Loss in Static Head Due to Friction in the n th. Circuit

The general equation of friction loss in any given circuit may be written as follows from equation (13);

$$-dP = \frac{4f \times dl}{2gd} = V^2$$

In terms of the entering velocity and density of such a circuit, this expression becomes:

$$-dP = \frac{4f dl V_o^2 P_o^2 P}{2gd P^2} \quad \text{ft. of liquid at density } P_o$$

If the entering density of this circuit is taking as unity:

$$-dP = \frac{4f dl V_o^2}{2gd P}$$

The change of relative density P with respect to entering relative density P_o is

$$P_o = \frac{1}{1 + \frac{Nl}{V_o}}$$

If the n th. circuit is being considered this becomes:

$$-dP_n = \frac{4f dl V_{on}^2}{2gd_n} \left[1 + \frac{Nnl}{V_{on}} \right] \text{—density } P_{on}$$

Using the entering density of circuit 1 as reference, the final differential equation for friction loss becomes:

$$-dP_n = \left(\frac{4f dl V_{on}^2}{2gd_n} \right) \left(\frac{1}{1 + \sum_1^n X_{n-1}} \right) \left(\frac{N_n l_n}{V_{on}} \right) \quad (29)$$

Or

$$\Delta P_n = \int_0^{L_n} \left(\frac{4f dl v_{on}^2}{2gd_n} \right) \left(\frac{1}{1 + \sum_1^n X_{n-1}} \right) \left(1 + \frac{N_n l_n}{V_{on}} \right) \quad (30)$$

Note: In the above integral, the lower limit is taken as zero because it is the point of zero of the reference axis of this circuit.

Integrating yields:

$$\Delta P_n = \frac{4fV_{on}^2}{2gd_n} \left[\frac{L_n}{1 + \sum_1^n X_{n-1}} \right] \left[1 + \frac{N_n L_n}{2V_{on}} \right] \quad (31)$$

Substituting for V_{on} from (28) in (31) yields the desired equation for the static head loss due to friction in the n th. circuit.

$$\Delta P_n = \frac{4fK_n^2 L_n V_o^2}{zg d_n} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right] \quad (32)$$

Acceleration Loss for the n th. Circuit

The general equation of the acceleration loss for any circuit is:

$$-dP = \frac{V_o dv}{g} \quad (33)$$

For the n th. circuit in terms of the relative density entering the first circuit:

$$\begin{aligned} \Delta P_n &= \frac{V_{on}}{g} \int_{V_{on}}^V \frac{dv}{1 + \sum_1^n X_{n-1}} \\ \Delta P_n &= \frac{V_{on}}{g} (Y - V_{on}) \left(\frac{1}{1 + \sum_1^n X_{n-1}} \right) \\ \Delta P_n &= V_{on}^2 \left(\frac{1}{1 + \sum_1^n X_{n-1}} \right) \frac{N_n L_n}{V_{on}} \\ \Delta P_n &= \frac{V_o^2}{2g} K_n^2 \times 2X_n \end{aligned} \quad (34)$$

Entrance and Exit Loss for the n th. Circuit

$$\Delta P = 1.5 \frac{V_o^2}{2g} \quad \text{For any circuit} \quad (35)$$

$$\begin{aligned} \Delta P_n &= \frac{V_{on}^2 (1.5)}{2g (1 + \sum_{i=1}^n X_{i-1})} \\ \Delta P_n &= \frac{1.5 V_o^2 K_n^2}{2g} \left(1 + \sum_1^n X_{n-1} \right) \end{aligned} \quad (36)$$

Bend Loss at Any Point in the Circuit

The bend loss in velocity heads of liquid flowing at the entrance to the bend can be obtained from Fig. 6. If the bend exists at some point in the n th circuit, the loss can be written in terms of the density entering the first circuit as follows:

$$V = K_n V_o \left(1 + \sum_{i=1}^n X_{i-1} + \alpha X_n \right) \quad (37)$$

$$\Delta P = \frac{K_B \left[K_n^2 V_o^2 \left(1 + \sum_{i=1}^n X_{i-1} + \alpha X_n \right)^2 \right]}{2g}$$

$$\Delta P_n = \frac{K_B K_n^2 V_o^2 \left(1 + \sum_{i=1}^n X_{i-1} + \alpha X_n \right)}{2g} \quad (38)$$

Where α equals the ratio of length of tube in the n th. circuit to the bend, to the total length of the n th. circuit.

Gravity Head of the n th. Circuit

$$-dH = P dl \quad (39)$$

The relative density at any point in a circuit with respect to the density entering the circuit is:

$$P = \frac{1}{1 + \frac{Nl}{V_o}}$$

For the n th. circuit in terms of the relative density entering the first circuit, the Gravity Head expression becomes:

$$\begin{aligned} \Delta H_n &= \int_0^{L_n} \frac{dl}{1 + \frac{N_n l}{V_{on}}} \\ \Delta H_n &= \frac{V_{on} N_n \log_e \left[1 + \frac{N_n L_n}{V_{on}} \right]}{\left(1 + \sum_{i=1}^n X_{i-1} \right)} \\ \text{Gravity Head} = \Delta H_n &= \frac{L_n}{X_n} \log_e \left[1 + \frac{X_n}{1 + \sum_{i=1}^n X_{i-1}} \right] \end{aligned} \quad (40)$$

If a circuit makes an angle θ with the horizontal, the above expression must be multiplied by $\sin \theta$.

If $X_n \rightarrow 0$, the expression for the Gravity head becomes of the form $\frac{0}{0}$, which is indeterminate. In the limit:

$$\begin{aligned}
X_n &\rightarrow O_1 \frac{L_n \sin \theta \log_e \left[1 + \frac{X_n}{1 + \sum_{i=1}^n X_{i-1}} \right]}{X_n} \\
X_n &\rightarrow O_1 \frac{\frac{d}{dX_n} \left(L_n \sin \theta \log_e \left[1 + \frac{X_n}{1 + \sum_{i=1}^n X_{i-1}} \right] \right)}{\frac{d}{dX_n} (X_n)} \\
&= L_n \sin \theta \left(\frac{1}{1 + \frac{X_n}{1 + \sum_{i=1}^n X_{i-1}}} \right) \left(\frac{1}{1 + \sum_{i=1}^n X_{i-1}} \right)
\end{aligned} \tag{41}$$

Setting $X_n = 0$ in this yields (41).

Vapor Fraction by Weight Leaving with n th circuit

If the vapor fraction by weight of any circuit is λ , then the ratio of specific volume of the mixture at any point in the circuit to the specific volume is:

$$\begin{aligned}
\frac{\$}{\$_{\text{entering}}} &= 1 + \frac{NI}{V_o} = \frac{\lambda S + (1 - \lambda)s}{s} = 1 + \frac{\lambda}{s}(S - s) \\
\lambda &= \frac{NI}{V_o} \times \frac{s}{S - s}
\end{aligned} \tag{42}$$

For the n th. circuit and compensating to the entering density of the first circuit:

$$\begin{aligned}
\lambda_n &= \frac{\left[\sum_{i=1}^n \frac{N_i L_i}{V_{oi}} \right]}{\left[\frac{1}{1 + \sum_{i=1}^n X_{i-1}} \right]} \times \frac{s}{S - s} \\
\lambda_n &= \frac{s}{S - s} \frac{\left[\frac{\sum_{i=1}^n X_n}{1 + \sum_{i=1}^n X_{i-1}} \right]}{\left[\frac{1}{1 + \sum_{i=1}^n X_{i-1}} \right]} \\
\lambda_n &= \frac{s}{S - s} \left[\sum_{i=1}^n X_n \right]
\end{aligned} \tag{43}$$

Vapor Fraction by Volume Leaving n th. Circuit

The ratio of vapor by volume to vapor fraction by weight is:

$$\frac{\frac{B}{\lambda}}{\frac{\frac{s}{s-s} \left(\frac{NI}{V_o} \right)}{1 + \frac{NI}{V_o}}} \frac{s}{S - s} \times \frac{NI}{V_o}$$

for the n th. circuit:

$$B_n = \frac{\frac{S}{S-s} [\sum_{i=1}^n X_n]}{[1 + \sum_{i=1}^n X_n]} \quad (44)$$

The equations developed in this section for Series Circuits enable the computation and prediction of the circulation in any circuit regardless of the number of circuits for Gravity Head or Friction. It is obvious, however, that if there are many such circuits, as is usually the case in a boiler, the entire process becomes tedious and involved. For this purpose, the curves developed for simple circuits may be used.

The sum of the losses in the n th. circuit can be written as follows if K_B is taken as 0.3 and f equal to 0.006.

$$\Sigma \Delta P_n = K_n^2 \frac{V_o^2}{2g} \left[.288 \frac{L_n}{d_n} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right] + 2X_n + 1.8 \left[1 + \sum_1^n X_{n-1} \right] \right] \quad (45)$$

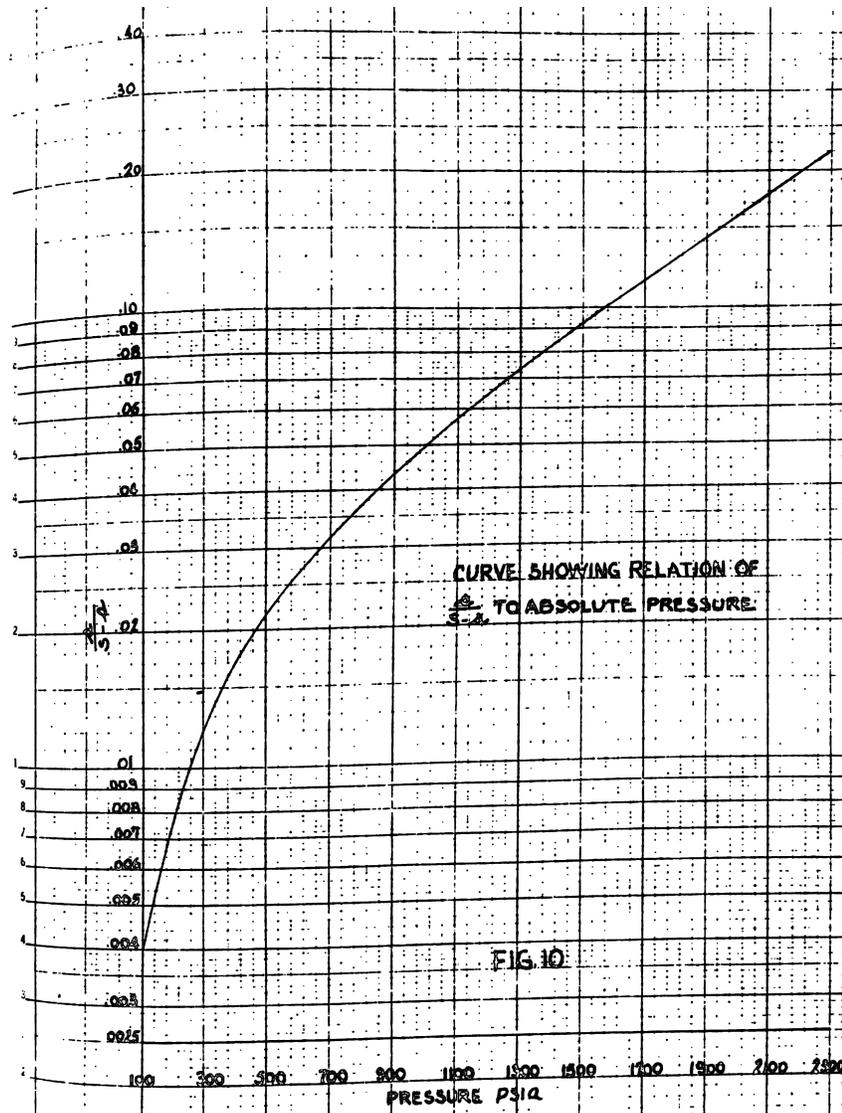
Comparison of the above expression with equation (26) shows that when $\sum_n^1 X_{n-1} = 0$, the two expressions are equivalent. Therefore, to evaluate the total static head loss for the n th. circuit, the value of ΔP is read from the proper curve at the corresponding value of n , and the value of ΔP at $n = 1$ is multiplied by the value of X . The sum of these values is the total static head loss for the n th. circuit.

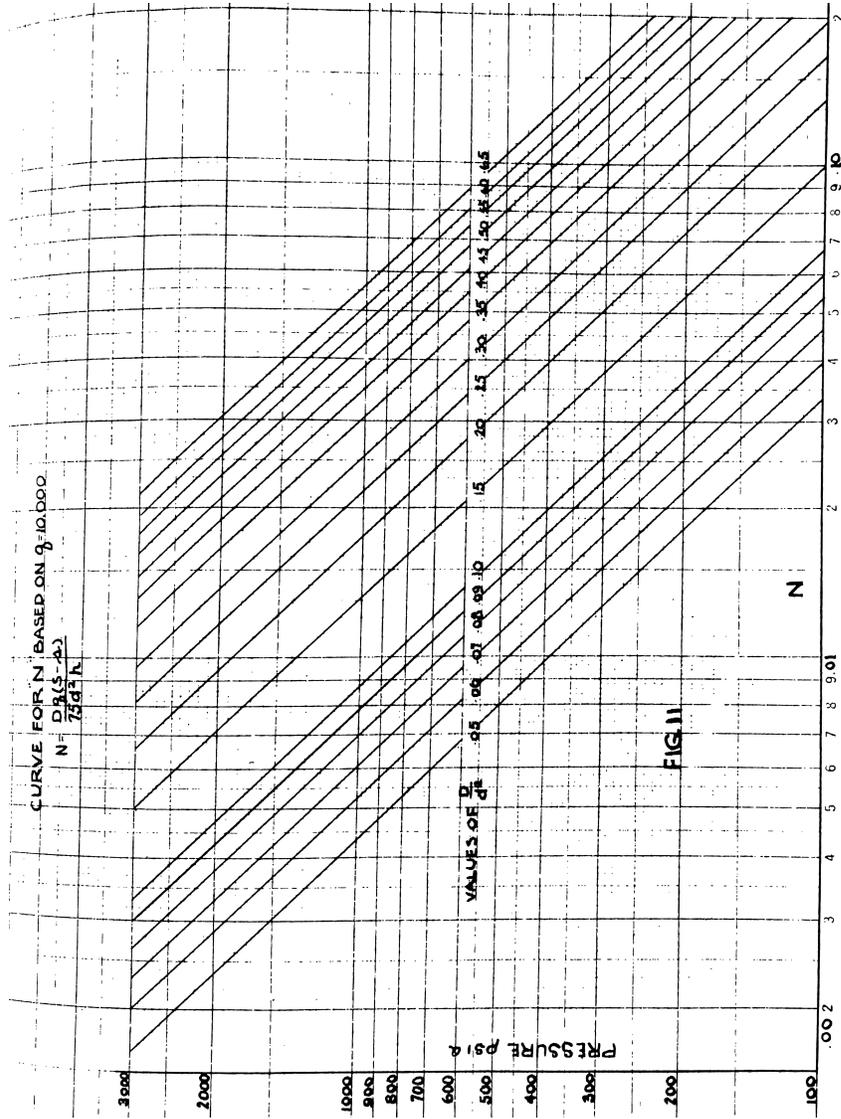
A graphical solution for the Gravity Head of the n th. circuit is given in Fig. 14. Thus, at a given value of total head required, it can readily be evaluated.

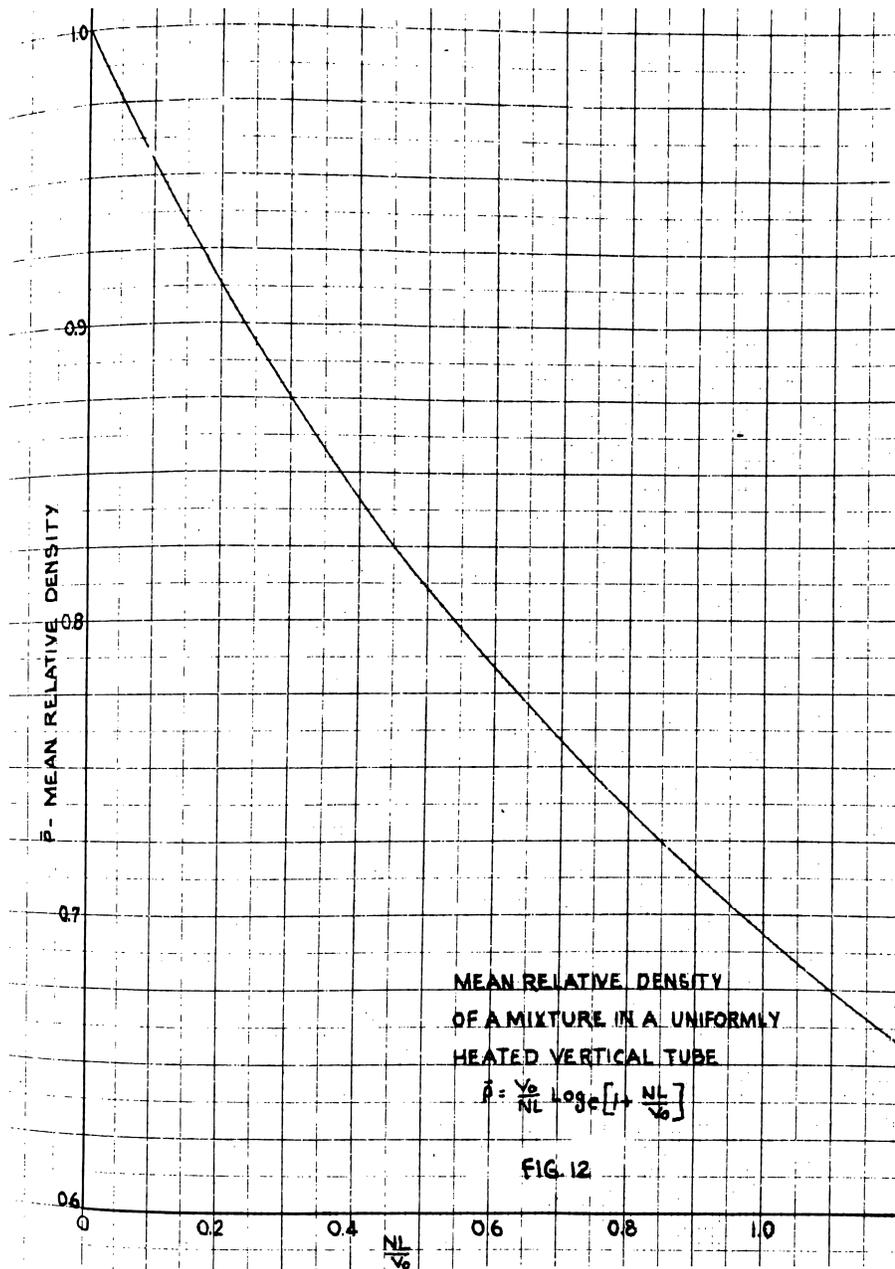
Should the entering liquid of the first circuit be subcooled or contain any steam, the computations can still be made on the basis of the equations for series circuits by the introduction of a fictitious circuit before the first circuit. This concept and its use presents no difficulties.

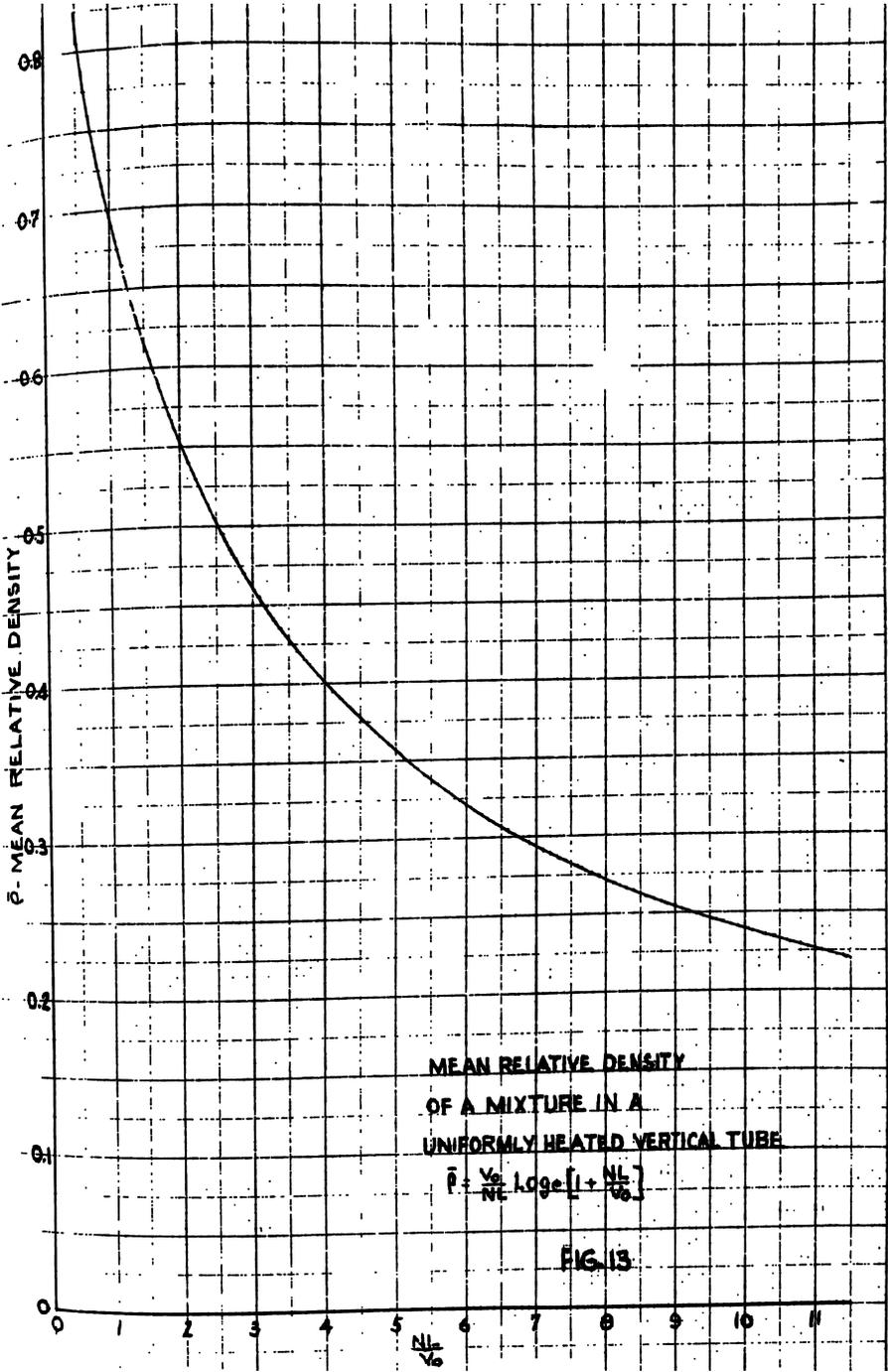
The next section gives all of the computations for the prediction of the circulation in a large boiler utilizing all the curves and equations developed so far. The method used is similar to that used in Hydraulics.⁽⁴⁹⁾ It consists essentially of evaluating equation (46):

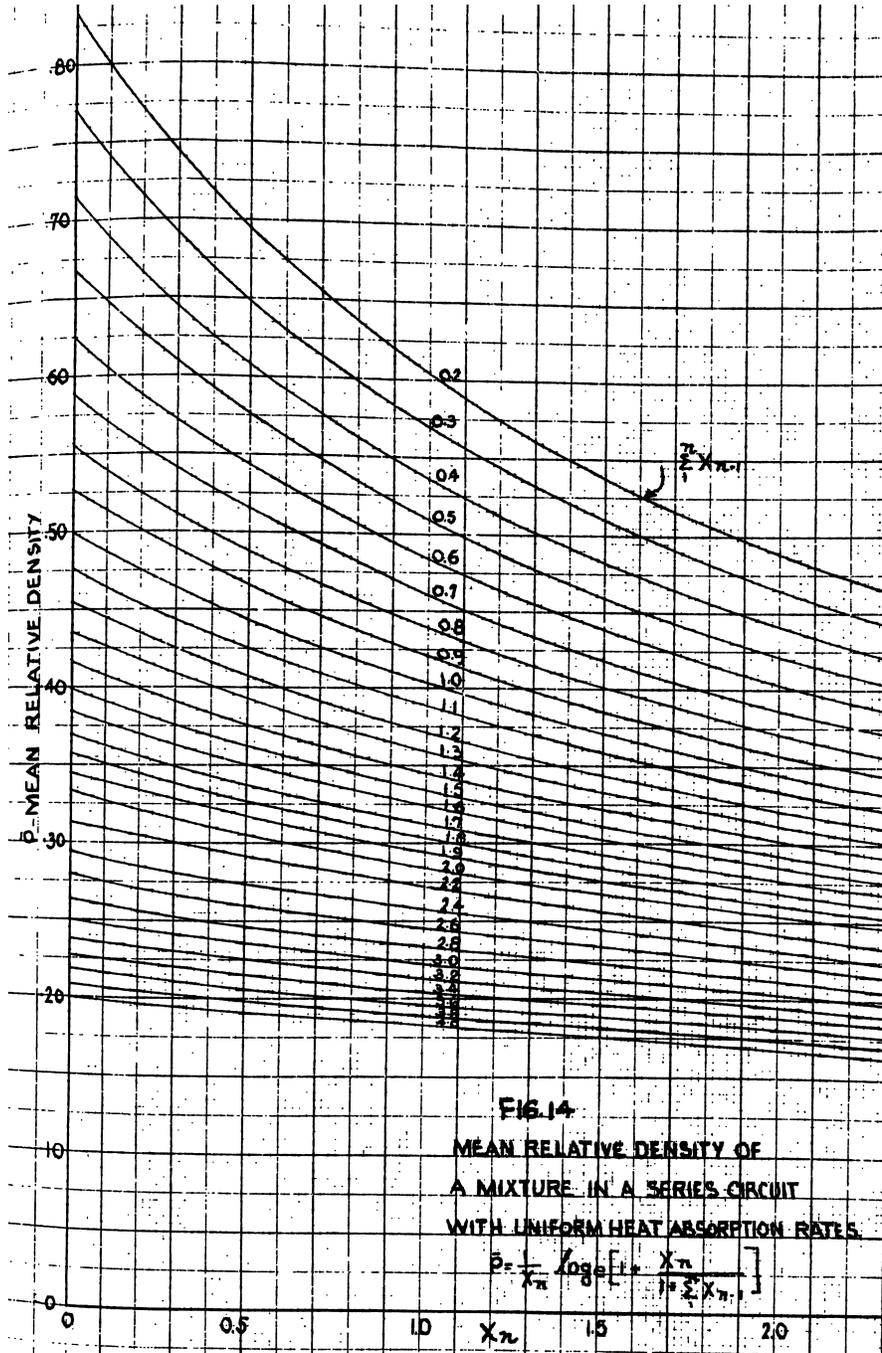
$$\text{Head available} - \text{Downcomer losses} = \text{Gravity Head} + \sum \text{Riser}_{\text{losses}} \quad (46)$$

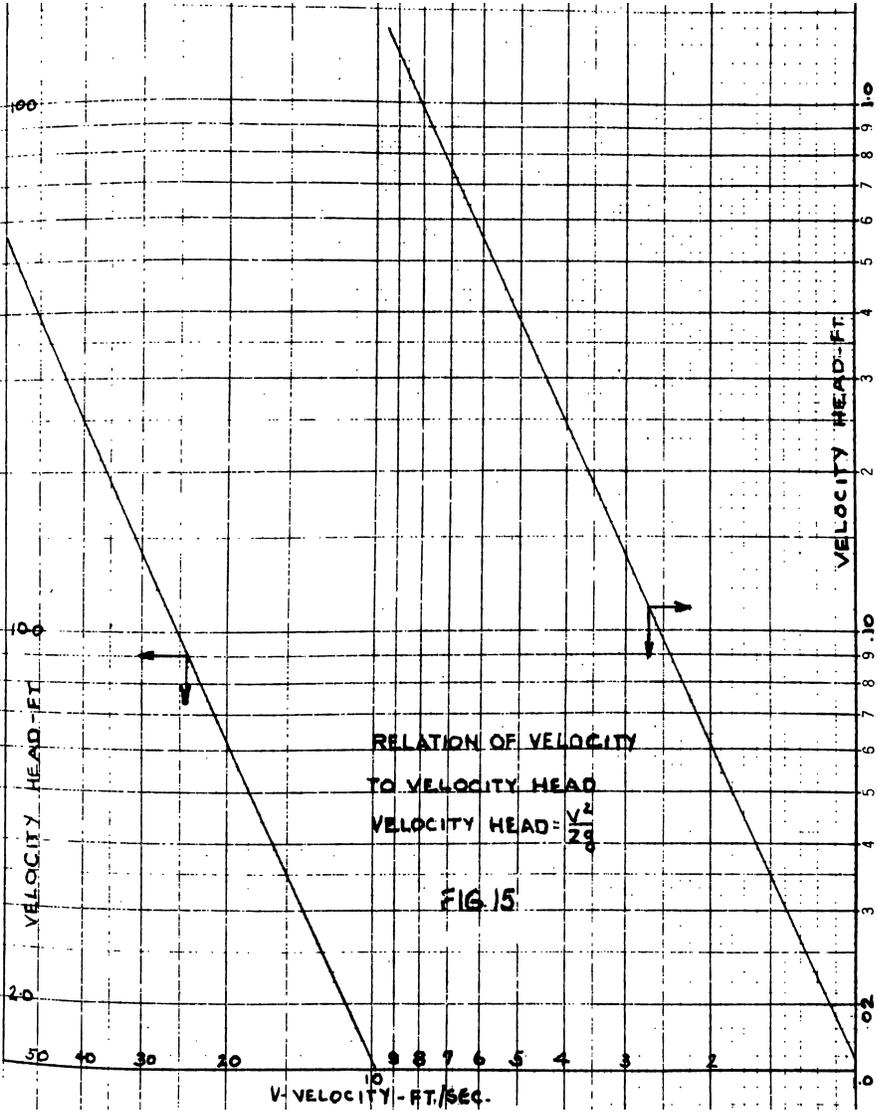


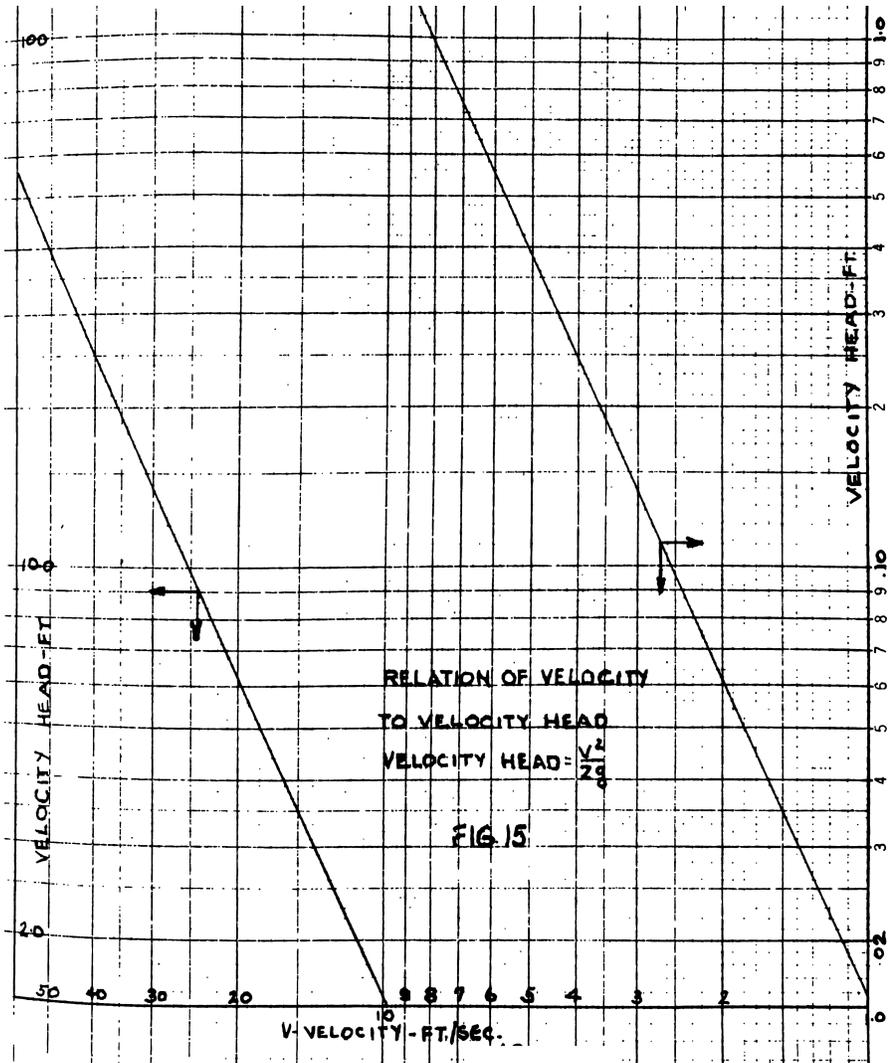


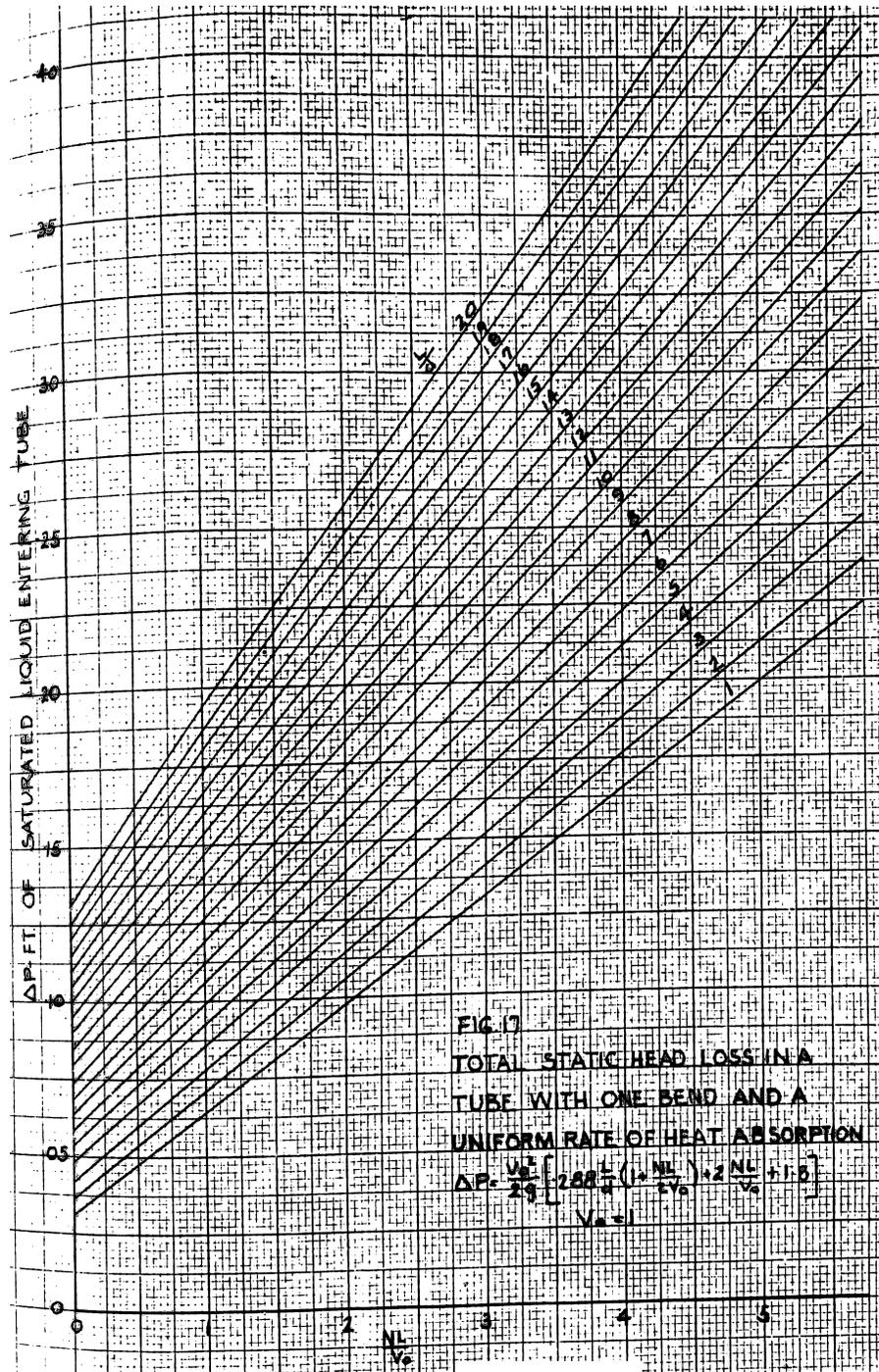


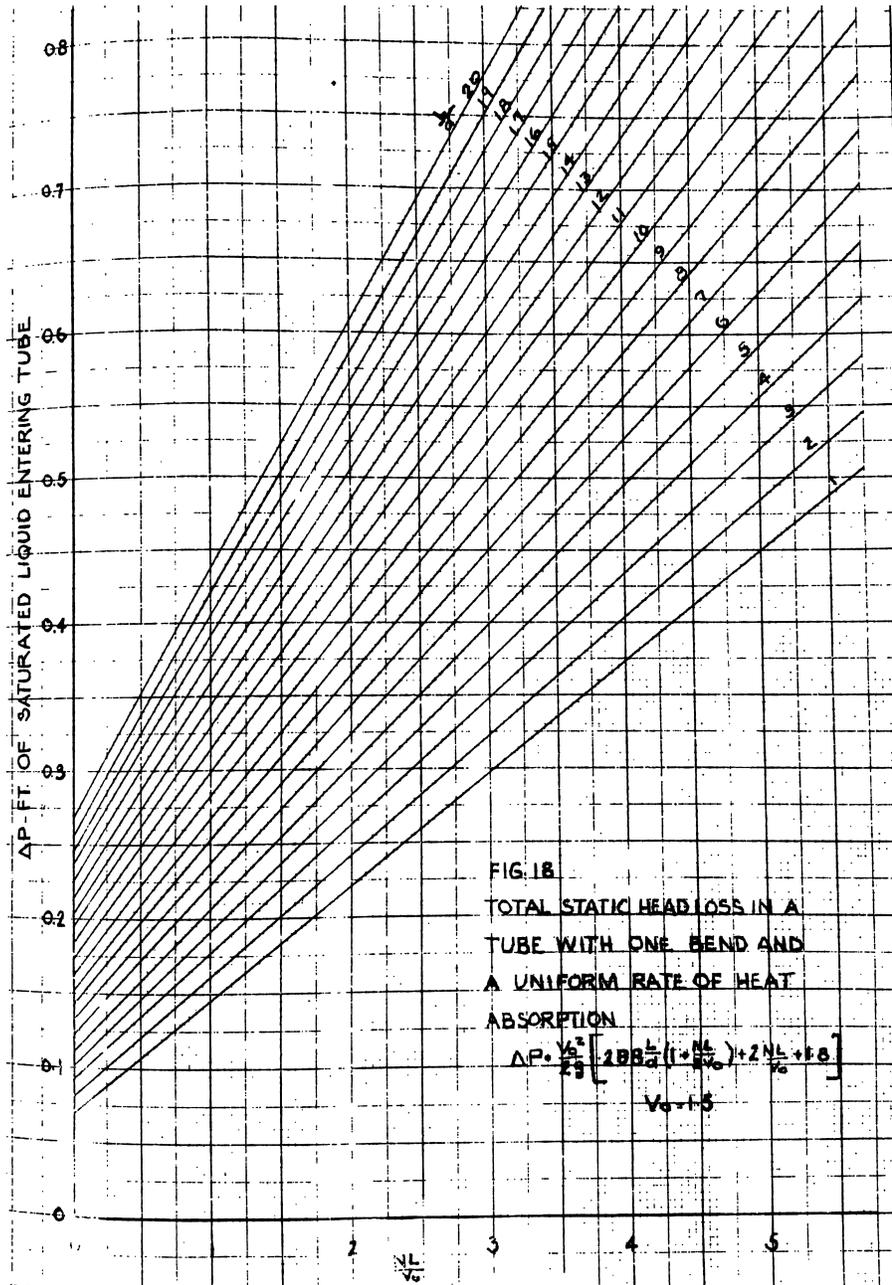


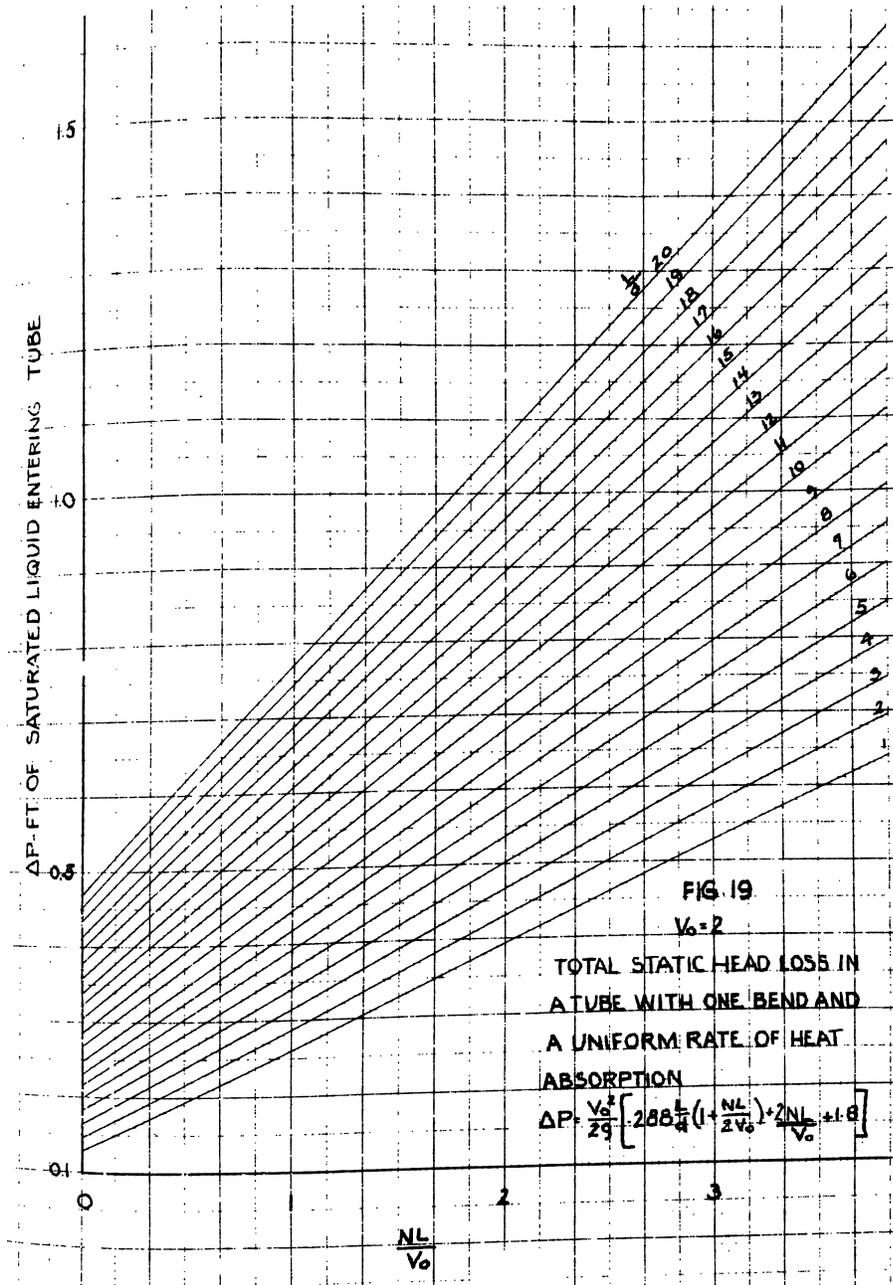


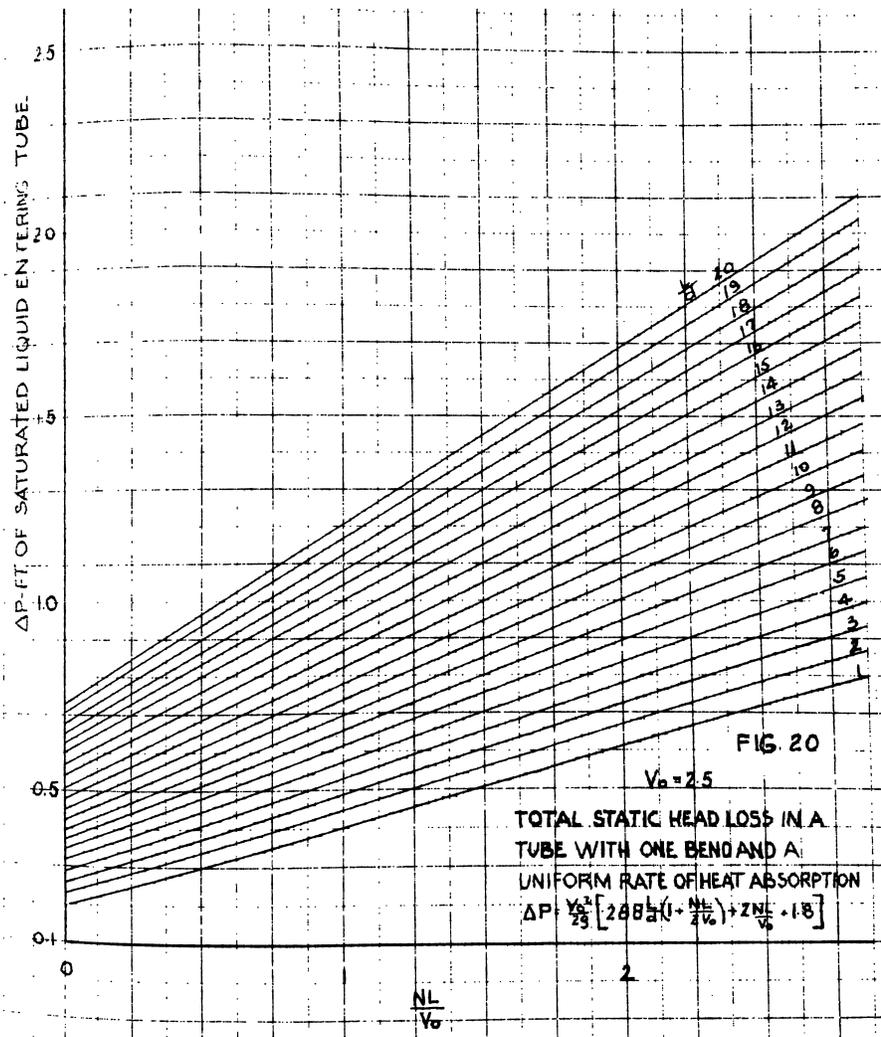


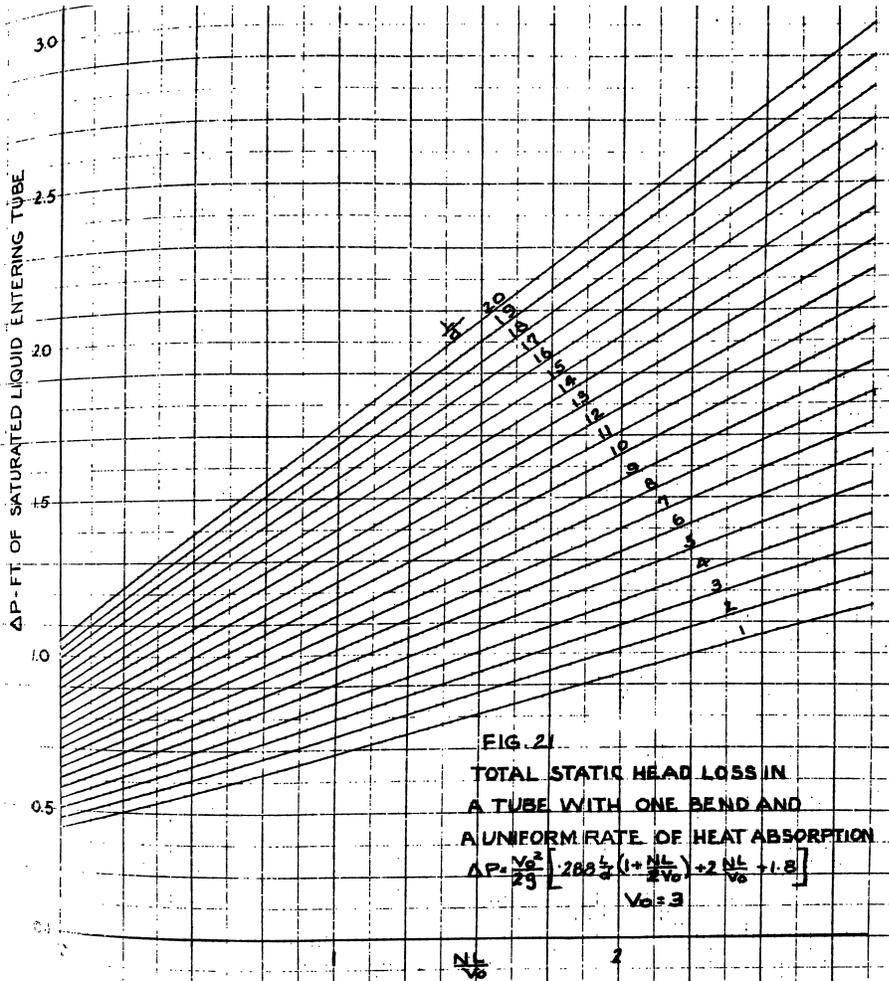


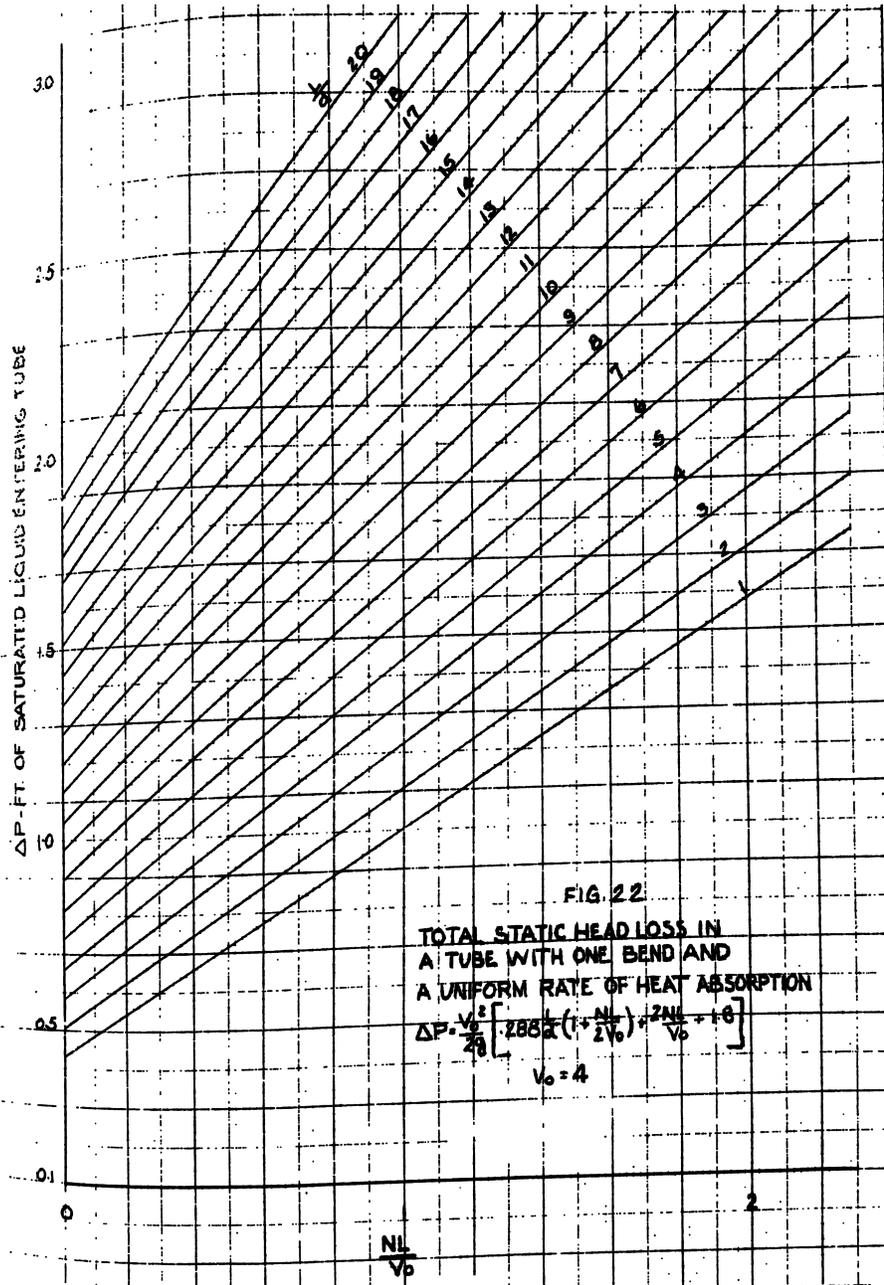










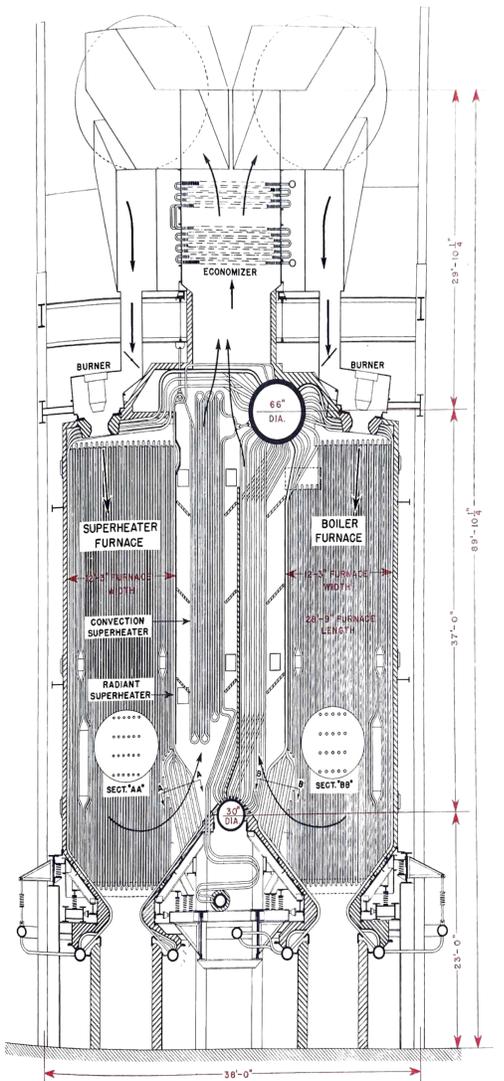


III *The Prediction of Circulation in a Large Boiler Installation*

The unit chosen for this section is the Twin Furnace Installation of the Duquesne Light Company's Frank R. Phillips station, Pittsburgh, Pa. This unit was chosen for two reasons: the computations involved are such that they bring out all of the problems likely to be encountered in predicting the circulation in any large unit, and secondly, through the courtesy and cooperation of the Foster Wheeler Corporation test data taken on this unit has been made available for comparison with predicted results.

The papers by John Blizard & A. C. Foster,⁽³⁰⁾ and Martin Frisch⁽⁵⁸⁾ give excellent descriptions of this type of steam generator and the reasons for its design. However, a brief description of this unit will be given along with all the pertinent data necessary for the computations.

Fig. 23 shows a vertical section taken looking to the rear of the installation. This illustration is used with the kind permission of the Foster Wheeler Corporation. The unit consists of a separately fired superheater furnace and a separately fired boiler furnace. The superheater furnace has both a radiant and convection superheater so arranged as to give almost constant final steam temperature over the greater part of the load range of the unit. In addition, both furnaces are designed to fire pulverized coal from the top, and the rate of firing is closely equal for both furnaces at full load. Final steam temperature is controlled by varying the rate of firing in both furnaces.



DUQUESNE LIGHT CO., FRANK R. PHILLIPS
STATION, PITTSBURGH, PA. PMD-624-J
56-900-1
1-668

Table 2 gives the downcomer, feeder, and water wall data for this unit as given in Mr. R. A. Lorenzini's circulation report,⁽²⁵⁾ while Table 3 shows the performance data for a steam output of 387,500 lbs. *per hr.* Though the design maximum load is 500,000 lbs. *per hr.*, the maximum load reported in the tests was 357,500 lbs. *per hour*, and the circulation characteristics will be predicted for this load. All the data in Table 3 are actual test data except those marked with an asterisk (*), which were calculated by the author from the test data, and the expected performance characteristics of this unit.

Fig. 24 is from Mr. Lorenzini's report and shows a plan view of the water wall feeders and also the location of the pressure taps used in the tests. During these tests, the density of the water flowing in the downcomers was measured utilizing the pressure drop method.⁽⁶⁹⁾ As far as could be determined within the limit of the accuracy of the instruments used, the water in the downcomers was essentially saturated and contained no entrained steam. For the calculations of this unit, it will therefore be assumed that the water in the downcomers is at saturation conditions and contains no steam.

This particular unit is fired from the top and the length of the flame is relatively short.⁽⁵⁸⁾ Therefore, it would be expected that the rate of heat absorption near the top of the tubes is very much greater than the rate of heat absorption near the bottom of the tubes. From Fig. 23, it is also apparent that the furnace gases can enter the screen bank without passing the tubes that constitute the ash hopper. The ash in this hopper section will also tend to further insulate the tubes in this section of the furnace. For the reasons just cited, the following assumptions regarding what will be considered as a reasonable distribution of heat absorption in this unit will be made:

1. The rate of heat absorption in the upper third of the heated area is twice that of the lower two-thirds area.
2. 50% of the total heat absorption occurs in the upper third of the heated area.
3. The length of the tube in the hopper section is essentially unheated, and heating is assumed to start at the top of the hopper line.
4. In all the heated wall sections, the heat absorption is uniform. As noted above, while the heat absorption is uniform in all the heated sections, the sections do not have equal rates of absorption.

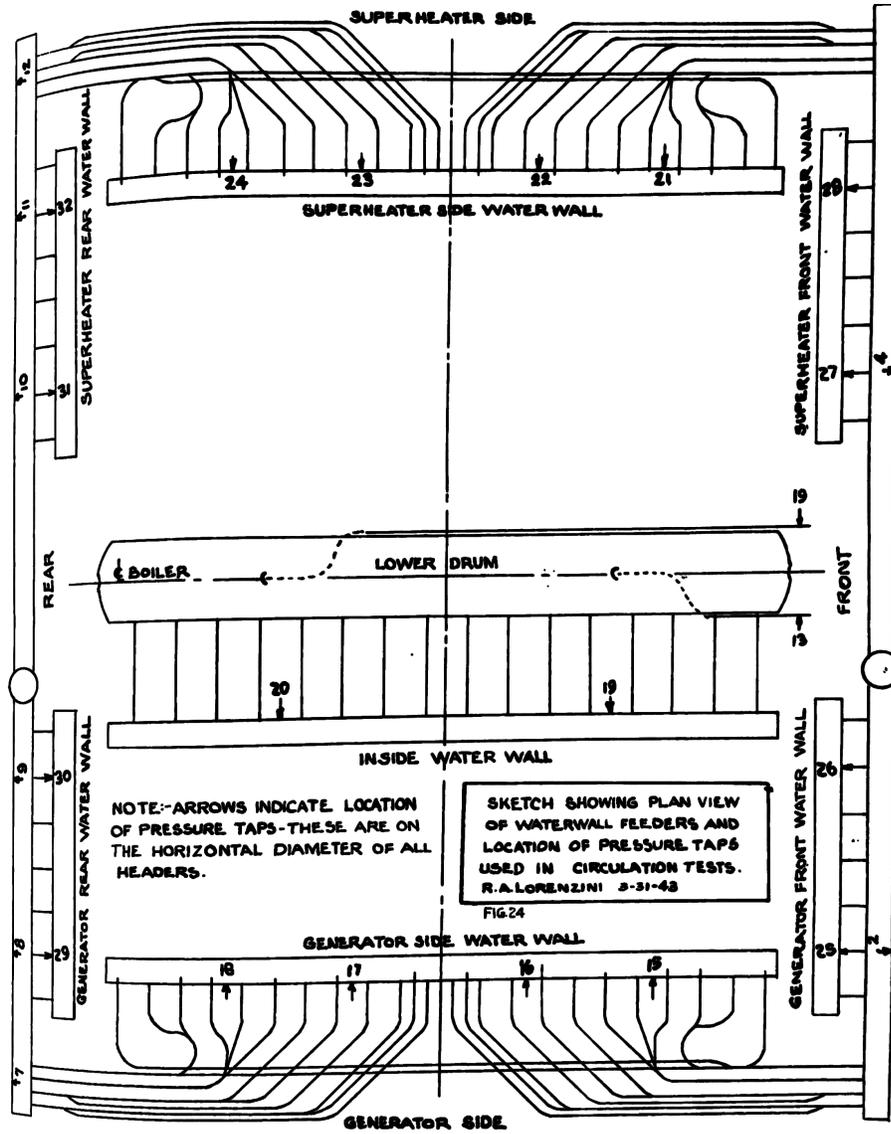


Table 2: Downcomer, Feeder, and Wall Data

Designation	Number	O.D. In.	I.D. In.	Total Area Sq.Ft.	Ratio-Feeder To Wall Area
GEN. FRONT	45	3	2.52	1.558	.1556
SUP. FRONT	45	3	2.52	1.558	.1556
GEN REAR	45	3	2.52	1.558	.1556
SUP. REAR	103	3	2.52	1.558	.1556
GEN. SIDE	103	3	2.52	3.566	.2333
INSIDE WALL	103	3	2.52	3.566	.1553
BOILER BANK	402	2	1.70	6.337	—
Location					
Front	1	16	13.5	.994	
Rear	1	16	13.5	.994	
Inside	2	10.75	8.75	.835	
FRONT	14	3	2.52	.485	
REAR	14	3	2.52	.485	
RIGHT SIDE	24	3	.832		
LEFT SIDE	24	3	2.52	.832	
INSIDE	16	3	2.52	.554	

Table 3: Circulation Test (3-31-43)

Test	1
DATE	3-15-43
TIME	3:00 PM
CORRECTED STEAM FLOW LBS./HR.	387,500
DRUM PRESSURE psig	928
PRESSURE-SUPERHEATER OUTLET psig	900
FINAL STEAM TEMPERATURE F.	894
TEMP. WATER ENT. ECON. F.	394
TEMP. WATER LVG. ECON. F.	488
GAS TEMP. LVG. BOILER	982
*FUEL BURNED LBS/HR	37,600
*WET GAS AT BOILER EXIT LBS/HR	462,000
*TEMP. AIR ENT. UNIT F.	80
*TEMP. AIR GAS LVG. AIR HEATER F.	505
*TEMP. GAS LVG. FURNACE F.	1880
*FUEL	Bituminous-12,900 Btu/lb. as fired
#TOTAL FURNACE VOLUME CU.FT.	27,000

From the data given in Table 3, the total heat absorbed in both furnaces can readily be determined.

Heat content in gases as fired in furnace: 1093 Btu/lb. of gas

Heat content in gases leaving furnace at 1880°F: 515 Btu/lb. of gas

Heat absorbed in furnace: 578 Btu/lb. of gas

Total furnace heat absorption: $462,000 \times 578 = 267,000,000$ Btu/hr.

The projected area of each wall is given below for both furnaces:

Generating side wall	$\frac{1}{4} \times 103 \times 37.3$	= 961
Generating front and rear walls	$2 \times \frac{1}{4} \times 4.5 \times 387$	= 871
Superheater side wall	$\frac{1}{4} \times 103 \times 37.3$	= 961
Superheater front and rear walls	$2 \times \frac{1}{4} \times 4.5 \times 38.7$	= 871
Inside wall	$\frac{1}{4} \times 103 \times 39.25$	= 1012
Radiant wall (assumed same as inside wall)		= 5688 sq.ft.
absorption <i>per</i> sq.ft. of total wall area	$q = \frac{267,000,000}{\pi \times 5688}$	= 14,950
$D = 3.00$	$N = \frac{Dq(S-s)}{75d^2h}$	
$q = 14,950$	$N = \frac{3.00 \times 14,950 \times (.4543)}{75 \times (2.52)^2 \times 660.5}$	
$S = .4757$	$N = 0.646$	
$s = .0214$		
$h = 660.5$	$d = 2.52$	

From Fig. 11, at $\frac{D}{d^2} .473$, and a pressure of 942.7 psia,

$$N = 0.43 \text{ for a } q \text{ of } 10,000$$

$$N = 1.495 \times 0.43 \approx 0.643$$

It is apparent that using the curves of Fig. 11 eliminates the necessity of looking up the necessary thermodynamic properties and interpolating in the Steam Tables. In this case, the error incurred by using this graph is on the order of 0.46.

For the upper heated sections, on the basis of the heat absorption distribution made:

$$N = 1.5 \times 0.646 \approx 0.97$$

and for the lower heated section:

$$N = \frac{1}{2} \times 0.97 = 0.485$$

On the following pages, a sketch of each wall being computed is shown and the necessary computations are made using the equations and also the curves developed in Section II of this work. These computations are mostly self-explanatory and are

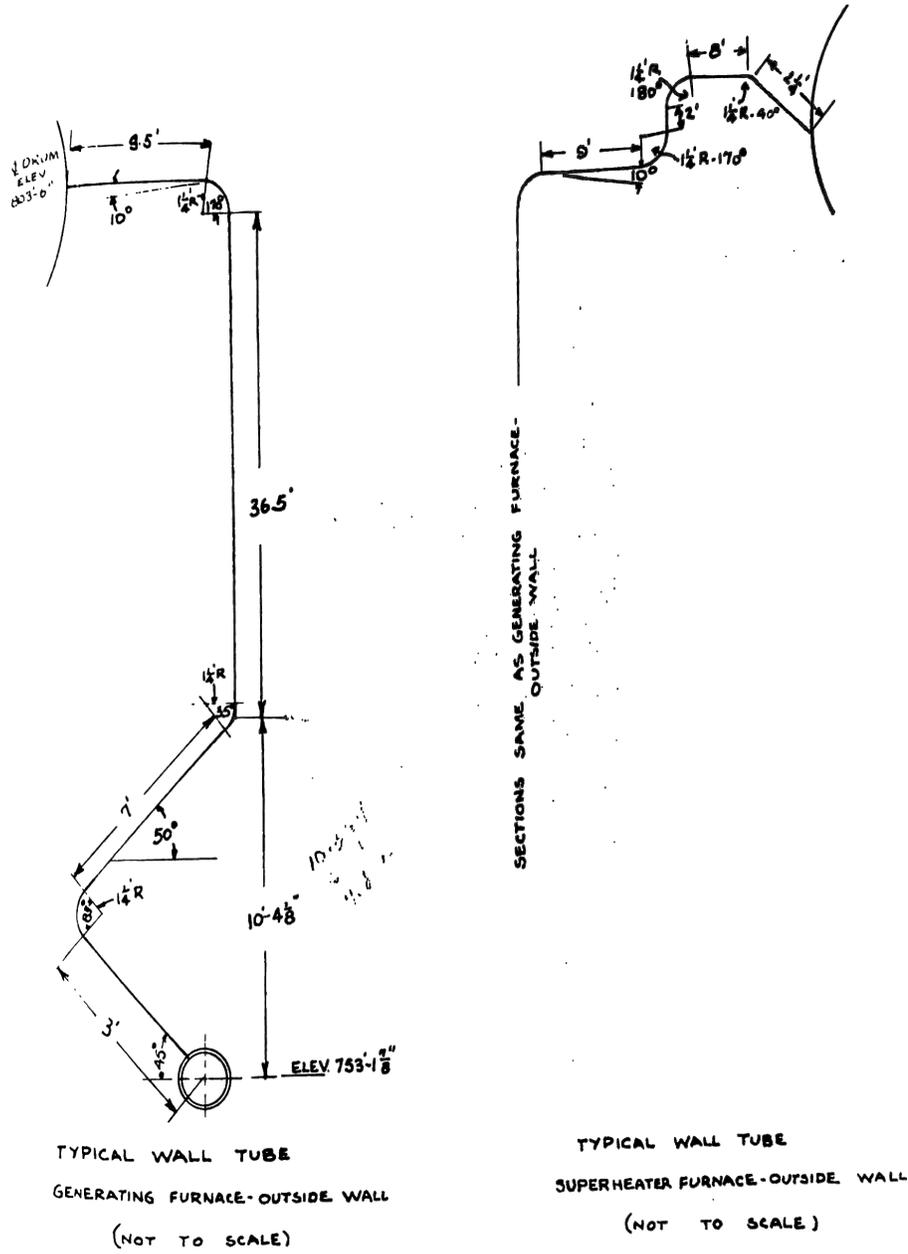
readily followed by referring to the typical wall sketches and to the equations for the effect being computed. It must be fully understood that these computations are subject to all the inherent assumptions made in the derivation of the equations in Section II. Therefore, these computations were done on a slide rule and it is important to understand that further accuracy is not justified.

**Calculation of Entrance & Exit,
Bend and Friction Loss Coefficients in Feeders**

Feeder Number	Bends Deg.	Bend Loss Coeff	Total	Dev length Ft.
450-451	45-90-90-12.5-12.5	.21-.3-.3-.075-.075	1.0	35.07
452-453	90-180-90	.3-.4-.3	1.0	16.02
454-455	45-135-45-45	.21-.36-.21-.21	1.0	13.87
456-457	90-12.5-12.5-90-45	.3-.075-.075-.3-.21	1.0	15.30
458-459	90-60-30	.3-.24-.15	0.7	15.34
460-461	45-45-45-45	.21-.21-.21-.21	0.8	15.32
462-463	90-45-45	.3-.21-.21	0.7	17.73
464-465	45-45-90-45	.21-.21-.3-.21	0.9	19.17
466-467	45-12.5-12.5-45-45	.21-.075-.075-.21-.21	0.8	19.37
468-469	90-45-45	.3-.21-.21	0.7	22.01
470-471	45-45-90-45	.21-.21-.3-.21	0.9	22.64
472-473	12.5-12.5-45-45-45	.075-.075-.21-.21-.21	0.8	22.03
474	90	.4	0.4	4.48
475	90-70-50	.3-.26-.23	0.8	15.5

Feeder Number	Ent. Loss Coeff.	Exit Loss Coeff.	Bend Loss Coeff.	Fric. Loss Coeff.	Total Loss Coeff.
450-451	.5	1.0	1.0	3.34	5.84
452-453	.5	1.0	1.0	1.53	4.03
454-455	.5	1.0	1.0	1.32	3.82
456-457	.5	1.0	1.0	1.46	3.96
458-459	.5	1.0	0.7	1.46	3.66
460-461	.5	1.0	0.8	1.46	3.76
462-463	.5	1.0	0.7	1.69	3.89
464-465	.5	1.0	0.9	1.83	4.23
466-467	.5	1.0	0.8	1.85	4.15
468-469	.5	1.0	0.7	2.10	4.30
470-471	.5	1.0	0.9	2.26	4.66
472-473	.5	1.0	0.8	2.10	4.40
450-473	(Side Wall Feeders)			Average Total Loss Coeff.	4.23
474	(Front & Side Wall Feeders)			Average Total Loss Coeff.	2.71
475	(Inside Wall Feeders)			Average Total Loss Coeff.	3.78

The calculations above refer to the un-numbered feeders shown in Fig. 24.



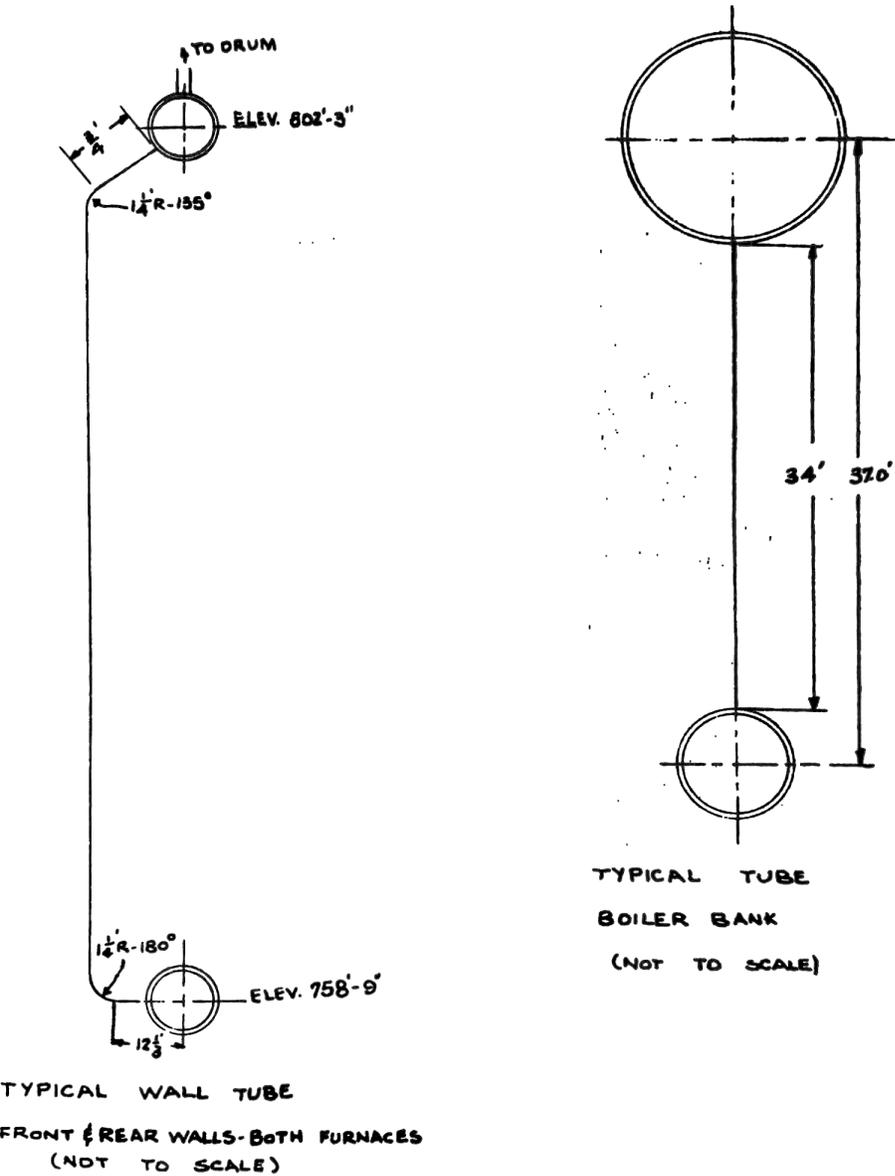


FIG. 26

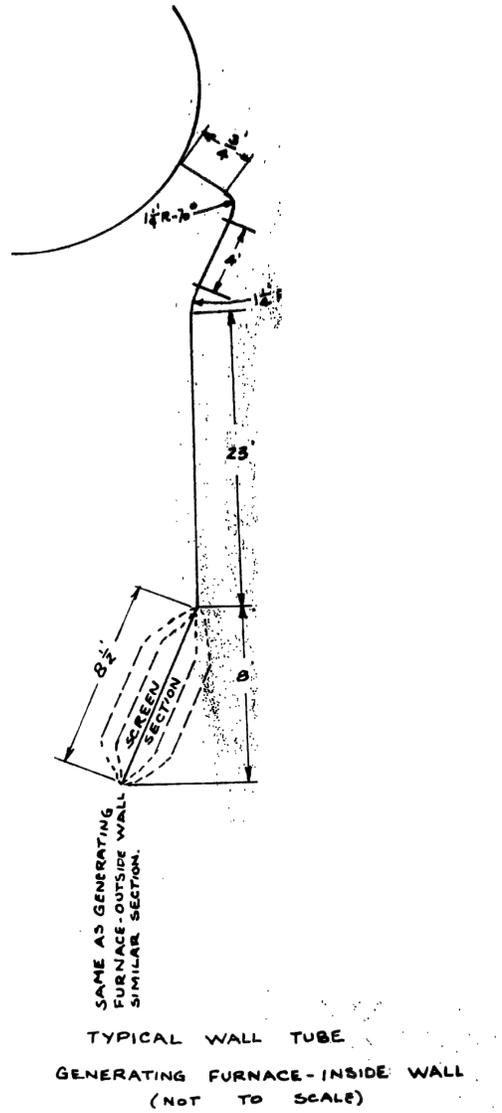


FIG. 27

Generating Furnace: Outside Wall

(Refer to Fig. 25)

Gravity Head:

Circuit 1 10.34

Circuit 2 $\frac{L_n}{X_n} \log_e(1 + X_n)$

V_0	X_n	$1 + X_n$	Gravity Head
0.5	2.42	3.42	12.70
1.0	1.21	2.21	16.40
1.5	0.806	1.806	18.30
2.0	0.605	1.605	19.51

Circuit 3 $\frac{L_n}{X_n} \log_e \left[1 + \frac{X_n}{1 + \sum_1^n X_{n-1}} \right]$

V_0	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	X_n	$\frac{X_n}{1 + \sum_1^n X_{n-1}}$	$\frac{X_n}{1 + \frac{X_n}{1 + \sum_1^n X_{n-1}}}$	Gravity Head
0.5	2.42	3.42	2.230	0.653	1.653	2.59
1.0	1.21	2.21	1.115	0.504	1.504	4.20
1.5	0.806	1.806	0.743	0.412	1.412	5.34
2.0	0.605	1.605	0.557	0.347	1.347	6.14

Circuit 4 $\frac{L_n \sin \theta}{1 + \sum_1^n X_{n-1}}$

V_0	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	Gravity Head
0.5	4.65	5.65	0.62
1.0	2.325	3.325	1.05
1.5	1.55	2.55	1.37
2.0	1.162	2.162	1.62

Losses: Acceleration

Circuit 1 0

Circuit 2 $\frac{V_0^2}{2g} \times 2X_n$

Generating Furnace: Outside Wall (cont.)

V_0	$\frac{V_0^2}{2g}$	$\frac{V_0^2}{2g}$	X_n	$2X_n$	Acceleration Loss
0.5	0.25	0.0039	2.42	4.84	0.019
1.0	1.00	0.0155	1.21	2.42	0.038
1.5	2.25	0.035	0.806	1.612	0.056
2.0	4.00	0.062	0.605	1.21	0.075

Circuit 3 $\frac{V_0^2}{2g} \times 2X_n$

V_0	$\frac{V_0^2}{2g}$	$\frac{V_0^2}{2g}$	X_n	$2X_n$	Acceleration Loss
0.5	0.25	0.0039	2.23	4.46	0.017
1.0	1.00	0.0155	1.115	2.23	0.035
1.5	2.25	0.035	0.743	1.486	0.052
2.0	4.00	0.062	0.557	1.115	0.069

Circuit 4 0**Entrance and Exit Loss** $1.5 \frac{V_0^2}{2g}$

V_0	$\frac{V_0^2}{2g}$	Entrance and Exit Loss
0.5	0.0039	0.006
1.0	0.0155	0.023
1.5	0.035	0.053
2.0	0.062	0.093

Bend Loss**Circuit 1-2 Bends**

$$K_{B_1} = 0.3$$

$$K_{B_2} = 0.18$$

$$\Sigma K_B = 0.48$$

$$\text{Bend Loss} = K_B \frac{V_0^2}{2g}$$

Generating Furnace: Outside Wall (cont.)

V_o	$\frac{V_o^2}{2g}$	Bend Loss
0.5	0.0039	0.002
1.0	0.0155	0.008
1.5	0.035	0.017
2.0	0.062	0.030

Circuit 2 0

Circuit 3 0

Circuit 4 1 bend

$$K_B = 0.39 ; K_B \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$$

V_o	$\frac{V_o^2}{2g}$	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	Bend Loss
0.5	0.0039	4.65	5.65	0.009
1.0	0.0155	2.325	3.325	0.020
1.5	0.035	1.55	2.55	0.035
2.0	0.062	1.162	2.162	0.052

Friction Loss

Circuit 1 $\frac{.288L}{d} \frac{V_o^2}{2g}$

V_o	$\frac{V_o^2}{2g}$	$.288 \frac{V_o^2}{2g}$	$\frac{L}{D}$	Friction Loss
0.5	0.0039	0.001125	5.02	0.006
1.0	0.0155	0.00447	5.02	0.022
1.5	0.035	0.0101	5.02	0.050
2.0	0.062	0.01785	5.02	0.090

Circuit 2 $.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} \right]$

Superheater Furnace: Outside Wall

Refer to Fig. 25

All values of Gravity Head and Losses for this wall are essentially the same as in corresponding sections of the **Generating Furnace: Outside Wall** with the exception of the bend loss and friction loss in the last section.

Bend Loss Circuit 4 4 bends

$$K_{B_1} = 0.39$$

$$K_{B_2} = 0.39$$

$$K_{B_3} = 0.39$$

$$K_{B_4} = 0.20$$

$$\sum K_B = 1.37$$

$$K_B \frac{V_o^2}{2g} \left[1 + \sum_1^n X_{n-1} \right]$$

V_o	$\frac{V_o^2}{2g}$	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	Bend Loss
0.5	0.0039	4.65	5.65	0.030
1.0	0.0155	2.325	3.325	0.071
1.5	0.035	1.55	2.55	0.122
2.0	0.062	1.162	2.162	0.84

Friction Loss

Circuit 4 $.288 \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$

V_o	$.288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	$1 + \sum_1^n X_{n-1}$	Friction Loss
0.5	0.001125	11.7	5.65	0.075
1.0	0.00447	11.7	3.325	0.174
1.5	0.0101	11.7	2.55	0.302
2.0	0.01785	11.7	2.162	0.453

Front and Rear Walls: Both Furnaces

Refer to Fig. 26

Gravity Head

Circuit 1	4.75
Circuit 2	Essentially the same as corresponding section Generating Furnace: Outside Wall
Circuit 3	$\frac{L_n}{X_n} \log_e \left[1 + \frac{X_n}{1 + \sum_1^n X_{n...}} \right]$

V_o	$\sum_1^n X_{n-1}$	X_n	$1 + \sum_1^n X_{n-1}$	Gravity head
0.5	2.42	2.64	3.42	2.95
1.0	1.21	1.32	2.21	4.82
1.5	0.806	0.86	1.806	6.16
2.0	0.605	0.66	1.605	7.09

Entrance and Exit Loss $1.5 \frac{V_o^2}{2g}$

V_o	$\frac{V_o^2}{2g}$	Entrance & Exit Loss
0.5	.0039	.006
1.0	0.0155	.023
1.5	.035	.053
2.0	.062	.093

Acceleration Loss

Circuit 1	0
Circuit 2	Essentially the same as corresponding section Generating Furnace: Outside Wall
Circuit 3	$\frac{V_o^2}{2g} \times 2X_n$

V_o	$\frac{V_o^2}{2g}$	X_n	$2X_n$	Acceleration Loss
0.5	.0039	2.64	5.28	.021
1.0	.0155	1.32	2.64	.041
1.5	.035	0.86	1.72	.060
2.0	.062	0.66	1.32	.082

Front and Rear Walls: Both Furnaces (cont.)**Bend Loss****Circuit 1** 1 bend

$$K_B = .39$$

$$K_B \frac{V_o^2}{2g}$$

V_o	$\frac{V_o^2}{2g}$	K_B	Bend Loss
0.5	.0039	.39	.002
1.0	.0155	.39	.006
1.5	.035	.39	.014
2.0	.062	.39	.24

Circuit 2 —0 **Circuit 3**

$$K_B = .30$$

$$K_B \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$$

V_o	$\frac{V_o^2}{2g}$	K_B	\sum_1^n	$1 + \sum_1^n X_{n-1}$	Bend Loss
0.5	.0039	.30	5.06	6.06	.006
1.0	.0155	.30	2.53	3.53	.016
1.5	.035	.30	1.666	2.666	0.28
2.0	.062	.30	1.265	2.265	.042

Friction Loss**Circuit 1** $.288 \frac{L}{d} \frac{V_o^2}{2g}$

V_o	$\frac{V_o^2}{2g}$	$.288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	Friction Loss
0.5	.0039	.001125	3.30	.004
1.0	.0155	.00447	3.30	.015
1.5	.035	.0101	3.30	.033
2.0	.035	.0101	3.30	.033
2.0	.062	.01785	3.30	.059

Circuit 2 Essentially the same as corresponding
section **Generating Furnace: Outside
Wall**

Front and Rear Walls: Both Furnaces (cont.)

$$\text{Circuit 3} \quad .288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$\frac{V_o^2}{2g}$	$.288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_n}{2}$	$1 + \sum_1^n X_{n-1}$	$1 + \frac{X_n}{2} + \sum_1^n X_{n-1}$	Friction Loss
0.5	.0039	.001125	4.83	1.32	3.42	4.74	.026
1.0	0.155	.00447	4.83	0.66	2.21	2.87	.062
1.5	.035	.0101	4.83	0.44	1.806	2.246	.110
2.0	.062	.01785	4.83	0.33	1.605	1.935	.167

$$\text{Feeder Loss} \quad 2.71 \frac{V_o^2}{2g} \times \left(\frac{1}{.1556} \right)^2 = 11.25 \frac{V_o^2}{2g}$$

V_o	$\frac{V_o^2}{2g}$	Feeder Loss
0.5	.0039	.438
1.0	0.155	1.748
1.5	.035	3.940
2.0	0.62	6.980

Each of these walls ends in a header and from this header feeders are taken to the drum. These are essentially unheated.

$$\text{Area of wall} = 1.558 \times 144 = 224 \text{sq.in.}$$

$$\text{Area of feeders} = \frac{\pi}{4} (2.52)^2 \times 4 + \frac{\pi}{4} (3.44)^2 \times 7 = 85 \text{sq.in.}$$

$$K^2 = \left(\frac{224}{85} \right)^2 = 6.95$$

Superheater Furnace Walls

Entrance and Exit Loss $1.5 \frac{V_o^2}{2g} \times 6.95 [1 + \sum^n + 1X_{n-1}]$

V_o	$10.4 \frac{V_o^2}{2g}$	$1 + \sum_1^n X_{n-1}$	Entrance and exit loss
0.5	.0406	6.06	.246
1.0	.1615	3.53	.570
1.5	.364	2.666	.969
2.0	.645	2.265	1.460

Front and Rear Walls: Both Furnaces (cont.)

$$\text{Gravity Head} = \frac{4.75}{1 + \sum_1^n X_n - 1}$$

V_o	$1 + \sum_1^n X_n - 1$	Gravity Head
0.5	6.06	.784
1.0	3.53	1.345
2.0	2.265	2.100

$$\text{Friction Loss} = .288 \frac{L}{d} \times 6.95 \frac{V_o^2}{2g} [1 + \sum_1^n X_n - 1]$$

V_o	$6.95 \times .288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	$1 + \sum_1^n X_n - 1$	Friction Loss
0.5	.00782	1.52	6.06	0.72
1.0	.0311	1.52	3.53	.167
1.5	.0703	1.52	2.666	.284
2.0	.124	1.52	2.265	.427

Generating Furnace

$$\text{Gravity Head} = \frac{3.00}{1 + \sum_1^n Xn - 1}$$

V_o		Gravity Head
0.5	6.06	.495
1.0	3.53	.850
1.5	2.666	1.125
2.0	2.265	1.322

$$\text{Friction Loss} = .288 \frac{L}{d} \times 6.95 \frac{V_o^L}{2g} [1 + \sum_1^n Xn - 1]$$

Σ Gravity Head + Σ Losses

V_o	$6.95 \times \frac{V_o^2}{2g}$	$\frac{L}{d}$	$1 + \sum_1^n Xn - 1$	Friction Loss	Generating Furnace	Superheater Furnace
0.5	.00782	0.96	6.06	.045	21.73	22.05
1.0	.0311	0.96	3.53	.105	29.52	30.07
1.5	.0703	0.96	2.666	.180	35.92	36.68
2.0	.124	0.96	2.265	.270	41.16	43.09

Boiler Bank and Inside Wall: Generating Furnace

The **Boiler Bank and Inside Wall: Generating Furnace** of this unit are more involved since both radiation and convection occur in these walls. The methods and experimental data used to compute the heat transfer in design are usually as given in McAdams⁽³³⁾ or other standard sources, but once the conditions of operation are predicted or known, the total heat absorbed in each section can be obtained as follows:

Enthalpy of steam at Superheater outlet	1447.7 $\frac{\text{Btu}}{\text{lb.}}$			
Enthalpy of saturated steam at drum conditions	1193.9 $\frac{\text{Btu}}{\text{lb.}}$			
Change in enthalpy	253.8 $\frac{\text{Btu}}{\text{lb.}}$			
Heat absorbed in Superheater	$387,500 \times 253.8 = 98,000,000 \frac{\text{Btu}}{\text{hr.}}$			
Change in Enthalpy in heating water leaving economizer	<table> <tbody> <tr> <td>1447.7</td> </tr> <tr> <td>— 473.9</td> </tr> <tr> <td style="border-top: 1px solid black;">973.8 $\frac{\text{Btu}}{\text{lb.}}$</td> </tr> </tbody> </table>	1447.7	— 473.9	973.8 $\frac{\text{Btu}}{\text{lb.}}$
1447.7				
— 473.9				
973.8 $\frac{\text{Btu}}{\text{lb.}}$				
Total water absorption	$973.8 \times 422,200 = 410,000,000 \frac{\text{Btu}}{\text{hr.}}$			
Heat absorbed in Boiler Bank	$45,000,000 \frac{\text{Btu}}{\text{hr.}}$			

The heat absorption in the **Inside Wall: Generating Furnace** due to radiation can be taken as essentially the same as in the rest of the furnace. The Boiler Bank is essentially a convection heating surface and as such can properly be treated by the equations developed for this case in Section II. However, since the rates of heat absorption are comparatively low, the equations for the case of uniform heat absorption can be applied with very little error.

V_0	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	X_n	$\frac{X_n}{1 + \sum_1^n X_{n-1}}$	$1 + \frac{X_n}{1 + \sum_1^n X_{n-1}}$	Gravity Head
0.5	3.00	4.00	1.104	0.276	1.276	1.26
1.0	1.50	2.50	0.652	0.261	1.221	2.06
1.5	1.00	2.00	0.368	0.184	1.184	2.62
2.0	0.75	1.75	0.276	0.158	1.158	3.03

$$\text{Circuit 5 } \frac{L_n}{X_n} \sin \theta \log_e \left[1 + \frac{X_n}{1 + \sum_1^n X_{n-1}} \right]$$

V_0	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	X_n	$\frac{X_n}{1 + \sum_1^n X_{n-1}}$	$1 + \frac{X_n}{1 + \sum_1^n X_{n-1}}$	Gravity Head
0.5	4.104	5.104	0.904	0.177	1.177	0.73
1.0	2.052	3.052	0.452	0.148	1.148	1.23
1.5	1.368	2.368	0.301	0.127	1.127	1.60
2.0	1.026	2.026	0.226	0.112	1.112	1.89

$$\text{Circuit 6 } \frac{L}{X_n} \sin \theta \log_e \left[1 + \frac{X_n}{1 + \sum_1^n X_{n-1}} \right]$$

V_0	$\sum_1^n X_{n-1}$	$1 + \sum_1^n X_{n-1}$	X_n	$\frac{X_n}{1 + \sum_1^n X_{n-1}}$	$1 + \frac{X_n}{1 + \sum_1^n X_{n-1}}$	Gravity Head
0.5	5.008	6.008	0.388	0.065	1.065	0.21
1.0	2.504	3.504	0.194	0.0554	1.0554	0.36
1.5	1.669	2.669	0.129	0.0484	1.0484	0.47
2.0	1.252	2.252	0.097	0.043	1.043	0.56

Losses

Acceleration Loss

$$\text{Circuit 1 } -0$$

$$\text{Circuit 2 } \frac{V_0^2}{2g} \times 2X_n$$

V_o	$\frac{V_o^2}{2g}$	X_n	Acceleration Loss
0.5	.0039	1.32	.0103
1.0	.0155	0.66	.0205
1.5	.035	0.44	.0309
2.0	.062	0.33	.041

Circuit 3 $\frac{V_o^2}{2g} \times 2X_n$

V_o	$\frac{V_o^2}{2g}$	X_n	Acceleration Loss
0.5	0.0039	1.68	0.013
1.0	0.0155	0.84	0.026
1.5	0.0350	0.56	0.039
2.0	0.0620	0.42	0.052

Circuit 4 $\frac{V_o^2}{2g} \times 2X_n$

V_o	$\frac{V_o^2}{2g} \times 2X_n$	X_n	Acceleration Loss
0.5	0.0039	1.104	0.009
1.0	0.0155	0.552	0.017
1.5	0.0350	0.368	0.0260
2.0	0.0620	0.276	0.034

Circuit 5 $\frac{V_o^2}{2g} \times 2X_n$

V_o	$\frac{V_o^2}{2g}$	X_n	Acceleration Loss
0.5	0.0039	0.904	0.007
1.0	0.0155	0.452	0.014
1.5	0.0350	0.301	0.021
2.0	0.0620	0.226	0.028

Circuit 6 $\frac{V_o^2}{2g} \times 2X_n$

V_o	$\frac{V_o^2}{2g}$	X_n	Acceleration Loss
0.5	0.0039	0.388	0.003
1.0	0.0155	0.194	0.006
1.5	0.0350	0.129	0.009
2.0	0.0620	0.097	0.012

Inside Wall: Generating Furnace (cont.)**Entrance and Exist Loss**

$$1.5 \frac{V_o^2}{2g}$$

V_o	$\frac{V_o^2}{2g}$	Entrance and Exit Loss
0.5	0.039	0.006
1.0	0.155	0.023
1.5	0.350	0.053
2.0	0.620	0.093

Bend Loss

Circuit 1: Essentially as corresponding section Generating Furnace: Outside Wall.

Circuit 2: 1 bend

$$K_B = 0.25; \quad K_B \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$$

V_o	$\frac{V_o^2}{2g}$	$1 + \sum X_{n-1}$	Bend Loss
0.5	0.039	2.32	0.002
1.0	0.155	1.66	0.006
1.5	0.350	1.44	0.013
2.0	0.620	1.33	0.021

Circuit 3: —0

Circuit 4: 1 bend

$$K_B = 0.24; \quad K_B \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$$

V_o	$\frac{V_o^2}{2g}$	$1 + \sum X_{n-1}$	Bend Loss
0.5	0.039	5.104	0.005
1.0	0.155	3.052	0.011
1.5	0.35	2.368	0.020
2.0	0.62	2.026	0.030

Circuit 5: 1 bend

$$K_B = 0.3; \quad K_B \frac{V_o^2}{2g} [1 + \sum_1^n X_{n-1}]$$

V_o	$\frac{V_o^2}{2g}$	$1 + \sum X_{n-1}$	Bend Loss
0.5	0.0039	6.008	0.007
1.0	0.0155	3.504	0.016
1.5	0.0350	2.669	0.028
2.0	0.0620	2.252	0.042

Circuit 6: O**Friction Loss**

Circuit 1 Essentially the same as corresponding section Generating Furnace: Outside Wall.

Circuit 3

$$.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$\frac{.288V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_n}{2}$	Friction Loss
0.5	0.001125	3.17	1.660	0.006
1.0	0.004470	3.17	1.330	0.019
1.5	0.010100	3.17	1.220	0.039
2.0	0.017850	3.17	1.165	0.066

Circuit 4

$$.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$\frac{.288V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_n}{2}$	$1 + \sum_1^n X_{n-1}$	Friction Loss
0.5	0.001125	6.87	0.84	2.32	0.024
1.0	0.004470	6.87	0.42	1.66	0.064
1.5	0.010100	6.87	0.28	1.44	0.120
2.0	0.017850	6.87	0.21	1.33	0.189

Circuit 4

$$.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$\frac{.288 V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_p}{2}$	$1 + \sum_1^n X_{n-1}$	Friction Loss
0.5	0.001125	2.26	0.552	4.00	0.012
1.0	0.004470	2.26	0.276	2.50	0.028
1.5	0.010100	2.26	0.184	2.00	0.050
2.0	0.017850	2.26	0.138	1.75	0.076

Circuit 5

$$.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$.288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_n}{2}$	$1 + \sum_1^n X_{n-1}$	Friction Loss
0.5	0.001125	1.85	0.452	5.104	0.012
1.0	0.00447	1.85	0.226	3.052	0.027
1.5	0.01010	1.85	0.151	2.368	0.047
2.0	0.01785	1.85	0.113	2.026	0.071

Circuit 6

$$.288 \frac{L}{d} \frac{V_o^2}{2g} \left[1 + \frac{X_n}{2} + \sum_1^n X_{n-1} \right]$$

V_o	$.288 \frac{V_o^2}{2g}$	$\frac{L}{d}$	$\frac{X_n}{2}$	$1 + \sum_1^n X_{n-1}$	Friction Loss
0.5	0.001125	0.80	0.194	6.008	0.006
1.0	0.004470	0.80	0.097	3.504	0.013
1.5	0.01010	0.80	0.065	2.669	0.022
2.0	0.01785	0.80	0.048	2.252	0.033

Feeder Loss

$$3.78 \left(\frac{1}{0.1553} \right)^2 \times \frac{V_o^2}{2g}$$

V_0	Feeder Loss	Σ Gravity Head + Σ Losses
0.5	0.61	24.00
1.0	2.43	31.32
1.5	5.46	37.83
2.0	9.72	44.67

Boiler Bank**Refer to Fig. 26**

In this section the average heated length of tube is 37 feet and may be taken as a single vertical tube.

$$N = 0.040$$

Gravity Head

$$\frac{L_n}{x_n} \log_e [1 + X_n] + 1 + \frac{2}{1 + X_n}$$

V_0	x_n	$1 + x_n$	Gravity Head
0.5	2.720	3.720	16.94
1.0	1.360	2.360	23.35
1.5	0.907	1.907	26.20
2.0	0.680	1.680	28.09

Acceleration Loss

$$\frac{V_0}{2g} \times 2X_n$$

V_0	$\frac{V_0^2}{2g}$	$2X_n$	Acceleration Loss
0.5	0.039	5.440	0.021
1.0	0.155	2.720	0.042
1.5	0.350	1.813	0.064
2.0	0.620	1.360	0.084

Bend Loss: Essentially 0

Entrance and Exit Loss; Friction Loss

$$\frac{1.5V_o^2}{2g}; .288 \frac{V_o^2 L}{2g d} \left[1 + \frac{X_n}{2} \right]$$

V_o	$\frac{V_o^2}{2g}$	Entrance & Exit Loss	$\frac{L}{d}$	$1 + \frac{X_n}{2}$	Friction Loss	Σ Gravity Head + Σ Losses
0.5	0.039	0.06	200	2.360	0.53	17.02
1.0	0.155	0.23	200	1.680	1.50	23.57
1.5	0.350	0.53	200	1.440	2.91	26.61
2.0	0.620	0.93	200	1.340	4.78	28.75

From Mr. Lorenzini's report the following values were found:

VELOCITY ENTERING WALL TUBES - Ft./Sec.

WALL	V_o
Generating side wall	1.687
Superheater side wall	1.692
Generating front wall	0.894
Superheater front wall	1.011
Generating rear wall	1.262
Superheater rear wall	1.278
Inside wall	1.182

B. Calculations By Use of Curves

All the computations in this section are independent of those made in the previous section of this work. For each wall, refer to the figure of the typical tube in the wall.

Generating Furnace: Outside Wall

Circuit 1

V_o	Gravity Head	$\frac{L}{d}$	Losses
0.5	10.34	5.02	0.012
1.0	10.34	5.02	0.055
1.5	10.34	5.02	0.115
2.0	10.34	5.02	0.210

Circuit 2

X_n	Gravity Head	$\frac{L}{d}$	Losses
2.42	$25 \times 0.51 = 12.75$	9.93	0.050
1.21	$25 \times 0.655 = 16.40$	9.93	0.138
0.806	$25 \times 0.735 = 18.40$	9.93	0.260
0.605	$25 \times 0.783 = 19.55$	9.93	0.440

Circuit 3

X_n	$\sum_1^n X_{n-1}$	$\frac{L}{D}$	Gravity Head	Losses
2.23	2.42	4.58	$11.5 \times 0.225 = 2.59$	$0.035 + 0.029 = 0.64$
1.115	1.21	4.58	$11.5 \times 0.367 = 4.22$	$0.95 + 0.64 = 1.59$
0.743	0.806	4.58	$11.5 \times 0.460 = 5.30$	$0.175 + 0.088 = 0.263$
0.557	0.605	4.58	$11.5 \times 0.535 = 6.15$	$0.280 + 0.121 = 0.401$

Circuit 4

V_0	X_n	$\sum_1^n X_{n-1}$	$\frac{l}{d}$	Gravity Head	Losses	Feeder Loss $78.4 \frac{V_0^2}{2g}$	Σ Gravity Head + Σ Losses
0.5	0	4.65	5.25	0.62	0.67	0.305	26.80
1.0	0	2.325	5.25	1.05	0.175	1.218	33.75
1.5	0	1.549	5.25	1.37	0.282	2.740	39.07
2.0	0	1.162	5.25	1.62	0.432	4.860	44.00

Superheater Furnace: Outside Wall

All values of Gravity Head are essentially the same as corresponding sections of **Generating Furnace: Outside Wall**. All values of Losses are the same as those in corresponding sections of **Generating Furnace: Outside Wall** except for the last section.

Circuit 4

V_o	$\sum_1^n X_n = 0$	$\frac{L}{d}$	Losses	Σ Gravity Head+ Σ Losses
0.5	4.650	11.7	0.118	26.85
1.0	2.325	11.7	0.316	33.90
1.5	1.550	11.7	0.472	39.26
2.0	1.165	11.7	0.692	44.26

Front and Rear Walls: Both Furnaces

Circuit 1

V_o	Gravity Head	$\frac{L}{d}$	Losses	X_n
0.5	4.75	3.30	0.011	2.42
1.0	4.75	3.30	0.045	1.21
1.5	4.75	3.30	0.100	0.806
2.0	4.75	3.30	0.180	0.605

Circuit 2

V_o	Gravity Head	$\frac{L}{d}$	Losses
0.5	$25 \times 0.51 = 12.75$	9.93	0.050
1.0	$25 \times 0.655 = 16.40$	9.93	0.138
1.5	$25 \times 0.735 = 18.410$	9.93	0.260
2.0	$25 \times 0.783 = 195.75$	9.93	0.440

Circuit 3

V_o	X_n	$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses
0.5	2.64	2.42	4.83	$136 \times 217 = 295$	0.071
1.0	1.32	1.21	4.83	$136 \times 355 = 483$	0.169
1.5	0.86	0.806	4.83	$136 \times 454 = 616$	0.279
2.0	0.66	0.605	4.83	$136 \times 523 = 710$	0.431

Feeder to Drum

V_0	Feeder to Wall $2.71 \frac{V_0^2}{2g} \times \left(\frac{1}{0.1556}\right)^2$	Generating Furnace			Superheater Furnace				
		$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses	$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses
0.5	0.438	5.06	0.96	$3 \times 1.65 = 4.95$	0.337	5.06	1.52	$4.75 \times 0.165 = 0.785$	0.379
1.0	1.748	2.53	0.96	$3 \times 0.284 = 0.85$	0.797	2.53	1.52	$4.75 \times 0.284 = 1.350$	0.859
1.5	3.940	1.666	0.96	$3 \times 0.375 = 1.125$	1.130	1.666	1.52	$4.75 \times 0.375 = 1.770$	1.210
2.0	6.980	1.265	0.96	$3 \times 0.441 = 1.323$	1.800	1.265	1.52	$4.75 \times 0.441 = 2.090$	1.920

Feeder to Drum (cont.) Σ Gravity Head + Σ Losses

Generating Furnace	Superheater Furnace
21.85	22.18
29.73	30.29
36.14	36.87
42.56	43.44

Inside Wall: Generating Furnace**Circuit 1**

V_o	Gravity Head	$\frac{L}{d}$	Losses
0.5	10.34	5.02	0.012
1.0	10.34	5.02	0.055
1.5	10.34	5.02	0.115
2.0	10.34	5.02	0.210

Circuit 2

V_o	X_n	Gravity Head	$\frac{L}{d}$	Losses
0.5	1.32	$8 \times 0.635 = 5.07$	3.17	0.023
1.0	0.66	$8 \times 0.77 = 6.16$	3.17	0.068
1.5	0.44	$8 \times 0.828 = 6.63$	3.17	0.130
2.0	0.33	$8 \times 0.865 = 6.92$	3.17	0.210

Circuit 3

V_0	X_n	$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses
0.5	1.68	1.32	6.87	$17.3 \times 0.325 = 5.63$	$0.034 + 0.20 = 0.054$
1.0	0.84	0.66	6.87	$17.3 \times 0.49 = 8.46$	$0.098 + 0.042 = 0.140$
1.5	0.56	0.44	6.87	$17.3 \times 0.587 = 10.15$	$0.185 + 0.058 = 0.243$
2.0	0.42	0.33	6.87	$17.3 \times 0.655 = 11.35$	$0.310 + 0.076 = 0.386$

Circuit 4

V_0	X_n	$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses
0.5	1.104	3.00	2.26	$5.7 \times 0.22 = 1.26$	$0.019 + 0.023 = 0.042$
1.0	0.552	1.500	2.26	$5.7 \times 0.36 = 2.06$	$0.057 + 0.060 = 0.117$
1.5	0.368	1.00	2.26	$5.7 \times 0.458 = 2.62$	$0.115 + 0.087 = 0.202$
2.0	0.276	0.75	2.26	$5.7 \times 0.535 = 3.05$	$0.190 + 0.116 = 0.306$

Circuit 5

V_0	X_n	$\sum_1^n X_{n-1}$	$\frac{L}{d}$	Gravity Head	Losses	Feeder Loss
0.5	0.904	4.104	1.85	$4.03 \times 0.18 = 0.73$	$0.017 + 0.041 = 0.058$	0.61
1.0	0.904	4.104	1.85	$4.03 \times 0.305 = 1.23$	$0.053 + 0.081 = 1.34$	2.43
1.5	0.301	1.368	1.85	$4.03 \times 0.40 = 1.61$	$0.108 + 0.117 = 0.225$	5.46
2.0	0.226	1.026	1.85	$4.03 \times 0.47 = 1.90$	$0.180 + 0.156 = 0.336$	9.73

Circuit 6

V_0	X_n	$\sum_1^n X_{n-1}$	$\frac{L}{a}$	Gravity Head	Losses	Σ Gravity Head + Σ Losses
0.5	0.388	5.008	0.80	$1.3 \times 0.162 = 0.21$	$0.011 + 0.040 = 0.051$	24.10
1.0	0.194	2.504	0.80	$1.3 \times 0.278 = 0.36$	$0.035 + 0.075 = 0.110$	31.66
1.5	0.129	1.669	0.80	$1.3 \times 0.365 = 0.47$	$0.70 + 0.100 = 0.170$	38.36
2.0	0.097	1.252	0.80	$1.3 \times 0.435 = 0.56$	$0.130 + 0.150 = 0.280$	45.57

Boiler Bank

V_o	$\frac{L}{d}$	X_n	Gravity Head (total)	Losses	Σ Gravity Head + Σ Losses
0.5	20.0	2.720	16.95	0.081	17.03
1.0	20.0	1.360	23.35	0.218	23.57
1.5	20.0	0.907	26.20	0.420	26.62
2.0	20.0	0.680	28.10	0.650	28.75

The values of Gravity Head and Losses as tabulated on the preceding pages were obtained as follows:

To obtain the Gravity Head of any particular element, the values of X_n and X_n^{-1} were tabulated as previously. The vertical height of the circuit was then multiplied by the value of \bar{P} as read from Fig. 14 at these values of X_n and $\sum_1^n X_n - 1$. This gave the Gravity Head of the circuit. The Losses were obtained by entering the proper curve for V_o at the proper values of $\frac{L}{d}$ and X_n . As previously explained in Section II, to this value read from the curves, the quantity equal to this value read at $X_n = 0$ multiplied by $\sum_1^n X_n - 1$ was added to obtain the total losses in the circuit in question.

It will be noted from the tabulations of \sum Gravity Head $- \sum$ Losses that the values as computed from the graphical method are numerically greater than the values obtained from the straightforward application of the equations developed earlier in this work. In this particular case, the tube was divided into n series circuits. Therefore, the use of the curves introduced $n - 1$ extraneous entrance and exit losses. This accounts for the greater part of the difference found in the tabulations. The assumption of one bend with a K_B of 0.3 in each of the series circuits does not affect the final answer obtained by use of the curves to any appreciable extent. However, the total deviation in the final values is so small as to be negligible. The inherent assumptions made in the derivations and the assumptions in the rates of heat absorption can lead to errors that may be of the order of hundreds of times greater than any made by using the curves. The use of the curves will, in general, yield values of V_o slightly lower than use of the equations, and consequently, slightly lower circulation. This is conservative for design purposes.

On the following pages Figs. 29 & 30 show the values of \sum Gravity Head $- \sum$ Losses plotted as functions of V_o .

The Front and Rear, and Outside Walls of this installation are fed by two downcomers having an inside diameter of 13.5 in. and a length of 49.4 ft.

$$\begin{aligned}\text{Friction Loss} &= 4f \frac{L}{d} \frac{V^2}{2g} = 1.06 \frac{V^2}{2g} \\ \text{Entrance and Exit Loss} &= 1.5 \frac{V^2}{2g} \\ \text{Bend Loss (essentially)} &= 0.3 \frac{V^2}{2g}\end{aligned}$$

As can be seen from Fig. 23, these downcomers join a manifold from which the separate walls are fed. The loss at this "T" connection is very closely $2 \frac{V^2}{2g}$.⁽⁸⁸⁾ In addition, there is the friction loss in the manifold which, when taken as one-third of the normal friction loss,⁽⁴⁹⁾ is closely $0.7 \frac{V^2}{2g}$.

Total loss in these downcomers is equal to $5.56 \frac{V^2}{2g}$.

$$\text{Head available: Front and Rear Walls} = 44.75 - 5.56 \frac{V^2}{2g}$$

$$\text{Head available: Outside Walls} = 50.34 - 5.56 \frac{V^2}{2g}$$

The method of finding the operating point of the various walls consists of assuming various values of downcomer velocities. From each assumption, the head available to each of the walls is obtained and consequently each V_o . If the values of V_o for the head assumed give a total water flow that differs from the initial assumption, a new value of downcomer velocity is assumed until agreement is reached. Doing this, the following values of V_o are found:

Superheater Furnace: Outside Wall	1.680
Superheater Furnace: Front and Rear Walls	1.360
Generating Furnace: Outside Wall	1.710
Generating Furnace: Front and Rear Walls	1.400

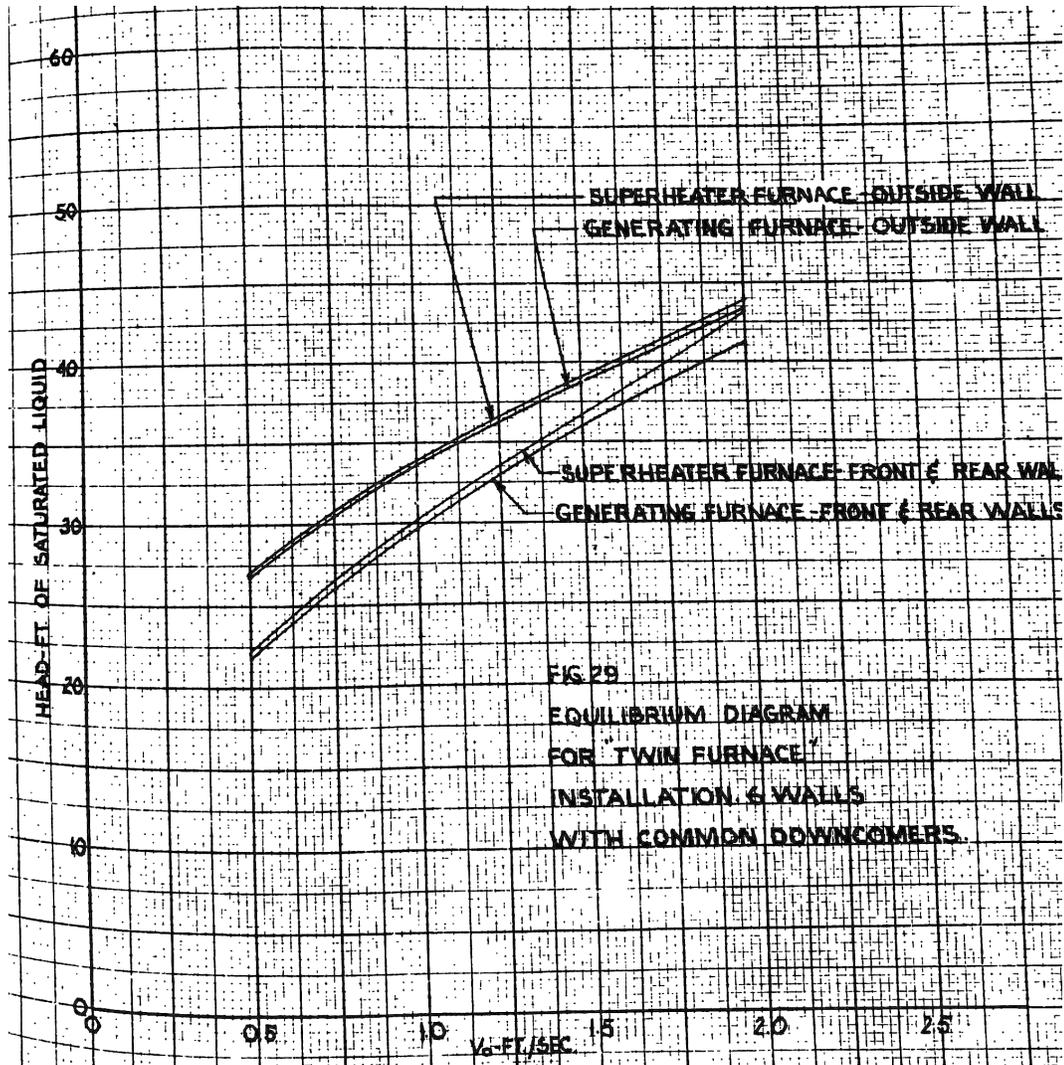
The downcomers for the **Boiler Bank** and **Inside Wall: Generating Furnace** extend from the upper steam drum to the mud drum. From the mud drum, feeders are taken to the lower header of the **Inside Wall: Generating Furnace**.

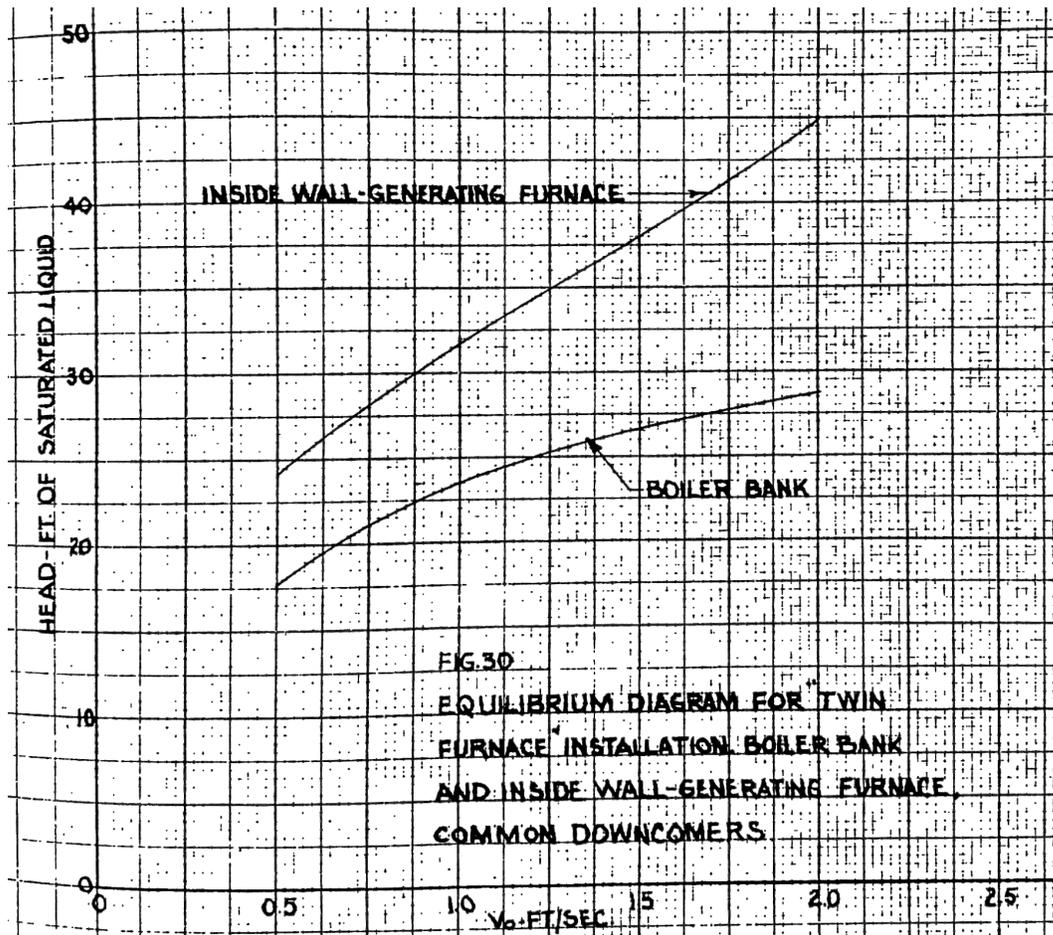
$$\text{Head available: Boiler Bank} = 37.0 - 2.93 \frac{V^2}{2g}$$

$$\text{Head available: Inside Wall-Generating Furnace} = 50.34 - 2.93 \frac{V^2}{2g}$$

The values of V_o for these walls are closely aligned:

Inside Wall: Generating Furnace	1.50
Boiler Bank	1.25





Knowing V_o , it is now possible to completely determine the circulation characteristics of each wall. These are tabulated below. because of the close agreement of the values determined for each wall by use of the special curves and by direct computation, only the values found by the direct computation method are given here.

	V_o	Water Entering Wall (lbs./hr.)	Steam Generated (lbs/hr)	β_n	λ_n	$\frac{1}{\lambda_n} =$ Circulation Ratio
Wall						
Outside Generating	1.71	1,028,000	66,000	0.605	0.0642	15.6
Outside Superheater Front	1.68	1,010,000	66,000	0.609	0.0654	15.3
Generating Front	1.40	366,000	31,300	0.676	0.0855	11.7
Superheater Rear	1.36	355,000	31,200	0.682	0.0878	11.4
Generating Rear	1.40	366,000	31,300	0.676	0.0855	11.7
Superheater Inside	1.36	355,000	31,200	0.682	0.0878	11.4
Generating Inside	1.50	902,000	76,500	0.675	0.0848	11.8
Boiler Bank	1.25	1,330,000	68,500	0.547	0.0515	19.4
Total		5,712,000	402,000	Overall Circulation Ratio		14.2

From the tabulation on the preceding page and the values of V_o from Mr. Lorenzini's tests, it can be seen that the computed values are in fair agreement with test values. It will also be noted that the total steam generation computed does not agree with the value of 422,000 (including steam condensation to heat the feed water to saturation conditions) used. On a previous page it was assumed that the total heat absorption in the **Radiant Wall: Superheater Furnace** could be taken as essentially the same as that in the **Inside Wall: Generating Furnace**, also the heat absorption in various sections of this unit was found by difference and these methods could easily lead to the discrepancy noted. Since this discrepancy is of the order of 2% it will not affect the final tabulation enough to warrant an adjustment of the values.

The author had occasion to speak to Mr. Lorenzini concerning the tests made on this unit, and Mr. Lorenzini noted the following difficulties encountered during this test:

1. One of the meters used on the downcomers of this unit was apparently faulty and regardless of all the attempts made to correct it, it still gave consistently low readings regardless of where it was positioned.
2. Difficulty was had with the burners during the test at this load and Mr. Lorenzini and the author both feel that this may have caused a condition in the furnaces to account for the fact that the test values for the **Front Walls**—both furnaces were consistently lower than the values for the **Rear Walls**.

In view of these difficulties, it is felt that the agreement of the calculated values with test values is very good for the water walls.

Before leaving this discussion, it must be noted that the entering velocity (V_o) of the **Inside Wall: Generating Furnace** as computed is greater than the test values. The downcomers for this wall and the **Boiler Bank** are heated to some extent even though they are insulated. In order to determine the possible effect of steam generation in these downcomers, the author assumed that the steam generated in them was 1% by weight. Using this value, almost exact agreement was found with test values. While in itself, this is not conclusive evidence that this amount of steam is generated in these downcomers, it is an indication that steam is generated in these downcomers. If it had been possible to determine the steam generation in these tubes, it could have been taken into account in the computations. Because of their location, such a determination is practically impossible, and under the circumstances, the indication that steam is generated in these downcomers must be taken as only a surmise.

C. Flow Reversal

Dr. B. Leib^(64,72) has demonstrated the fact that it is possible for a heated riser tube to reverse its direction of flow and act as a downcomer under certain conditions. If the tube acts as either a downcomer or riser with a positive flow in the direction in which it is acting, the overall effect on the unit may not be too serious. However, if the tube is acting as a riser or downcomer and only a slight change in operating conditions is necessary for it to change its direction of flow, it is possible to have overheating

occur in the tube due to steam blanketing or pocketing. The presence of steam in the downcomers will also cause the head available for flow to be materially decreased and consequently, in general, decrease the total water circulated. Special tests conducted by the Foster Wheeler Corporation have indicated that this may have occurred in actual boiler installations.

If a tube acts as a riser, the head necessary to maintain the flow at a given value of V_o is equal to the \sum Gravity Head + \sum Losses. When the tube acts as a downcomer, this becomes \sum Gravity Head - *sum* Losses. These statements are based upon the assumptions made in Section II of this work.

As an example, a vertical tube 50 feet long, having an inside diameter of 2.52 in. and a value of N 0.024 will be used. It is further assumed that this tube has no bends. The following tabulation gives the results of all the necessary computations:

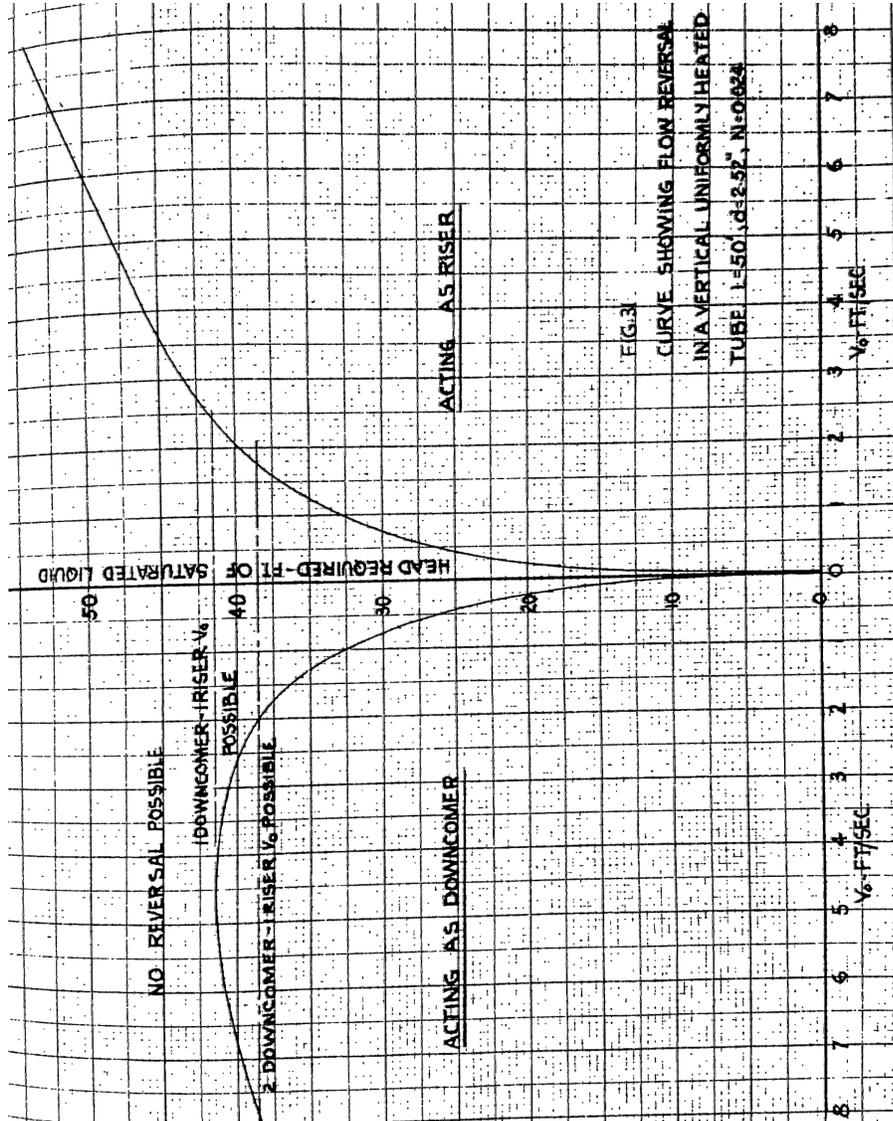


FIG. 3

CURVE SHOWING FLOW REVERSAL
IN A VERTICAL UNIFORMLY HEATED
TUBE $L=50$, $d=2.5$, $N=0.024$

V_0	Gravity Head	Acceleration Loss	Entrance & Exit Loss	Friction Loss	Σ Losses	Gravity Head + Σ Losses	Gravity Head - Σ Losses
1.0	32.8	0.037	0.023	0.142	0.202	33.0	32.6
2.0	39.2	0.075	0.093	0.462	0.630	39.8	38.6
3.0	42.0	0.112	0.209	0.960	1.281	43.3	40.7
4.0	43.6	0.149	0.373	1.640	2.162	45.8	41.4
5.0	44.8	0.186	0.582	2.490	3.258	48.1	41.5
6.0	45.5	0.224	0.840	3.520	4.584	50.1	40.9
7.0	46.0	0.270	1.140	4.720	6.220	52.2	39.8
8.0	46.4	0.298	1.490	6.100	7.888	54.3	38.5

A curve of the head required for flow for the case of the tube acting as a downcomer or riser is given in Fig. 31. It will be noted from this set of curves that if the tube can act as a riser with velocities (V_o) up to approximately 2.5 ft./sec., it is also possible for this same tube to act as a downcomer at two distinct velocities and still be in equilibrium. At approximately equal to 2.5 ft./sec. (riser) the tube can act as a downcomer at only one velocity and still be in equilibrium. Riser velocities (V_o) greater than 2.5 ft./sec. show that there is no velocity at which this tube can act as a downcomer and still be in equilibrium.

From the previous tabulation and the curves in Fig. 31, it is apparent that the introduction of added resistance in the riser circuit will tend to ensure the tube acting as a riser. However, as Nothman has shown,⁽¹⁾ care must be taken so as to avoid the restriction of flow to any great extent. Also, the introduction of added resistance in the riser or out may cause the deposition of impurities on the tube walls. Such an action will tend to further restrict the flow and also lower the overall coefficient of heat transfer to a point where tube failure may occur.

In connection with this subject of flow reversal, the question of heated downcomers must be mentioned. It has been demonstrated that if heat is applied to the downcomers so as to bring the fluid to its saturation state, the effect is beneficial as far as circulation is concerned.^(1, 62) Figs. 34 and 35 show the effect of steam entrainment on circulation. Additional heating beyond the saturation point is usually detrimental to the circulation characteristics of the unit as shown in the figures mentioned above. If sufficient heat is supplied to the downcomers, they will eventually, at some rate of heating, act as risers. However, it must be noted that once a tube starts to circulate in a given direction, reversal of flow will not occur if heat is applied to the downcomers at a later time, up to a limiting condition. Up to this condition, heat supplied to the downcomers is stored in the circulating fluid and released in the risers in the form of steam generation.^(1, 15, 62)

D. The Effect of Pressure on Circulation

Nothman⁽¹⁾ and Lewis & Robertson⁽⁶²⁾ have made very comprehensive correlations of the various factors that affect circulation. One of the most important of these is pressure, and while both of the references mentioned above treat this question, it is worthwhile to treat it briefly here because of its importance.

As an example, a fictitious air circuit consisting of a riser circuit of 2.00 in. O.D. and 1.73 in. I.D. and a length of 50 ft. will be used. It will also be assumed that the downcomer circuit is also 50 ft. long and has a flow area equal to that of the riser circuit.

The following set of calculations refers to the circuit mentioned above for a q of 10,000:

Pressure (psia)	N	NL
600	0.093	4.65
1000	0.058	2.90
1500	0.0415	2.07
2000	0.032	1.60
3000	0.0235	1.17

$$\text{Gravity Head} = \frac{V_o}{N} \log_e \left[1 + \frac{NL}{V_o} \right]$$

Pressure psia

V_o	600	1000	1500	2000	3000
1	18.6	23.5	27.0	29.9	33.0
2	25.9	30.9	34.2	36.7	39.2
3	30.1	34.9	37.9	40.0	42.1
4	33.2	37.6	40.2	42.1	43.7
5	35.3	39.4	41.8	43.4	44.9
6	37.0	40.7	42.8	44.3	45.5
7	38.4	41.8	43.8	45.1	46.2
8	39.2	42.6	44.4	45.6	47.0

$$\text{Losses} = \frac{V_o^2}{2g} \left[2.88 \left(1 + \frac{NL}{2V_o} \right) + 2 \frac{NL}{V_o} + 1.8 \right] \quad (f = 0.06, K_B = 0.3)$$

$$= \frac{V_o^2}{2g} \left[10.12 + 6.16 \frac{NL}{V_o} \right]$$

Pressure (psia) Data

V_o	600	1000	1500	2000	3000
0	0.62	0.42	0.37	0.32	0.28
1	1.52	1.18	1.03	0.995	0.85
2	2.75	2.25	2.01	1.88	1.76
3	4.32	3.63	3.32	3.13	2.97
4	6.16	5.32	4.93	4.70	4.50
5	8.40	7.32	6.86	6.59	6.35
6	10.85	9.65	9.12	8.81	8.50
7	13.68	12.30	11.68	11.30	10.97

Totals

Totals for Pressure (psia)

V_0	600	1000	1500	2000	3000
0	19.22	23.92	27.37	30.22	33.28
1	27.42	32.08	35.23	37.70	40.05
2	32.85	37.15	39.91	41.88	43.86
3	37.52	41.23	43.52	45.23	46.67
4	41.46	44.72	46.73	48.10	49.40
5	45.36	48.02	49.66	50.89	51.85
6	49.25	51.45	52.92	53.91	54.70
7	52.88	54.90	56.08	56.90	57.97

$$\text{Downcomer Losses} = 10.12 \frac{V_0^2}{2g}$$

V_0	
0	0.162
1	0.628
2	1.42
3	2.52
4	3.94
5	5.66
6	6.78
7	7.71
8	10.10

On the following page is a curve showing the values of head available and head required as functions of V_0 . From this curve, the values of V_0 are obtained and the circulation computed. By a similar process to that given above, the circulation characteristics of the hypothetical circuit for 1 of 10,000; 20,000; 30,000 & 40,000 have been computed and the results of these computations are shown graphically in Fig. 33.

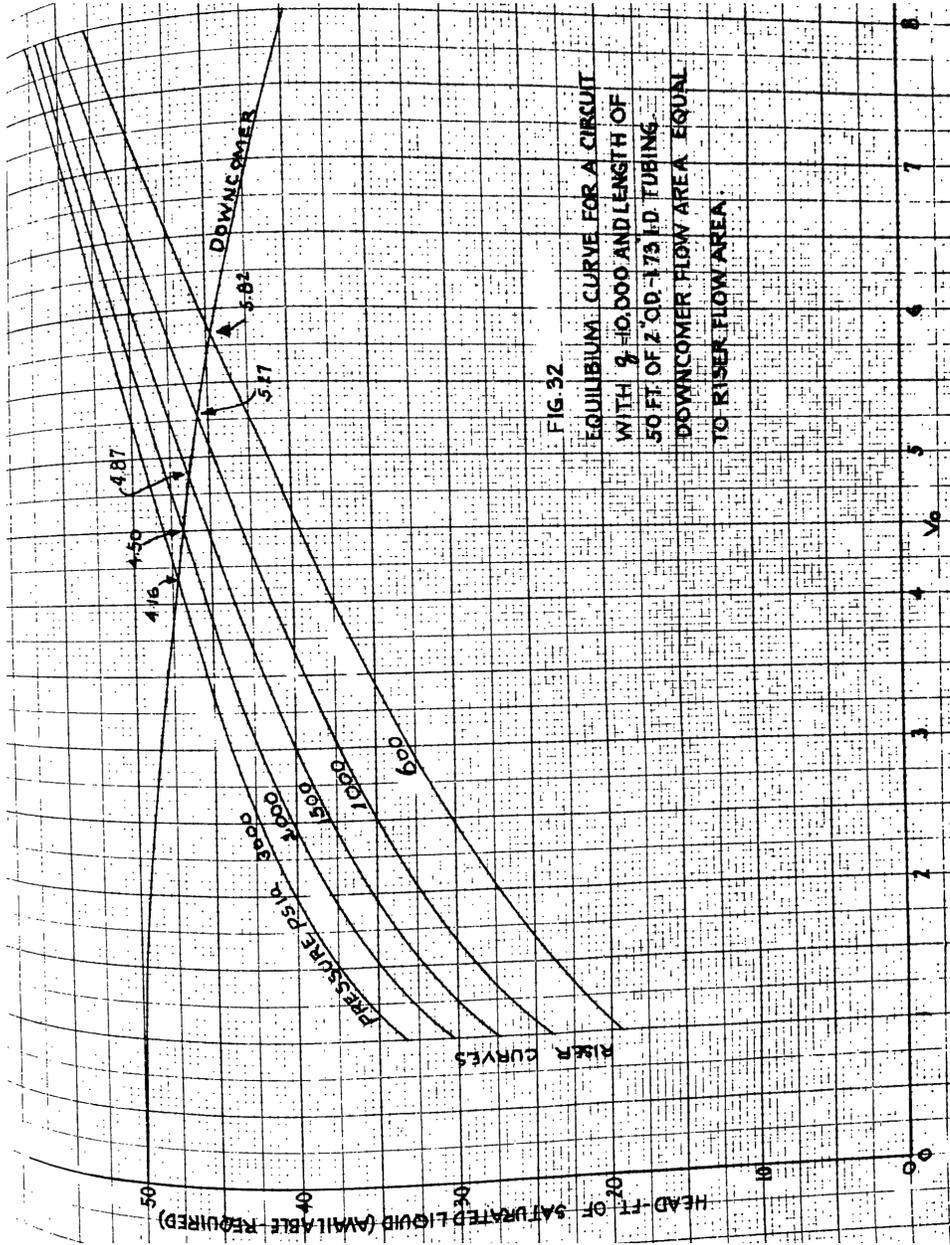


FIG. 32
EQUILIBIUM CURVE FOR A CIRCUIT
WITH 9" I.D. AND LENGTH OF
50 FT. OF 2" O.D. 173 I.D. TUBING
DOWNCOMER FLOW AREA EQUAL
TO RISER FLOW AREA

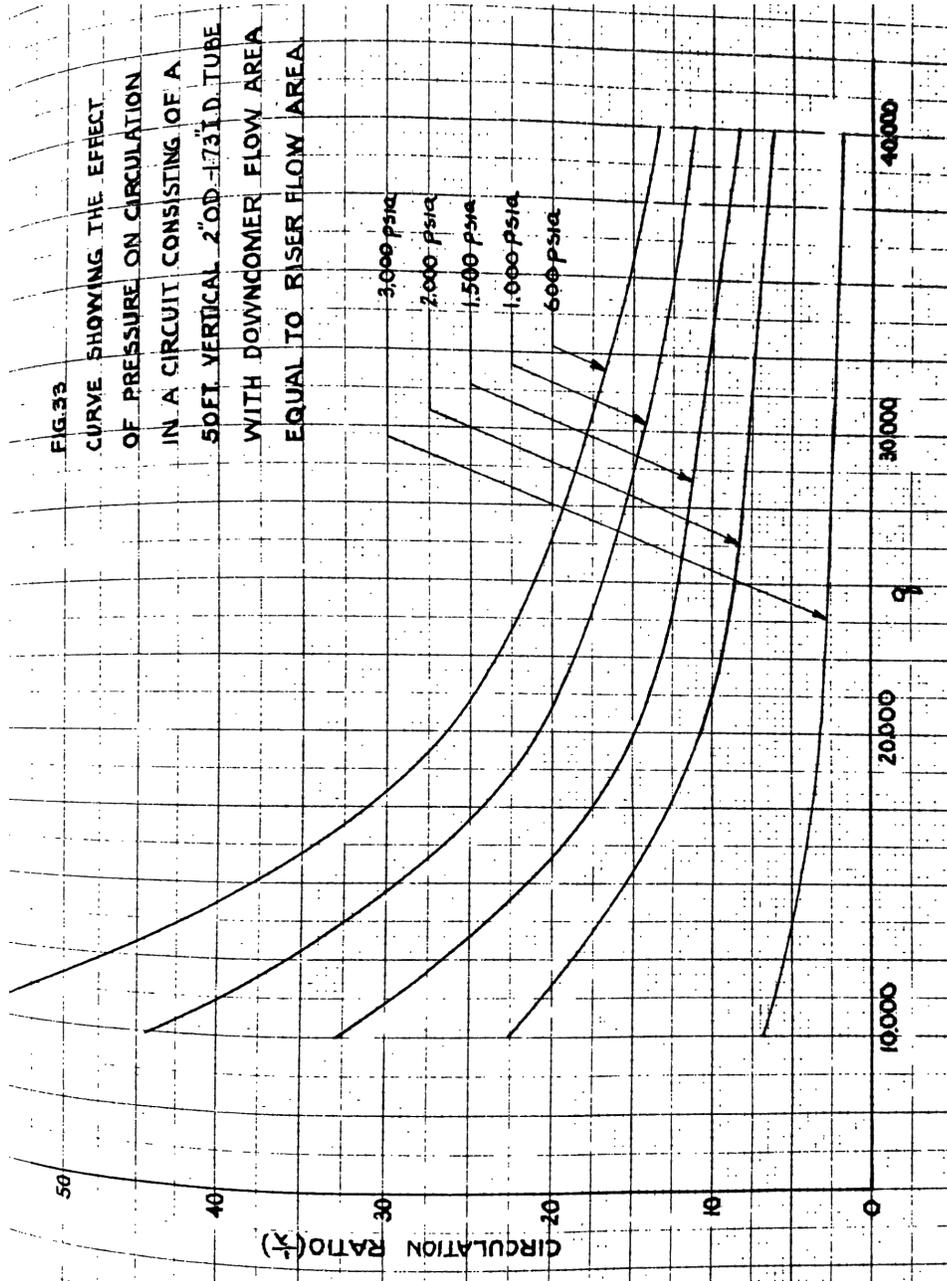


Fig. 33 clearly indicates the marked effect that an increase in pressure has on the circulation of the circuit chosen for this example. In conjunction with this curve, two things must be understood: for a given value of q , a different amount of steam is generated in the tube depending upon the pressure, and secondly, the amount of steam generated at a given pressure is directly proportional to the value of q .

The entire analysis and derivations made in this work were based on there being steam and water in the tube at all times. Therefore, they would not be directly applicable if superheated steam is formed in any section of the tube. If saturated steam at the critical pressure enters the circuit, it will, upon being heated, immediately become superheated steam. This follows from the fact that the latent heat of vaporization at the critical pressure is zero. Also, the density of saturated steam and saturated liquid at the critical pressure are equal to each other. Thus, at the critical pressure, the equations and analysis given here are not valid. However, if the curves of Fig. 33 are extrapolated, it would appear that a positive circulation can be maintained in the circuit. Lewis & Robertson,⁽⁶²⁾ in their analysis, also reached the conclusion that a positive and, in their case, an adequate circulation could be maintained at the critical pressure.

In their work, these authors, while discussing the effect of pressure on circulation, make the following statement: "... at 3,400 psi the density of water at 720 deg. F. is 17.04 lb. per cu. ft., and the total heat per pound (evidently Enthalpy) is 1,001.2 Btu." Using the conditions of pressure and temperature that these authors did in the above statement and the data in the Keenan & Keyes Tables, three discrepancies are to be found in this statement. The first discrepancy is that at this pressure and temperature, the steam is superheated and does not exist as water. Secondly, the density of the superheated steam is 12.95, and thirdly, the Enthalpy is 1024.1. It is also stated in this paper that the critical pressure is 3226 psi, while the Keenan & Keyes value is given as 3206.2 psi. The values of the physical properties of steam and water given in Appendix I of this paper also do not agree with the Keenan & Keyes data.

While the use of the incorrect values of the physical properties of steam and water makes the Lewis & Robertson calculations incorrect, their conclusions as to the effect of pressure on circulation appear to be valid on the basis of the example used in this work.

Recently, the paper by Martin Frisch and Robert A. Lorenzini⁽⁹⁸⁾ has been brought to the author's attention. In this paper, two of the topics discussed are the effect of pressure and steam entrainment in the downcomer on circulation. Figs. 34 & 36 have been reproduced from this work and are extremely interesting. The following is quoted directly from their work:

The effect on the circulation of even small amounts of steam in the circulating water is appreciable at pressure below 1500 psi. This may be seen in figure, which shows the calculated circulation at various pressures from 500 to 3000 psia in the simple circuit illustrated. This is for a uniform heat absorption rate of 50,000 btu per square foot of projected surface per hour,

and at three values of steam entrainment in the down-take water, namely the ideal zero, the maximum tolerable one percent, and an extreme value of two percent by weight.

Fig. 34 shows that the total circulation in the circuit falls as the pressure increases and at each pressure as the amount of steam entrainment increases. At a pressure of 500 psia, 1 percent entrainment by weight causes the circulation to fall off by 32 percent and 2 percent entrainment by 48 percent. At a pressure of 1500 psia, the corresponding values are 11 and 19 percent. The effect of steam entrainment on the circulation decreases as the pressure increases and is of less importance than the pressure itself. Thus, the circulation at a pressure of 2500 psia is about one-half of that at 1300 psia and about one-third of the circulation at a pressure of 500 psia when steam in the down-take supply is zero.

Fig. 35, also from this work of Frisch & Lorenzini, shows the effect of steam entrainment on circulation in a Twin Furnace unit similar to the one shown in Fig. 23.

If the circulation ratios are taken from Fig. 33 based on the example chosen for this work at a value of q and pressures equal to those in the Frisch & Lorenzini paper, it will be found that the conclusions that these authors reached as to the effect of pressure on circulation are essentially substantiated. While the author has not completely checked Fig. 34, calculations at several of the pressures and steam entrainment have been made using the equations developed in this work, and these values were found to agree with those shown in Fig. 34. The method used was to assume that a fictitious heated circuit preceded the riser circuit and had a value of $\frac{NL}{V_o}$ necessary to give the amount of stress by weight assumed to enter the riser circuit. The rest of the computations were made by the direct application of the equations that were developed for the case of circuits in series.

Fig. 36 shows the results of special tests made to determine the effect of pressure on circulation. The trends shown by these curves verify the conclusions above.

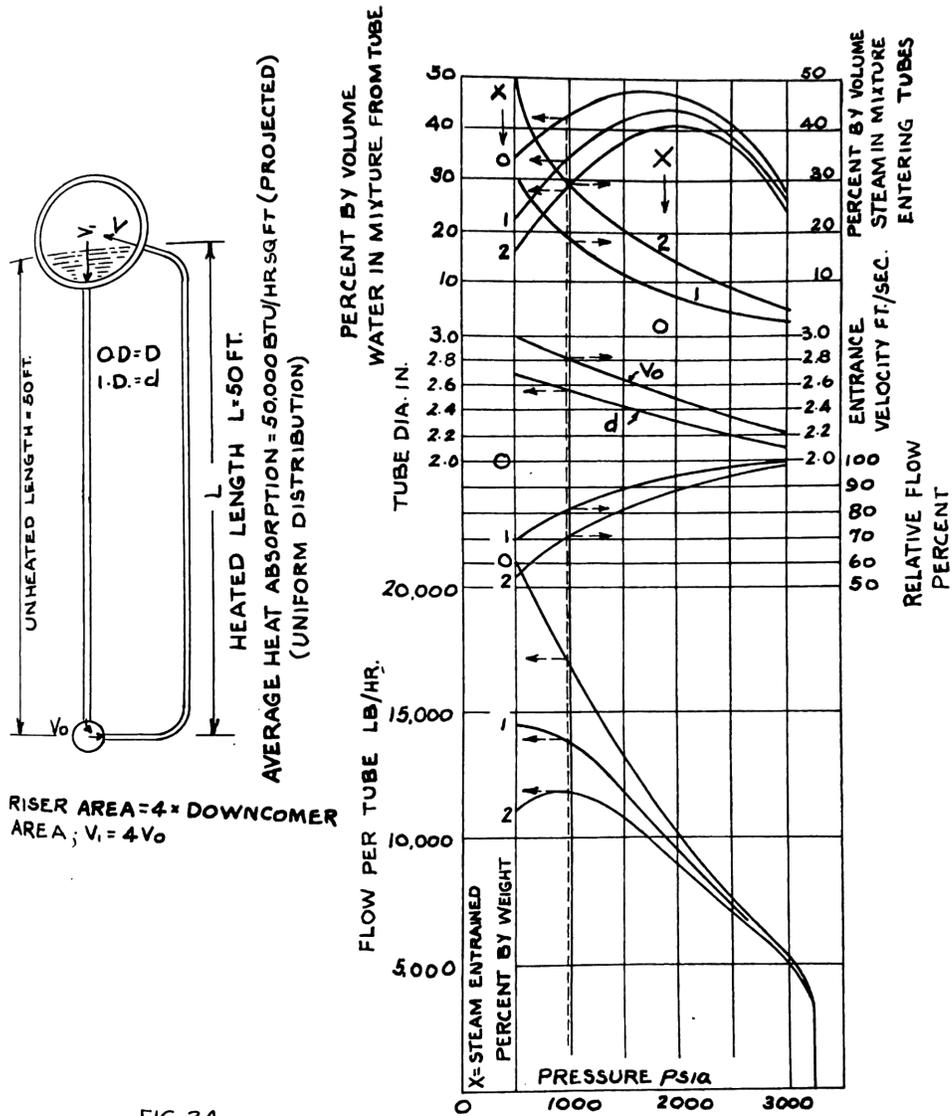


FIG. 34
EFFECT OF PRESSURE AND STEAM ENTRAINMENT
IN DOWNCOMER ON CIRCULATION IN A SIMPLE CIRCUIT

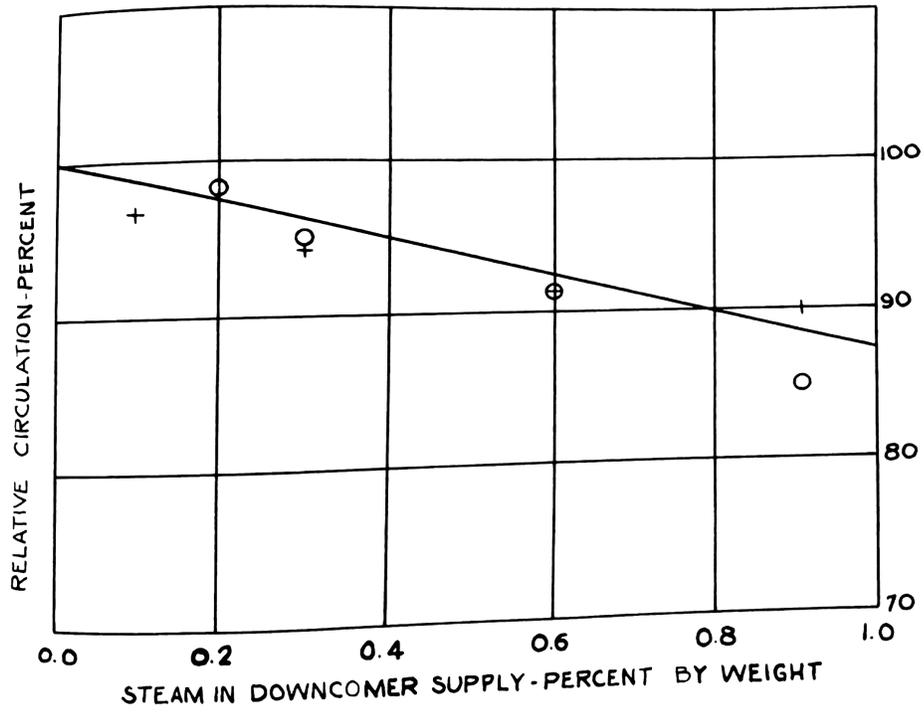
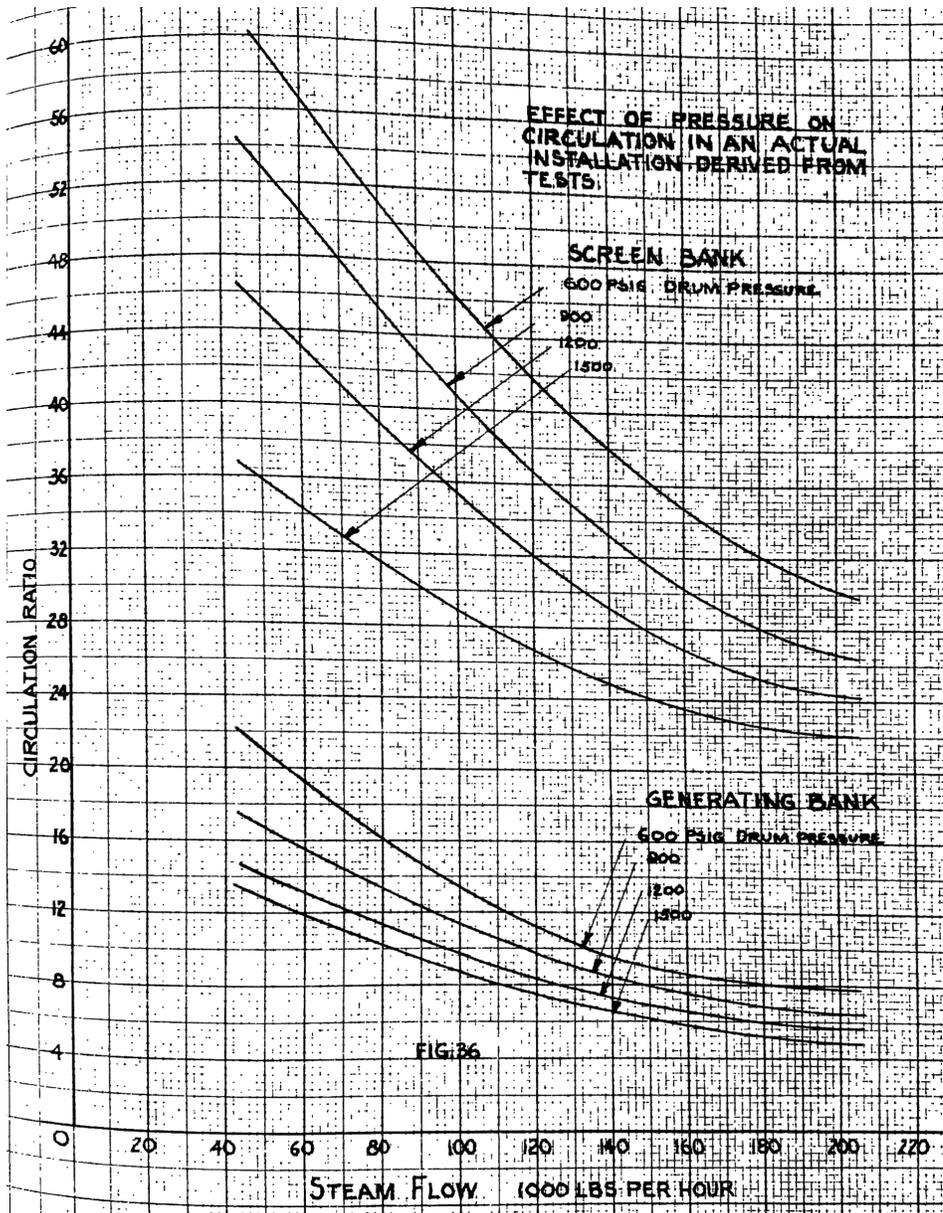


FIG 35 EFFECT OF STEAM ENTRAINMENT ON CIRCULATION

○ @ 400,000 LBS/HR. LOAD
 + @ 445,000 LBS/HR. LOAD

PRESSURE - 1400 psia (APPROXIMATELY)



Summary & Conclusions

Equations and curves have been developed from fundamental hydraulic and thermodynamic considerations to enable the complete circulation characteristics of a steam generating unit to be predicted. In these derivations, various assumptions about the distribution of heat absorption, friction factor, the effect of bubble slip, and the homogeneity of the mixture were made according to the best available data at the time. While the curves developed are strictly true only to the extent that these assumptions are true, the equations can be readily modified to account for any change in these assumptions when new data becomes available.

With these assumptions, the circulation characteristics of an actual unit were computed by use of both the curves and equations, and good agreement was found with test values. The use of the curves materially decreases the time needed for such computations and yields results that are essentially the same as those obtained by direct application of the equations. The effect of pressure on circulation and the possibility of flow reversal in a heated tube was also briefly discussed because of their importance in the design of natural circulation boilers.

The title of this work was purposely called "The Computation of Natural Circulation in Large Boilers" for very good reason. In the course of the author's work with the Foster Wheeler Corporation, he has had occasion to try to correlate the circulation characteristics of small Marine units on which test data was available by use of the methods of this work. In such units it is usual to find that the greater part of the steam generation occurs in the Boiler Bank, and a comparatively small amount of generation occurs in the Screen Bank and Water Walls. It has been found that the proper choice of friction factor and distribution of heat absorption is much more critical in these units than in a large boiler. An error of one foot of saturated liquid in a unit fifty feet in height causes a much smaller error in the final values than an equal error in a unit only ten feet high.

In almost every boiler built some form of internals or baffling is placed in the steam drum to insure steam free of impurities and decrease carry-over. These internals cause an added pressure drop in addition to those already discussed and, to be correct, this pressure drop should be taken into account in the circulation computations. However, as has been pointed out above, the percentage error incurred in a large boiler is much less than that incurred in a small unit if this pressure drop is neglected as was done in Section III of this work. The determination of the pressure drop in internals by tests is

extremely difficult and practically no data is available in the literature to enable one to compute it.

For the reasons just stated, this work has confined itself to large boilers. This does not mean that the derivations of Section II are not valid for small units; it means that further refinement of the assumptions must be made and that further tests are necessary before the same degree of correlation that has been found possible in large boilers is possible in smaller units.

Throughout this work, each assumption has purposely been pointed out to show where further tests are necessary. In the past, it has been found most expedient to run many of the tests with mixtures of air and water at or near atmospheric pressure. While much valuable information has been obtained by this method, there is a definite lack of knowledge concerning the mechanics of certain phases of the processes that occur during the transformation of water to steam at elevated pressures and temperatures. A test program to make such determinations as necessary to fill in the gaps in our present knowledge would be invaluable. Freon 12 has the physical properties at 200 psi that very nearly approach those of steam and water at 1400 psi. Because of the nearness of these properties and the relative ease in handling pressures of 200 psi compared to 1400 psi, it is suggested that a test program utilizing Freon 12 could be carried out to provide the necessary information on pressure drops.

Bibliography

Note: A large part of this bibliography is taken from the excellent one given in the work by Nothman.

1. “An Analytical Study and Correlation of Data on Natural Circulation in Steam Boiler Circuits” by G.A. Nothman, M.S. Thesis, Purdue University, 1942.
2. “Zur Theorie der Schnellumlauf-Warmwasserheizung” (“Investigation of the Theory of Rapid Velocity Hot Water Heating Systems”) by F. Hassenohrl, *Gesundheits Ingenieur*, Vol. 29, 1906, p. 365.
3. *Thermodynamics* by J.H. Keenan, John Wiley & Sons, New York 1941.
4. “Comptes rendus” by Hademard, *Académie des sciences, Paris*, Vol. 152, 1911, p. 1735.
5. “Über die fortschreitende Bewegung einer flussigen Kugel in einem zehen Medium” (“Treaties on the Nature of Motion of a Fluid Sphere through a Viscous Medium”) by W. Rybozinski, *Bulletin International de l’académie des sciences de Cravovie*, Serie A, 1911, p. 40.
6. Circulation in Horizontal Water Tube Boilers by P.A. Bancel, *J.A.S.M.E.*, Vol. 38, 1916, p. 17.
7. *Die Leistungsteigerung von Grossdampfkesseln (Improved Performance of Industrial Steam Boilers)* by F. Munzinger, J. Springer, Berlin, 1922, Chapter IV.
8. *Hutte, des Ingenieurs Taschenbuch (Engineering Handbook)*, 25th edition, Akademischer Verein Hutte, Berlin 1925, Vol. 1, pp. 349–360 and 516–520.
9. “Evaporators for Boiler-Feed Makeup Water” by W.L. Badger, *Trans. A.S.M.E.*, FSP–50, 1928, p. 45.
10. “High-Pressure Steem Boilers” by G.A. Orrok, *Trans. A.S.M.E.*, FSP–50, 1928, p. 32.
11. “Wassermulauf in Steil-und Schragohrkesseln” (“Water Circulation in Vertical and Inclined Tube Boilers”) by K. Cleve, *Archiv. f. Warmewirtschaft und Dampfkesselwesen*, Vol. 10, 1929, p. 379.

12. "Studies of Moisture at High Rates of Evaporation" by A.r. Mumford, *Trans. A.S.M.E., FSP-51*, 1929, p. 47.
13. "Velocity of Circulation in Water-Wall Tubes" by F.S. Smail, *Power*, Vol. 3, 1929, p. 411.
14. "Correct Boiler design an Essential Factor in the Production of Dry Steam" by K. Toensfeldt, *Combustion*, Vol. 9, 1929, p. 40.
15. "Der Wasserumleuf in Dampfkesseln" ("Water Circulation in Steam Boilers") by O. Berner, *Die Warme*, Vol. 52, 1930, p. T32.
16. "Circulation in Water Walls" by S.M. Finn, *Southern Power Journal*, Vol. 1.
17. "Der wasserumleuf im Wasserrohrkessel" ("Circulation in Water Tube Boilers") by R. Froehlich, *Die Warme*, Vol. 54, 1931, p. 465.
18. "Der Wasserumleuf in Stellrohrkesseln" ("Circulation of Water in Vertical-Tube Boilers") by W. Sohultes, *Die Warme*, Vol. 54, 1931, p. 535.
19. "Die Berechnung Des Wasserumlaufen in Kesselrohrbündeln und ihre Bedeutung für die Konstruktion von Waaserrohrkesseln" ("Circulations of Water Circulation in Boiler Tube Sheets and their Significance with respect to the Construction of Water Tube Boilers") by H. Seidel, *Z.d. Bayerischen Revisions-Vereins*, Vol. 35, 1931, p. 211.
20. "The Performance Rating of Steam-Generating Equipment" by H.L. Solbert, *Trans. A.S.M.E., FSP-53*, 1931, p. 8.
21. "Boiler Failures and their Causes", *Engineering*, Vol. 132, 1931, p. 241.
22. "Die Bedeutung der wasserumleuffrechnung bei dampfkesseln" ("The Significance water Circulation Analysis in steam Boile rs") by M. Blumel, *Z.d. Bayerischen Revisions-Reveins*, Vol. 36, 1932, p. 109.
23. "Neuere Arbeiten über den Wasserumleuf in wasserrohrkesseln" ("Recent Papers on Water Circulation in Water Tube Boilers by R. Boese, *Archiv f. Warme-wirtschaft und Dampfkesselwesen*, Vol. 13, 1932, p. 89.
24. "Foaming and Priming of Boiler Water" by C.W. Foulk, *Trans. A.S.M.E., RP-54*, 1932, p. 5.
25. "Circulation Test Twin Furnace Installation." Duquesne Light Co. by R.A. Lorenzini, Foster Wheeler Corp. 1943.
26. "Beitre Zur Berechnung des Wassermulsufes in Dampfkesseln" ("Contribution to the Analysis of Water Rication in Steam Boilers") by P. Koh, *Die Warme*, Vol. 55, 1932 p. 589.

27. "Characteristics of a High Pressure series steam Generator by A.A. Prosser, H.L. Solberg, and G.A. Hawkins, *Trans. A.S.M.E.*, RP-54-1b 1932, p. 9.
28. "Untersuchungen über den natürlichen Wasserumlauf in sulzer Hoehat-druckesseln" ("Investigations of the Natural Circulation in Sulzer High Pressure Boilers") by the Sulzer Company, *Feuerungstechnik*, Vol. 20, 1932, p. 65.
29. "Heat Transmission from Metal surfaces to Boiling Liquids" by D.s. Cryder & E.R. Gilliland, *Refrigeration Engineering*, Vol. 25, 1933, p. 78.
30. "Drop Versus Film Formation in the Condensation of steam on Condenser Tubes" by J.O. Jeffrey and J.R. Moynihan, *J. A.S.M.E.*, Vol. 55, 1933, p. 751.
31. "The Evaporation of a Liquid into a Gas—A Correction" by W.K. Lewis, *J. A.S.M.E.*, Vol. 55, 1933, p. 367.
32. "Stromungstechnische Fragen in Dampfkessel -und Feuerungebeu" ("Circulation Problems in Steam Boiler and Furnace Design") by Marcard, *Die Wärme*, Vol. 56, 1933, p. 291.
33. *Heat Transmission* by W.H. McAdams, McGraw-Hill Book Company, Inc., New York & London, 1942, 2nd Edition.
34. *Dampfkraft, Wasserrohrkessel und Dampfkraftanlagen.*, (*Steam Power in Water Tube Boilers and Steam Power Stations*) by F. Munzinger, J. Springer, Berlin 1933, pp. 135-156.
35. "Experiments regarding Circulation in Vertical-Tube Boilers" by E. Schmidt, *Combustion*, Vol. 8, 1935, p. 6.
36. "Paint Versus Bubbles" by the Dampney Company of America, *Power*, Vol. 4, 1934, p. 207.
37. "Wasserumlauf in Dampfkesseln" ("Water Circulation in Steam Boilers" by E. Schmidt, P. Behringer, & W. Schurig, *VDI-Forschungsheft*, № 365, 1934.
38. "Circulation in Vacuum Pens" by A.L. Webre, *Trans. A.S.M.E.*, PRO-56, 1934, p. 1.
39. "A Method of Determining the pressure drop for Oil-Vapor Mixtures Flowing Through Furnace Coils" by F.W. Dittus & A. Hildebrand, *Trans. A.S.M.E.*, Vol. 64, № 3, 1942, p. 185.
40. "Discussion of Reference (39)" by L.M.K. Boelter, *Trans. A.S.M.E.*, Vol. 64, № 3, 1942, p. 192.
41. "Velocity of Large Bubbles in vertical Tubes" by M.P. O'Brien & J.E. Goeline, *Industrial and Engineering Chemistry*, Vol. 27, 1935, p. 1436.

42. "Suspended Solids in the Foaming and Priming of Boiler Water" by C.W. Foulk, *J. A.S.M.E.*, Vol. 58, 1936, p. 372.
43. "Circulation in Water Tube Boilers" by R.M. Hanson, *Edison Bulletin*, Vol. 9, 1936, p. 385.
44. "Heat Transfer in Evaporation and Condensation" by M. Jakob, *J. A.S.M.E.*, Vol. 58, 1936, pp. 710 & 729.
45. *Thermodynamic Properties of Steam* by J.H. Keenan & F.G. Keyes, John Wiley & Sons, Inc., London, 1936.
46. "Modern Forms of Water-Tube Boilers and Land and Marine Use" by F. Munszinger, *Proc. Inst. Mech. Eng.*, Vol. 134, 1936, p. 5.
47. "Factors Influencing the Failure of Naval Boiler Tubes" by A.P. Calvert, *J. Am. Soc. Naval Eng.*, Vol. 51, 1939, No 1, pp. 1–34.
48. "Density and Boiler Circulation" by R.L. Sooreh, *Power Plant Engineering*, Vol. 40, 1936, p. 153.
49. *Hydraulics* by R.L. Daugherty, McGraw-Hill Book Co. , Inc., New York, 1937, p. 226.
50. "Schrifttum über Wasserumlauf in Dampfkesseln" ("Bibliography on Water circulation in steam Boilers") by K. Cleve, *Archiv f. Warmewirtschaft und Dampfkesselwesen*, Vol. 18, 1937, p. 1339.
51. "Foaming and Priming of Boiler Water" by C.W. Foulk, *Ohio State University Engineering Experiment Station News*, October–December 1937.
52. "Producing Oil by Gas-Lift and Natural-Flow Methods" by S.F. Shaw, *J. A.S.M.E.*, Vol. 59, 1937, p. 355.
53. "Experimental Investigation of the Influences of Tube Arrangement on Convection Heat Transfer and Flow Resistance in Cross Flow of Gases over Tube Banks" by O.L. Pierson, *Trans. A.S.M.E.*, Vol. 10, 1937, p. 563.
54. "Circulation in Boiler Tubes" by K. Toensfeldt, *Combustion*, Vol. 9, 1937, p. 24.
55. "Prediction of Pressure Drop During Forced Circulation of Boiling of Water" by R.C. Martinelli & D.B. Nelson, *A.S.M.E.* paper 47-A-113, 1947.
56. "Unstabilität der Stromung bei natürlichem und Zwengaumlauf" ("Instability of Circulation in Natural and Forced Circulation Circuits" by M. Ledinegg, *Die Wärme*, Vol. 61, 1936, p. 841.

57. "The Design of Water-Tube Units" by C.E. Lucke, Bulletin, № 3–235 of the Babcock and Wilcox Co., 1938, p. 10.
58. "Superheat Control and Steam Purity in High- Pressure Boilers" by Martin Frisch, *Trans. A.S.M.E.*, October 1940.
59. "Design of High-Capacity Boilers" by J. Van Brunt, *Trans A.S.M.E.*, FSP–60, 1938, p. 17.
60. "Attack on Steel in High-Capacity Boilers as a Result of Overheating due to Steam Blanketing" by E.P. Partridge & R.F. Hall, *Trans A.S.M.E.*, Vol. 51, 1939, p. 597.
61. "Corrosion in Partially Dry Steam-Generating Tubes" by F.G. Straub & E.E. Nelson, *J. A.S.M.E.*, Vol. 61, 1939, p. 199.
62. "The Circulation of Water and SSteam in Water Tube Boilers" by W.Y. Lewis & S.A. Robertson, *Proc. Inst. Mech. Eng.*, Vol. 143, 1940, p. 147.
63. "A New Steam Engine and Boiler" by S.L.G. Knox & J.I. Yellott, *Trans A.S.M.E.*, Vol. 63, 1941, p. 329.
64. "A Study of Circulation in High-Pressure Boilers and Water-Cooled Furnaces" by J. Van Brunt, *Trans A.S.M.E.*, Vol. 63, 1941, p. 339. *See also* E.O. Leib's Discussion p. 344–347.
65. "A Method of Estimating the Circulation in Steam-Boiler Furnace Circuits" by A.A. Markson, T. Ravese, & C.G.R. Humphreys, *Trans A.S.M.E.*, Vol. 64, 1942, p. 275.
66. "Studies of Heat Transmission Through Boiler Tubing at Pressures from 500 to 3300 Pounds" by W.F. Davidson, Ph.H. Hardie, C.G.R. Humphreys, A.A. Mumford, & T. Ravese, *Trans A.S.M.E.*, 1942.
67. "Computation of Circulation in Steam Boilers" by K.F. Roddatis & V.A. Loshkin (from *Izvestiya Vseoyuznogo Teplotechnicheskogo Instituts*, Vol. 15, № 4/5, 1946, p. 16), *The Engineers Digest*, Dec. 1946, Vol. 3, № 12.
68. *Combustion*, Sept. 1943, p. 45.
69. "The Measurement of Density and Quality of Steam-Water Mixtures in Steam Generators" by D. Du & R.A. Lorenzini, Chinese Institute of Engineers (reprinted in *Heat Eng.*), Nov. 1944.
70. *Fluid Mechanics for Hydraulic Engineers* by Hunter Rouse, McGraw Hill Book Co., 1938.
71. *The Mechanics of Turbulent Flow* by Bakhmeteff, Princeton University Press, 1941.

72. "Discussion of Reference (65)" by N. Artesy and E. Leib, *Trans A.S.M.E.*, Vol. 64, № 3, 1942, pp. 282–285.
73. "Absorption of Heat by Walls of a Furnace" by John Blizzard, *Trans A.S.M.E.*.
74. "Friction Factors for Pipe Flow" by L.F. Moody, *Trans A.S.M.E.*, Vol. 66, 1944.
75. "Vaporization Inside Horizontal Tubes, by W.H. McAdams, W.K. Woods, & R.L. Bryan, *Trans A.S.M.E.*, Vol. 62, 1940.
76. *Heat Power Engineering*, by Barnard, Ellenwood, & Hirshfeld, John Wiley and Sons, Vol. II, 1933.
77. "Heat Transfer to Vertical Evaporator Tubes" by E. Kirschenbaum, *V.D.I. Forschungshift* № 375, 1935.
78. "Tests of Marine Boilers" by H. Kreisinger, John Blizerd, A.B. Mumford, B.J. Cross, W.R. Argyle, & R.A. Sherman, U.S. Bureau of Mines, Bulletin 44, 1924, pp. 163–168.
79. "Tests on Models Concerning The Thermosyphonic Circulation in Bent TUBes and sectional Header Boilers" by K. Cleve, *V.D.I. Forschungshift*, № 322, 1929.
80. "Some Particulars of Design and Operation of Twin Furnace Boilers" by J. Blizzard & A.C. Foster, *Trans A.S.M.E.*, Aug. 1941, Vol. 63, № 6, p. 505.
81. "Isothermal Pressure Drop for Two-Phase, Two-Component Flow in a Horizontal Pipe" by R.C. Marintelli, L.M.K. Boelter, J.M. Taylor, E.G. Thomsen, & E.H. Morrin, *Trans A.S.M.E.*, Feb. 1944, Vol. 66, №2, p. 139.
82. "The Flow of a Flaming Mixture of Water and Steam Through Pipes" by M.W. Benjamin & J.G. Miller, *Trans A.S.M.E.*, Oct. 1942, Vol. 64, № 7, p. 657.
83. "Pressure Loss in Elbows and Duet Branches" by A. Vezsonyi, *Trans A.S.M.E.*, April 1944, Vol. 66, №3, p. 177.
84. "Boiling Film Heat Transfer Coefficients in a Long Tube Vertical Evaporator by O.W. Stroebe, E.M. Baker, & W.L. Bedger, *Industrial and Engineering Chemistry*, 1931, Vol. 31, p. 200.
85. "An Instrument for Indicating the amount of Gas in One-Liquid Mixtures" by B.R. Welsh & G.S. Peterson, *Trans A.S.M.E.*, July 1945, Vol. 67.
86. "A Comparison of Operation of Forced and Natural Circulation Boilers" by G.F. Ross & Leonard Wilkins, *Trans A.S.M.E.*, May 1946, Vol. 69, № 4.

87. "On the Velocity Distribution of Turbulent Flow in Pipes and Channels of Constant Cross Sections by C.-T. Wang, *J. Applied Mechanics*, A-95, June 1946, Vol. 13, No 9.
88. "Theoretical energy Losses in Intersecting Pipes" by J.C. Stevens, *Lefax Data Sheets*, Hydraulic Order No 16-46.
89. "Expansion Theory of Circulation in Water Tube Boilers" by R.F. Davis, *Engineering*, Feb. 1947, p. 147.
90. "The Viscosity of Water and Superheated Steam" by G.A. Hawkins, J.L. Solberg, & A.A. Potter, *Trans A.S.M.E.*, Vol. 57, 1935, p. 395.
91. "Temperature Drops and Liquid Film Heat Transfer Coefficients in a Vertical Tube" by R.M. Boarts, W.L. Badger, & S.J. Meisenberg, *Trans. Am. Inst. Chem. Eng.*, Vol. 33, No 363.
92. "Friction and Heat Transfer Coefficients" by W.F. Cope, *Proc. Inst. Mech. Eng.*, Vol. 137, p. 165.
93. "Boiling" by T.B. Drew & A.C. Mueller, *Trans. Am. Inst. Chem. Eng.*, Vol. 33, 1947, p. 449.
94. "Pressure Drop Accompanying Two-Component Flow Through Pipes by L.M.K. Boelter & R.H. Kepner, *Industrial and Engineering Chemistry*, 1939, Vol. 31, pp. 426-434.
95. *Mechanical Engineers Handbook* by R. Kent, (Power) John Wiley and Sons, 1935.
96. The unpublished notes of J. Blizard—TF 8, 43, 44, 45, dated April 1944, distributed within the Foster Wheeler Corp.
97. "The Maximum and Minimum Values of the Heat Transmitted from Metal to Boiling Water under Atmospheric Pressure" by S. Nukiyama, *J. Soc. Mech. Eng. Japan*, 1934, Vol. 37, PS-53.
98. "The Problems of Generating Pure Steam at High Pressures" by M. Frisch & R.A. Lorenzini, presented to the Eng. Soc. of Western Pennsylvania, April 30, 1948.