

# 1 Seismic Actions on Long Tunnels: Records from 1-g Shaking Table 2 Tests

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## 10 **Abstract**

11 This paper presents the current research progress in long tunnels subjected to earthquakes. Using the facilities of the  
12 multi-functional laboratory of the state-key laboratory, a series of large-scale shaking table tests were completed  
13 considering long tunnels under the excitation of travelling waves or junction structures, ground variations, tunnels  
14 crossing liquefiable ground, and fault sites under strong shaking. The test results were compared with numerical and  
15 analytical calculations to help understand this sophisticated problem. Several meaningful records can be used for the  
16 aseismic design of long tunnels and validation of the design formula.

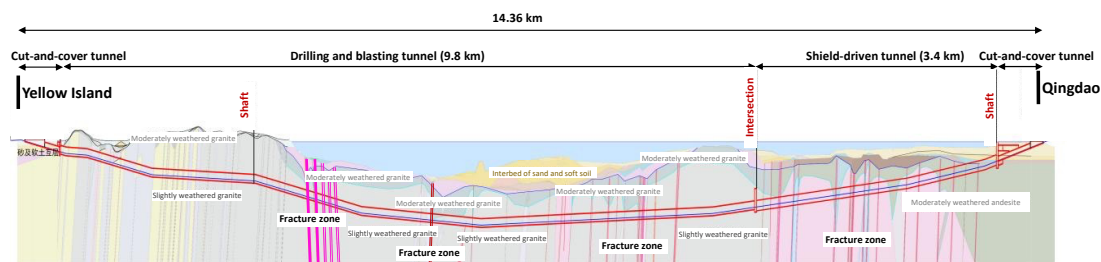
17 **Key words:** tunnel; travelling wave; variation of structure; site condition; liquefiable ground; fault; shaking table test

## 18 **1. Introduction**

19 The seismic design of underground structures enhances their resistance to damage during strong earthquakes<sup>1-3</sup>.  
20 Significant progress has been made in the past three decades to understand the seismic behavior of tunnels both  
21 experimentally and theoretically<sup>4</sup>.

22 Three types of seismic actions are enforced on tunnels (or underground structures), as identified in the review by  
23 John and Zahrah<sup>1</sup>. Specifically, (1) shaking deformation induced by strata vibration, (2) ground failures such as  
24 landslides or soil liquefaction, and (3) fault dislocation triggered by an earthquake.

25 The understanding of the seismic deformation gives analytical solution of ground deformation upon on tunnel. Most  
26 solutions, such as analytical analysis of elastic wave propagation and numerical simulation of vibration, can be verified  
27 under the transverse excitation of shaking table tests<sup>4</sup>. In this manner, a simplified approach can be applied to aseismic  
28 design, as documented by guidelines and codes<sup>5</sup>. The cross-sectional response of a tunnel is an idealized case of  
29 uniform excitation from a rigid bedrock. A long tunnel crosses sophisticated strata, as shown in Fig. 1, partially in rock  
30 strata that cross faults, soft ground, and even sand deposits that liquefy during strong earthquakes. However, these  
31 aspects have not been studied in detail.



32 **Figure 1** Jiaozhou Bay transpass.  
33

34 This paper presents a study on the three main actions of long tunnels with intensive 1-g shaking table tests, partially  
35 in contrast to analytical or numerical analysis of ground shaking deformation. The effects of discrepancy displacement  
36 owing to travelling waves, ground variations, and variation of stiffness of the tunnel were stressed correspondingly for  
37 the ground vibration action on the long tunnel. The action of ground liquefaction on the tunnel uplift was investigated in  
38 contrast to the free-field response, both on initial liquefaction and multiple shaking. Furthermore, experiments on  
39 tunnel-crossing faults have revealed a distinct dynamic response between the footwall and hanging wall.

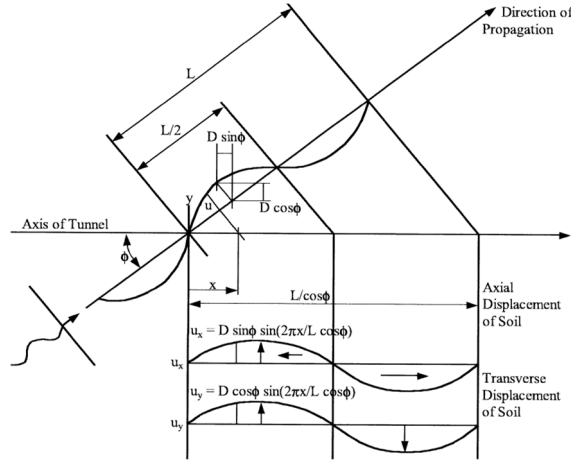
## 40 2. Deformation during earthquakes

### 41 2.1 Response under travelling wave

42 Long tunnels suffer non-uniform excitation of travelling waves even in uniform media if the length of the tunnel is  
 43 significantly larger than the wavelength of seismic propagation in the medium. Theoretical analysis of the displacement  
 44 response of uniform ground during shaking was proposed by Newmark<sup>6</sup> and Kuesel<sup>7</sup>. Free-field analysis ensures that  
 45 the seismic excitation is of the form of a sinusoidal function at a critical incident angle with respect to the axial  
 46 direction of the tunnel. A simplified analytical solution of the tunnel as an elastic beam subjected to the displacement of  
 47 free-field ground was deduced<sup>1-3</sup>. Theoretically, the displacement responses of the tunnel can be obtained by solving the  
 48 following differential equations

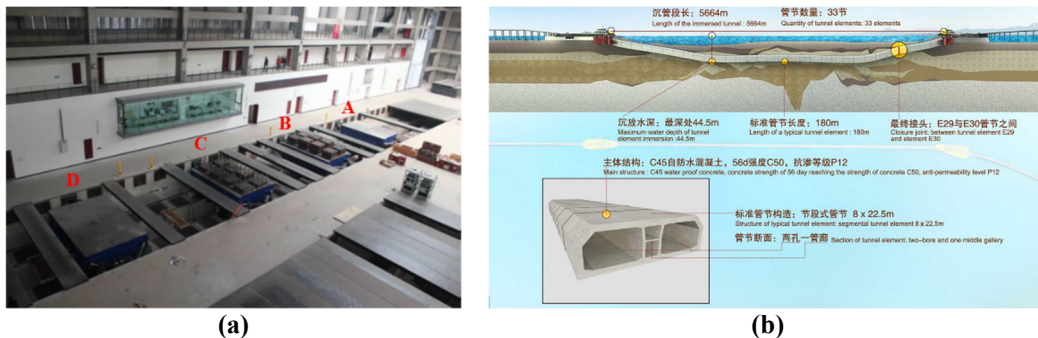
$$49 \begin{cases} EI \frac{d^4 v(x)}{dx^4} + k_t v(x) = k_t v_G(x) \\ EA \frac{d^2 u(x)}{dx^2} - k_a u(x) = -k_a u_G(x) \end{cases} \quad (1)$$

50 where  $EI$  and  $EA$  are the cross-sectional bending stiffness and axial stiffness per unit length of the tunnel, respectively;  
 51  $k_t$  and  $k_a$  are the vertical (lateral) and horizontal (axial) resistance factors of the foundation, respectively;  $v(x)$  and  
 52  $u(x)$  are the vertical and axial displacements of the tunnel at coordinate  $x$ , respectively; and  $v_G(x)$  and  $u_G(x)$  are the  
 53 vertical and axial displacements of the ground at coordinate  $x$ , respectively, under seismic action, as Fig. 2.  
 54 However, tunnels typically do not have portions, and the assumption of uniform stiffness is impractical. Furthermore,  
 55 ground variations cause the ground deformation to differ from an idealized sinusoidal formation.



56  
57 **Figure 2** Assumption of deformation action on longitudinal of tunnel.<sup>1-3</sup>

58 In the recorded ground movement during an earthquake, which is a random process. To obtain the response of a long  
 59 tunnel under a travelling wave input, a multi-shaking table test is a powerful tool. To transfer discrete vibration inputs  
 60 from an individual shaking table to the continuous propagation of shear waves in the modelled ground, a system should  
 61 be implemented using the sound principle. Based on the theory of elastic waves, an analytical solution for the dynamic  
 62 responses of a tunnel, simplified as a Euler beam, was deduced under an arbitrary loading process<sup>8</sup>. Using this  
 63 fundamental solution, a testing system with a shaking-table array, as shown in Fig. 3, was set up to simulate a travelling  
 64 wave<sup>9</sup>. This shaking array system has been successfully applied to immersed tunnels<sup>10</sup> and shield tunnels<sup>11</sup> to study the  
 65 dynamic responses of long tunnels under travelling waves.

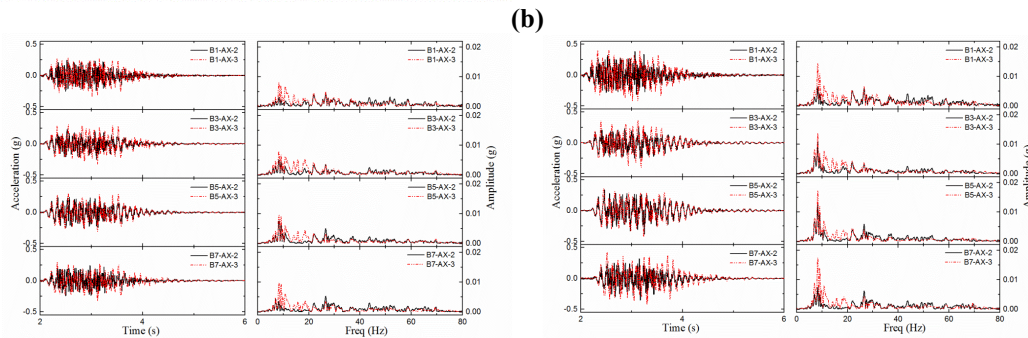
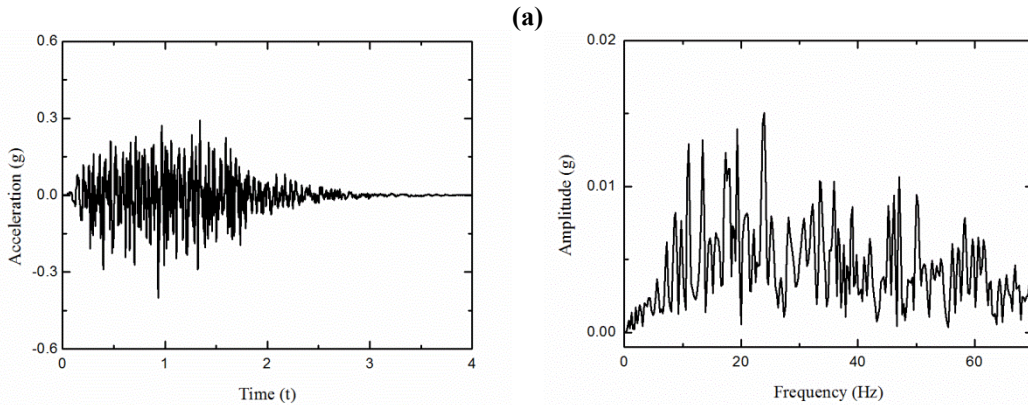
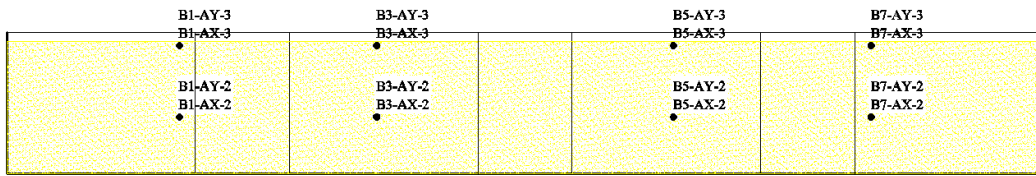


66 **Figure 3** Shaking-table array and testing of immersed tunnel<sup>10</sup>: (a) Shaking table array; and (b) Segments of HZM immersed tunnel.

67 **2.1.1 Free field responses with shaking table array**

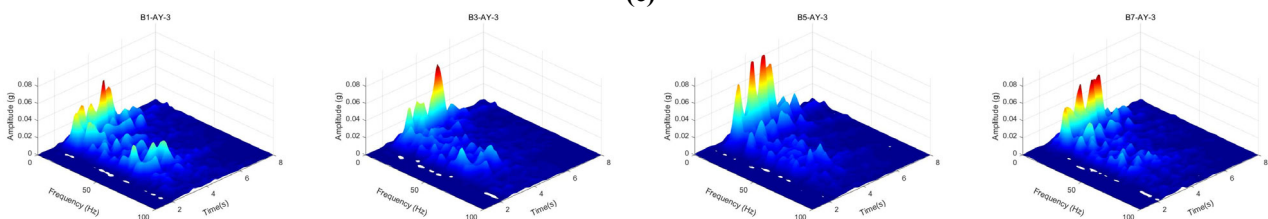
68 As a reference, the dynamic response of a free field (FF) under a travelling wave is of fundamental significance. A  
 69 scaled FF ground, as shown in Fig.4 (a), with the labels of the accelerometers was designed to test shear wave  
 70 propagation. The accelerometer was labelled in the manner of “B#-A\*-\*”, where # refers to Box location, \* means the  
 71 direction of input vibration (X-perpendicular to the sectional profile, Y-along the sectional profile), and @ indicates the  
 72 position (that is, -2 at the middle height, -3 at the surface of the ground), of an accelerometer. The input-excitation cases  
 73 are listed in Table 1. Here, SH01 means Shanghai synthetical motion as Fig. 4 (b) input from four tables simultaneously,  
 74 whereas N-SH01 indicates the same motion inputted from the far left to the far right tables in a travelling manner.

75 The recorded responses of each accelerometer under the inputs SH01 and N-SH01 are shown in Fig. 4 (c). It can be  
 76 observed that the acceleration response at the surface is dominant with respect to that in the middle of the ground,  
 77 whether under uniform or nonuniform excitation. Furthermore, the acceleration response of each box at the same  
 78 position is approximately identical under uniform excitation. This can be observed in the peak acceleration (PA) data  
 79 for each position listed in Table 2. In contrast, the delayed response in the sequential box is evident, as highlighted by  
 80 the Fourier spectrum in Table 3. Comparing Table 3 with Table 2, it can be seen that the PA under nonuniform  
 81 excitation is more prominent with respect to the PA under uniform excitation both at the middle and at the surface.  
 82 Figure 4 (d) presents the time/frequency spectrum at different locations. The spectrum varies in any domain of the  
 83 ground, which indicates that the impact of wave superposition varies with space during the propagation of the travelling  
 84 wave.  
 85



SH01

N-SH01



(d)

86 **Figure 4** Site responses under travelling wave: lateral excitation: (a) Scale FF ground; (b) Shanghai synthetical ground motion; (c)  
87 Acceleration responses (SH01 and N-SH01); and (d) Time/Frequency Spectrum: N-SH04.

88 **Table 1** Loading cases of shaking table tests: FF.

Input cases	SH01/N-SH01	SH02//N-SH02	SH03//N-SH03	SH04//N-SH04
Reference period(yr)	50	50	100	100
Probability of exceedance	10%	3%	10%	3%
PGA (g)	0.3	0.4	0.35	0.47
Predominate Frequency (Hz)	26.6	26.6	34.9	34.9

89 **Table 2** Peak acceleration response at each position (SH01).

		SH01	B1	B3	B5	B7
PA (g)	Inner	-0.256	-0.246	-0.250	0.244	
	Surface	-0.338	-0.327	-0.322	-0.325	
t <sub>p</sub> (s)	Inner	2.496	3.098	2.852	2.973	
	Surface	3.016	3.121	3.117	3.121	

90 **Table 3** Peak acceleration response at each position (N-SH01).

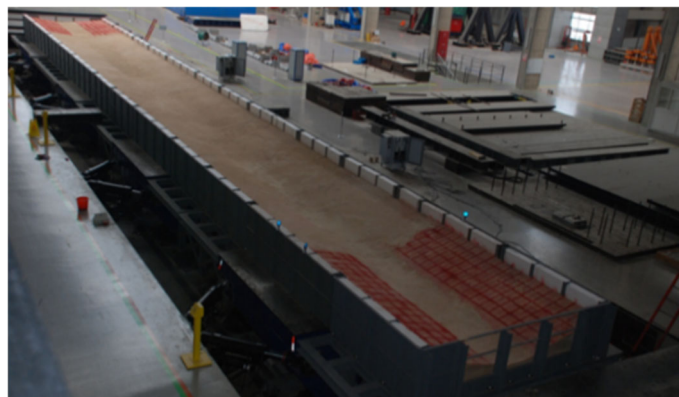
		N-SH01	B1	B3	B5	B7
PA (g)	Inner	0.38	0.27	-0.38	-0.35	
	Surface	-0.43	-0.42	-0.42	-0.42	
t <sub>p</sub> (s)	Inner	3.07	3.14	3.25	3.17	
	Surface	3.12	3.19	3.24	3.30	

91 **2.1.2 Slope site**

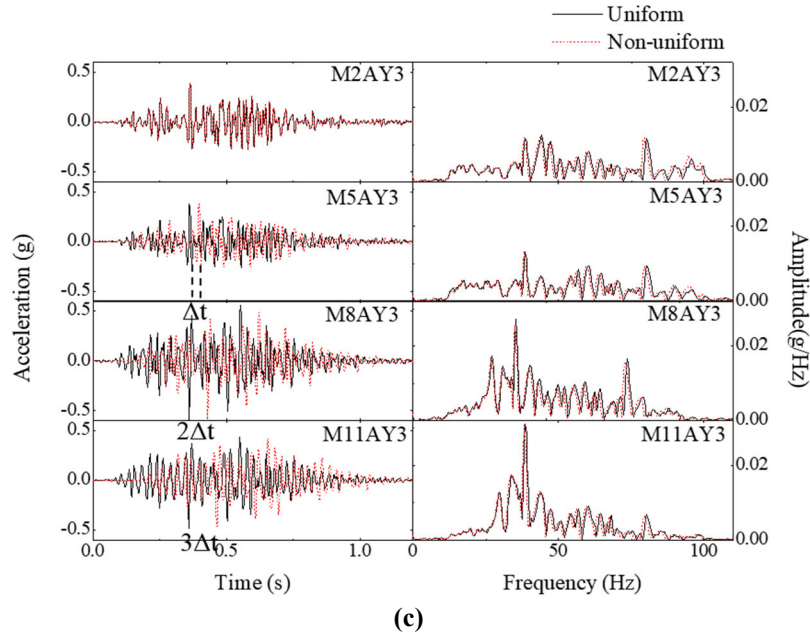
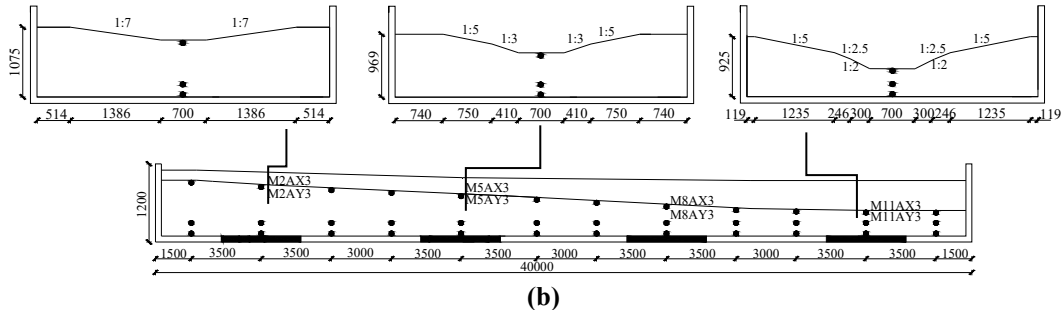
92 A slope site was modeled based on the prototype of the immersed tunnel of the Hong Kong–Zhuhai–Macau Bridge  
93 (HZM). Figures 5(a) and (b) show the slope site and the layout of the sensors, respectively. Table 4 lists the uniform  
94 and non-uniform excitations in the travelling mode, both with a peak ground acceleration (PGA) of 0.25 g. In Case DZ1,  
95 white noise was input to verify that the scaled ground model satisfied the similarity requirements. The acceleration  
96 responses observed at DZ2 and DZ3 are shown in Fig. 5(c). Compared with the test results gathered from Case DZ2, it  
97 is evident that the acceleration responses at each measuring point display significant discrepancies under non-uniform  
98 excitation in Case DZ3.

99 **Table 4** Loading cases of slope site.

Cases	PGA (g)	Motion	Excitation	Direction of vibration
DZ1	0.1	White noise	Uniform	Two ways
DZ2	0.25	Artificial motion	Uniform	Lateral
DZ3	0.25	Artificial motion	Non-uniform	Lateral (M2→M11)



(a)



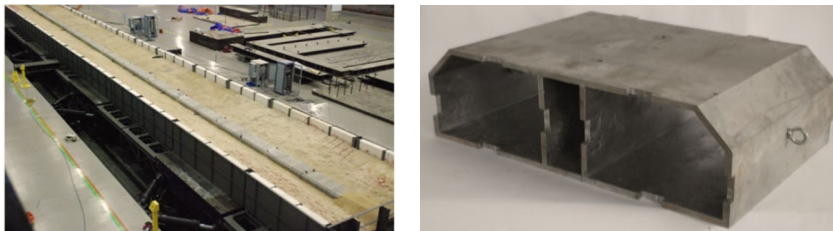
**Figure 5** Response of slope site : DZ2-uniform excitation and DZ3-travelling wave: **(a)** Slope site; **(b)** Layout of sensors; and **(c)** Acceleration responses: time histories and Fourier spectrum.

### 2.1.3 Response of immersed tunnel

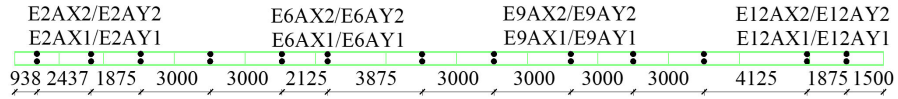
The scaled immersed tunnel was tested at the same slope site as described in Section 2.1.2, as shown in Fig. 6(a). This section presents the results for loading cases C01 and C02 under transverse excitation. The input artificial waves lasts 1.6 s, with a PGA of 0.25 g. Case C01 was subjected to uniform excitation, while case C02 experienced non-uniform excitation. Fig. 6(b) shows the sensor layout.

Figure 6(c) shows the acceleration responses of the tunnel and nearby sites under the C01 excitation. The results indicate that the peak responses of the tunnel are more pronounced than those of the surrounding soil, although they occur almost simultaneously in terms of the time histories and spectra. In the high-frequency domain, the tunnel played a dominant role in the interaction with the surrounding soil.

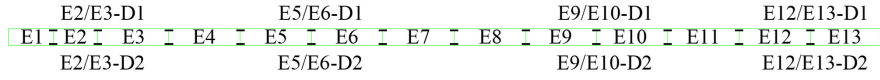
A comparison of the time histories and spectra of the acceleration between C01 and C02, as shown in Fig. 6(d), reveals no significant differences. However, the lateral displacement of the tunnel within the initial 0.15 s shows a clear distinction, as illustrated in Fig. 6(e). For C01, the tunnel moved nearly simultaneously toward one side. By contrast, the lateral displacement began with one tunnel section and propagated sequentially to the other sections in C02. Furthermore, the magnitude of the displacement in C02 was significantly larger, as depicted in Fig. 6(f). Joint dislocation occurred in a propagative manner, reaching the far end, even during the initial shaking period. This highlights the importance of accounting for nonuniform excitation in the seismic design of long tunnels.



**(a)**

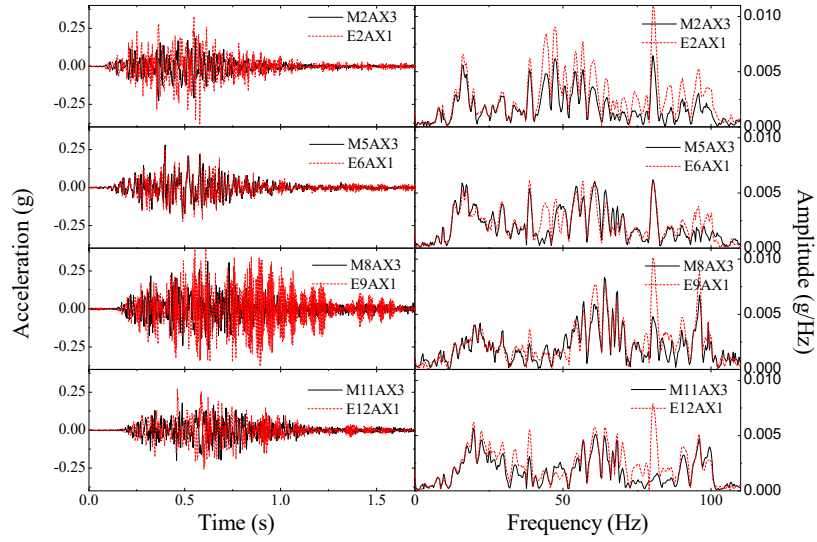


accelerometers

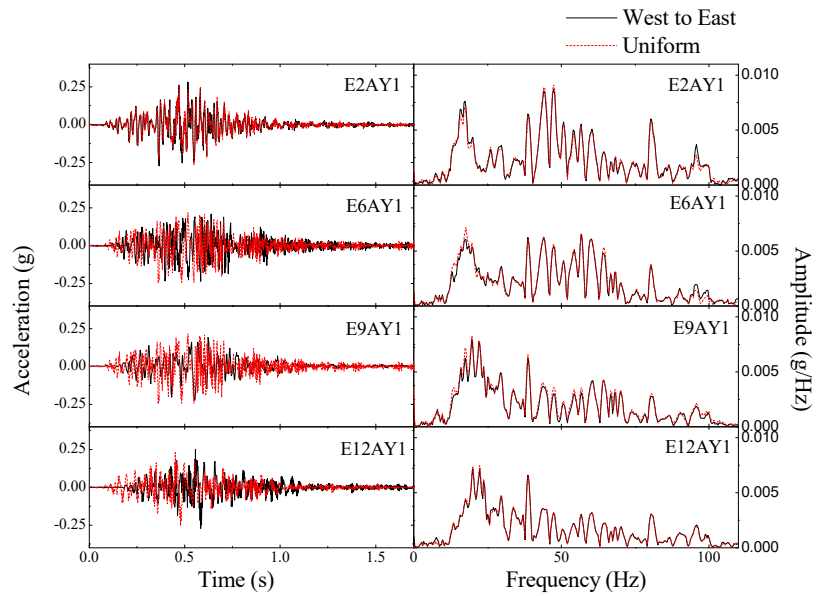


extensometers

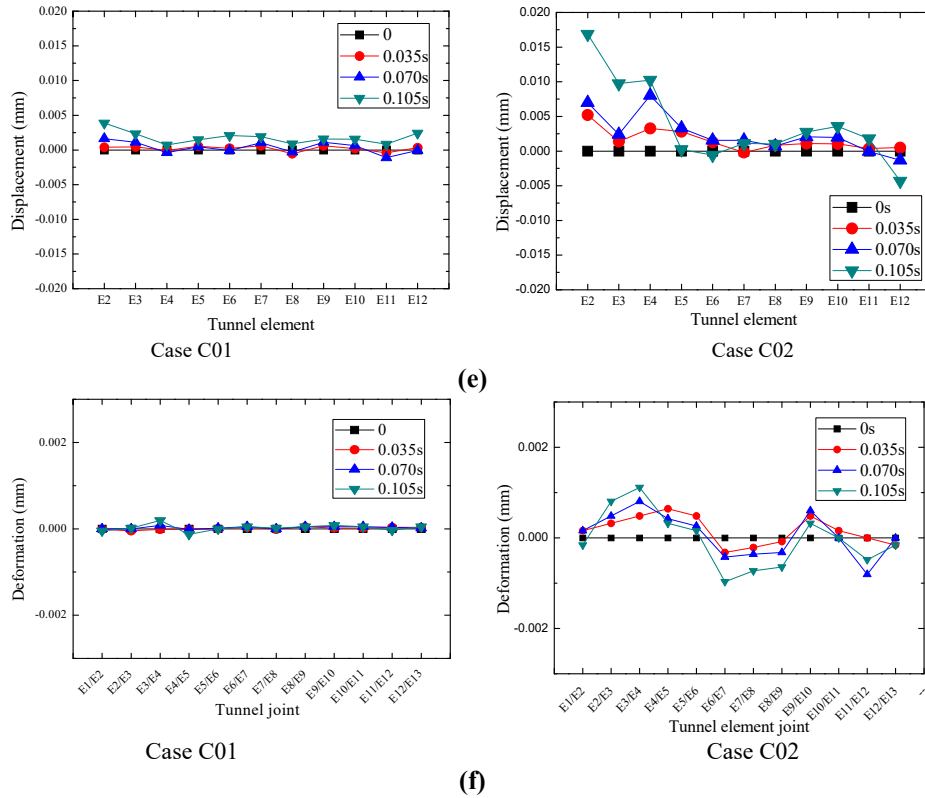
(b)



(c)



(d)



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**Figure 6** Dynamic responses of immersed tunnel: lateral excitation: (a) Scaled immersed tunnel; (b) Location of accelerometers and joint extensometers; (c) Case C01: Structure (red dot line, E); Soil (black line, M); (d) Structure: C01 (Uniform, dot line); C02 (Non-uniform: west to east, black line); (e) Lateral displacement (Case C01 and C02); and (f) Joint extension/closure (Case C01 and C02).

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## 2.2 Discrepant Responses due to Structural Variation

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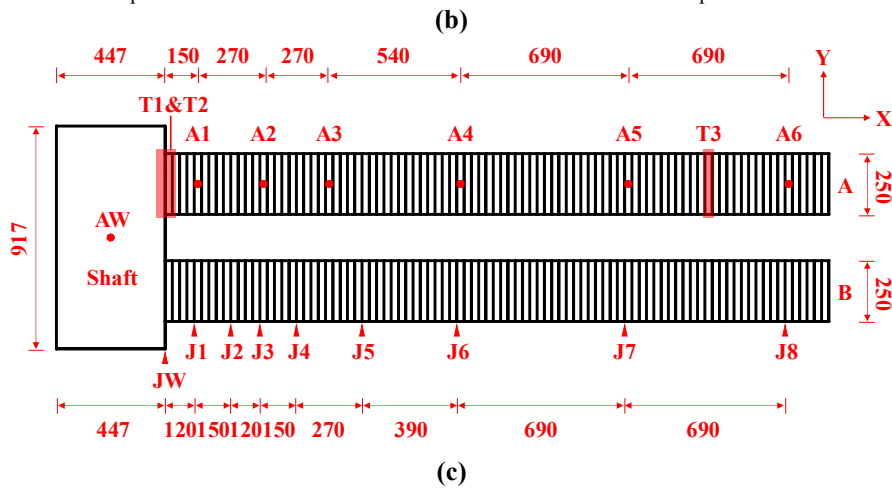
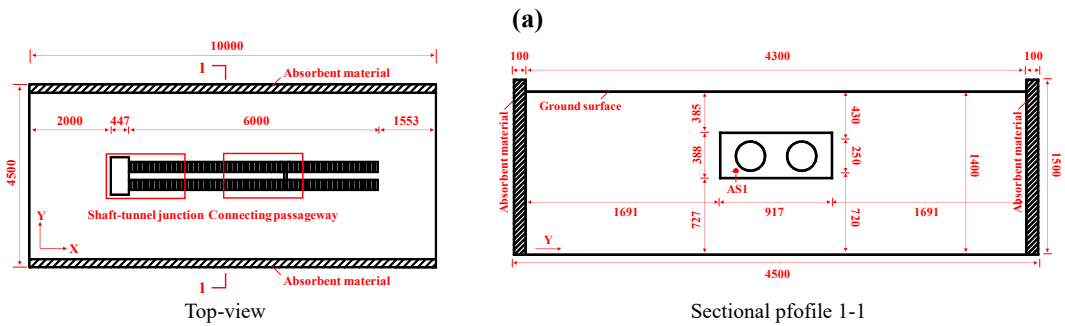
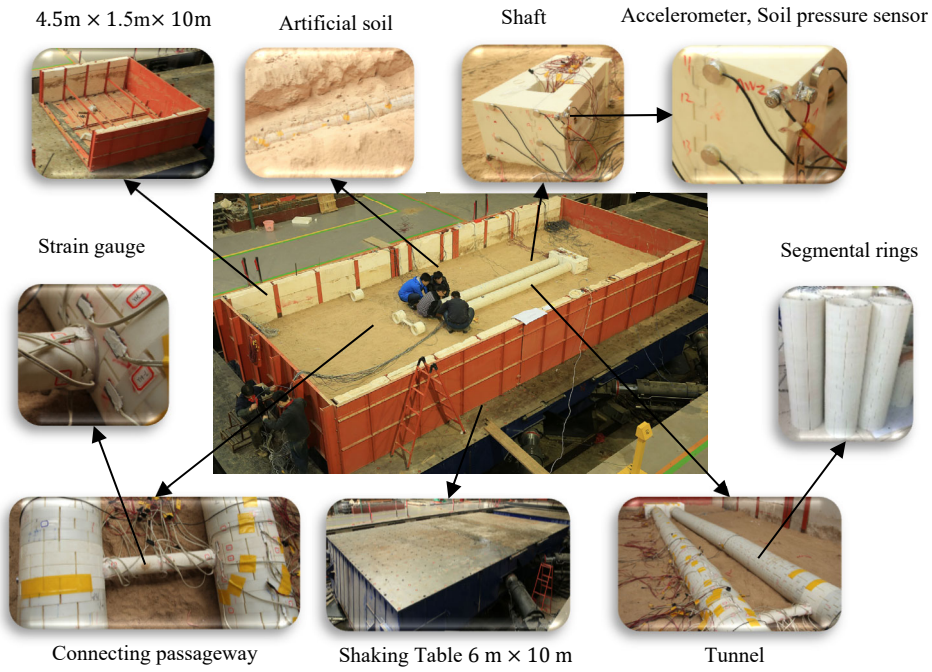
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A long tunnel presents discrepant responses even under uniform excitation under varying structural stiffness at a specified portion. As shown in Fig. 7(a), a large-scale shaking-table test was conducted on the conjunction structures between the shaft and tunnels and the connecting passageway between the two lanes of the tunnels<sup>12-14</sup>. Table 5 lists the primary test cases. The input excitations were similar to those used in the immersed tunnel, whose amplitudes were scaled up according to similitude relations. The table was shaken horizontally in the transverse and longitudinal directions of the tunnel. As illustrated in Fig. 7(b), the model of the conjunction structures was positioned at the longitudinal centerline of the container and buried at a depth of 385 mm. The following content of the subsection mainly focuses on the shaft-tunnel junction.

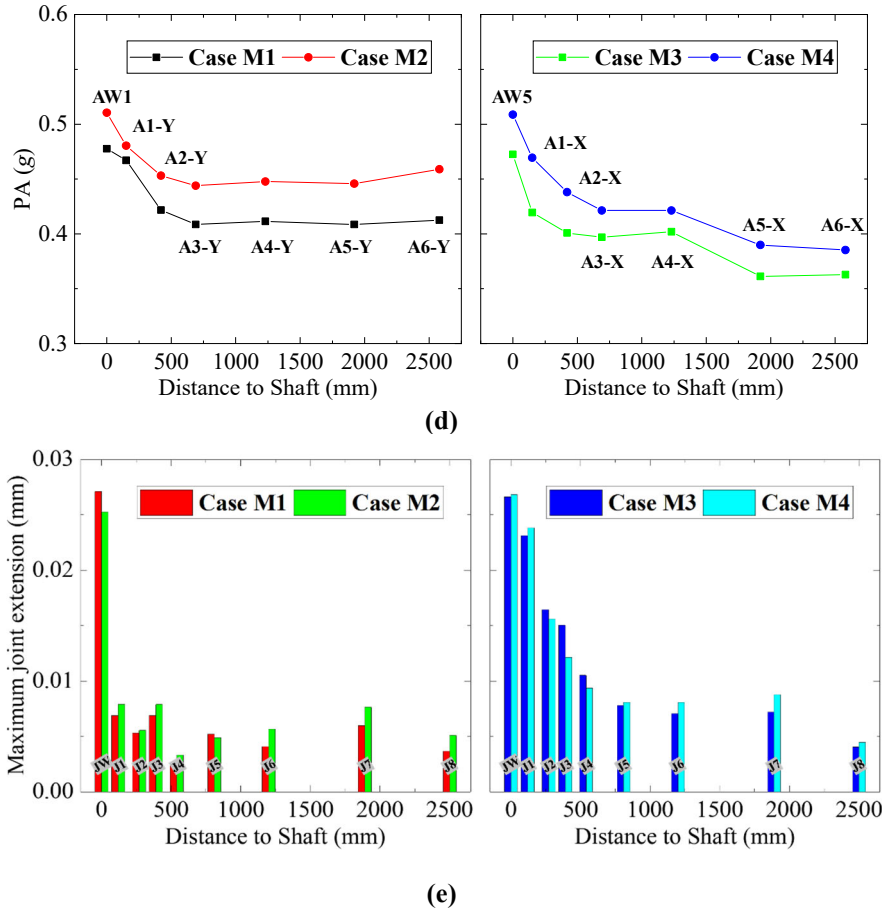
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**Table 5** Loading cases of shaking table tests: conjunction structures.

Input cases	M1	M2	M3	M4
Reference period (yr)	50	50	50	50
Probability of exceedance	10%	3%	10%	3%
PGA (g)	0.3	0.4	0.3	0.4
Predominate frequency (Hz)	26.6	23.9	26.6	23.9
Shaking direction	Transverse	Transverse	Longitudinal	Longitudinal







132 **Figure 7** Discrepant responses due to structural variation: experiments: (a) Set-up of model testing; (b) Layout of the conjunction  
 133 model (unit: mm); (c) Positions of sensors: accelerometers and joint extensometers; (d) Peak accelerations of the shaft-tunnel  
 134 junction; (e) Maximum joint extensions of the shaft-tunnel junction.

### 135 2.2.1 Discrepant responses of the tunnel

136 The model of the shaft-tunnel junction was heavily instrumented, as shown in Fig. 7 (c), where A # denotes the number  
 137 of accelerometers used and J denotes the number of joint extensometers. Discrepant responses were immediately  
 138 observed in the acceleration data. The peak accelerations recorded by the accelerometers are presented in Fig. 7(d). In  
 139 both the transverse and longitudinal shaking cases, the shaft was more sensitive to the input motion; therefore, it always  
 140 exhibited the largest peak acceleration. As the distance from the shaft increased, the recorded peak acceleration  
 141 decreased. The consequence of the discrepant accelerations is seen in the joint extension, which is similarly plotted in  
 142 Fig. 7 (e). As expected, the deformation was the largest at the connection of the shaft and tunnels, that is, JW, where the  
 143 discrepancy in acceleration was the most acute. For example, in Case M3, the extension at JW was approximately seven  
 144 times that at J8.

### 145 2.2.2 Dynamic analytical model of shaft-tunnel junction

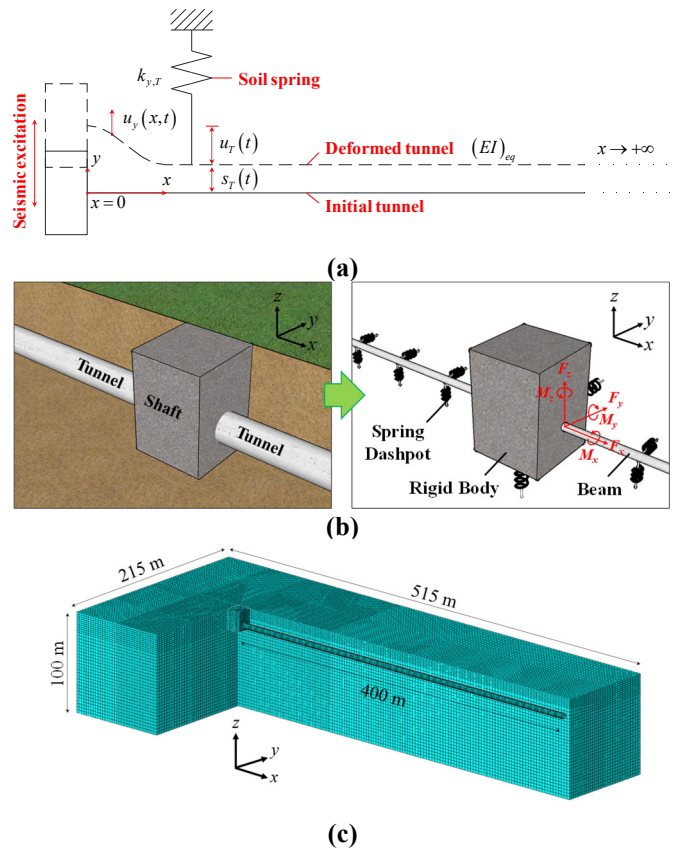
146 The test data of the joint extension can be interpreted using the classic beam-spring model for the tunnel. The  
 147 deformation mode for transverse shaking is shown in Fig. 8(a). The tunnel was primarily subjected to a longitudinal  
 148 bending deformation caused by its differential displacement relative to the shaft. Although this pseudo-static model can  
 149 predict the deformation of joint extensions with reasonable accuracy, it is inherently flawed because a) it neglects the  
 150 dynamic soil-structure interaction and b) the shaft-tunnel relative displacement is used as a known factor, which is  
 151 impossible in real applications. To overcome these flaws of the pseudo-static model, a more advanced dynamic  
 152 analytical model was developed for the shaft-tunnel junction<sup>15-18</sup>. As shown in Fig. 8(b), the tunnel was simplified into  
 153 a continuous Euler-Bernoulli beam, and the shaft was regarded as a rigid body. This implies that the shaft must be  
 154 sufficiently stiff to ignore the deformation. The surrounding soil is represented by a series of springs and dashpots  
 155 supporting the shaft and tunnel at one end and transmitting seismic motion at the other end. Thus, the dynamic soil-  
 156 structure interaction is mediated by springs and dashpots. In particular, the coefficients of the springs and dashpots on

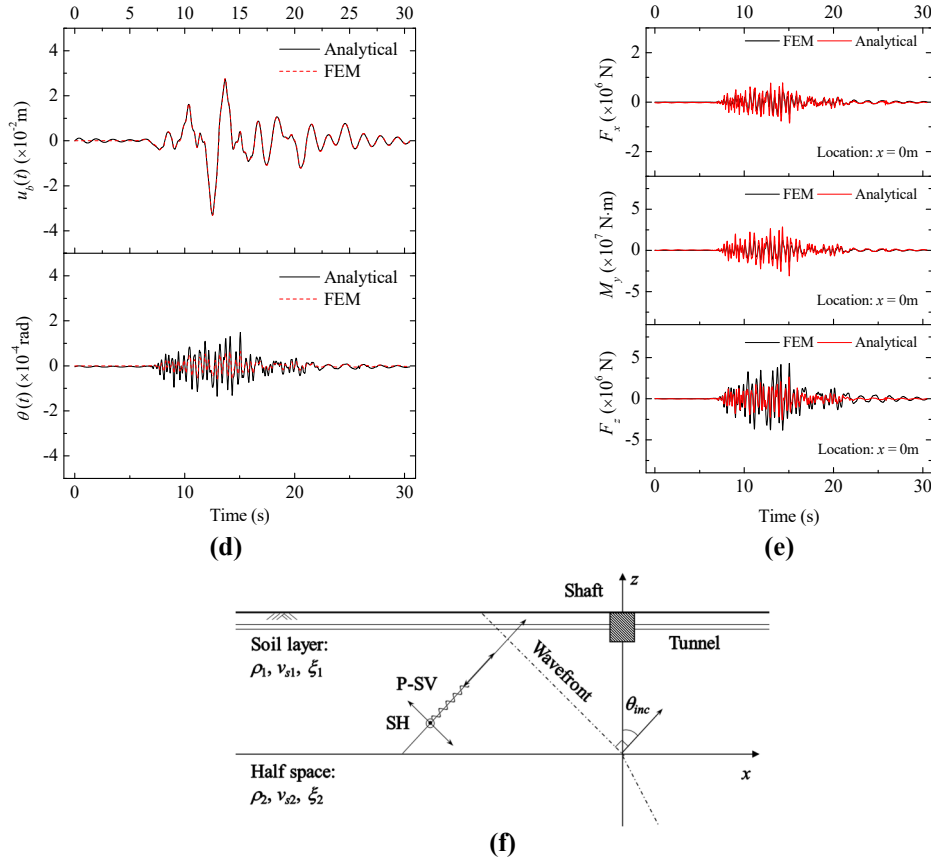
157 the shaft were determined using the foundation impedances for rigid caissons proposed by Gazetas<sup>19</sup>. An equation can  
 158 then be written for the shaft in the frequency domain in the form of

159 
$$(\tilde{\mathbf{K}} - \omega^2 \mathbf{M} + \mathbf{T})\mathbf{u} = \mathbf{P} + \mathbf{P}_T, \quad (2)$$

160 where  $\tilde{\mathbf{K}}$  is the complex stiffness matrix of the foundation;  $\omega$  is the angular frequency of the excitation;  $\mathbf{M}$  is the mass  
 161 matrix of the shaft;  $\mathbf{T}$  is the additional stiffness matrix of the tunnel;  $\mathbf{u}$  is the generalized unknown displacement vector  
 162 of the shaft;  $\mathbf{P}$  is the external loading vector caused by the seismic excitation;  $\mathbf{P}_T$  is the additional external loading  
 163 vector caused by the tunnel. Generally, the  $\tilde{\mathbf{K}}$  term, that is the stiffness of the surrounding ground, plays a dominant role.  
 164 The  $\mathbf{P}_T$  term is negligible; therefore, the tunnel primarily affects the shaft as an additional constraint via the  $\mathbf{T}$  term.  
 165 Once the displacements of the shaft are solved using this equation, the responses of the tunnel can be readily obtained  
 166 using the dynamic beam-spring theory.

167 To validate the proposed analytical solutions, a 3-dimensional finite element model of a shaft-tunnel junction  
 168 subjected to vertically propagating shear waves was constructed and computed, as shown in Fig. 8(c). The responses of  
 169 the shaft-tunnel junction under the same conditions were calculated using the analytical solutions. As demonstrated by  
 170 the comparisons in Figs. 8(d) and (e), the newly proposed analytical solutions yielded satisfactory results for the  
 171 displacements of the shaft and the internal forces of the tunnel.





172 **Figure 8** Discrepant responses due to structural variation: analytical models: (a) Pseudo-static model of shaft-tunnel junction subject  
 173 to transverse shaking; (b) Dynamic analytical model of shaft-tunnel junction.; (c) Finite element model for the validation of the  
 174 proposed analytical solutions; (d) Translational and rotational displacements of the shaft; (e) Internal forces at the connecting point;  
 175 and (f) Dynamic analytical model of shaft-tunnel junction subject to inclined plane wave.

### 176 2.2.3 Incorporation of travelling-wave effect

177 It has been extensively discussed in the previous subsection that non-uniform excitation is a major source of seismic  
 178 deformation in long tunnels. It is possible that a critical conjunction structure such as a shaft-tunnel junction is subject  
 179 to this type of seismic impact. As a special case of nonuniform excitation, the traveling wave effect of an inclined plane  
 180 wave was incorporated into the dynamic analytical model of the shaft-tunnel junction<sup>20,21</sup>.

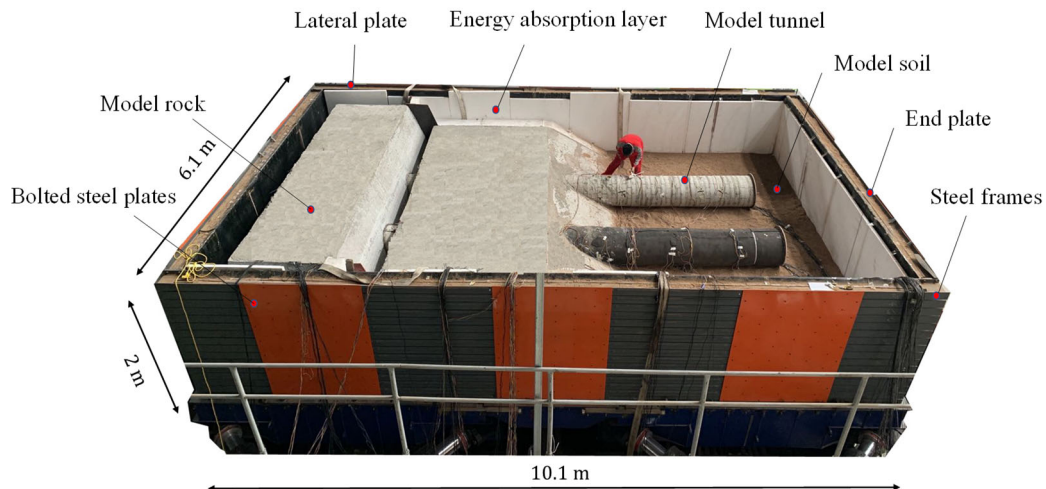
181 As illustrated in Fig. 8(f), the seismic motion was input in the form of inclined plane P-SV or SH waves. The ground  
 182 was modeled using a viscoelastic soil layer resting on the underlying half-space. The tunnel axis is oriented in the  
 183 direction of the horizontal wave propagation such that the traveling wave effect is most prominent in the tunnel. The  
 184 spatial displacement field is calculated using the stiffness matrix method for layered media<sup>22</sup>. The equation for the  
 185 displacement of the shaft remains the same as Eq. (2), only external loading vectors  $\mathbf{P}$  and  $\mathbf{P}_T$  depend on the  
 186 displacement field of the travelling wave. The solutions were also validated by the results of 3-dimensional numerical  
 187 computations, similar to those shown in Figs. 8(a), (b), and (c).

188 Because the shaft generally has limited dimensions, it is less affected by the traveling wave effect. In contrast, the  
 189 displacements of the tunnel are the superpositions of the shaft displacements and the ground displacement. The  
 190 influence of the shaft decreased exponentially as the distance from the shaft increased. When the distance is sufficiently  
 191 large, the response of the tunnel is dominated by the propagation of the travelling wave.

### 192 2.3 Variation of Strata

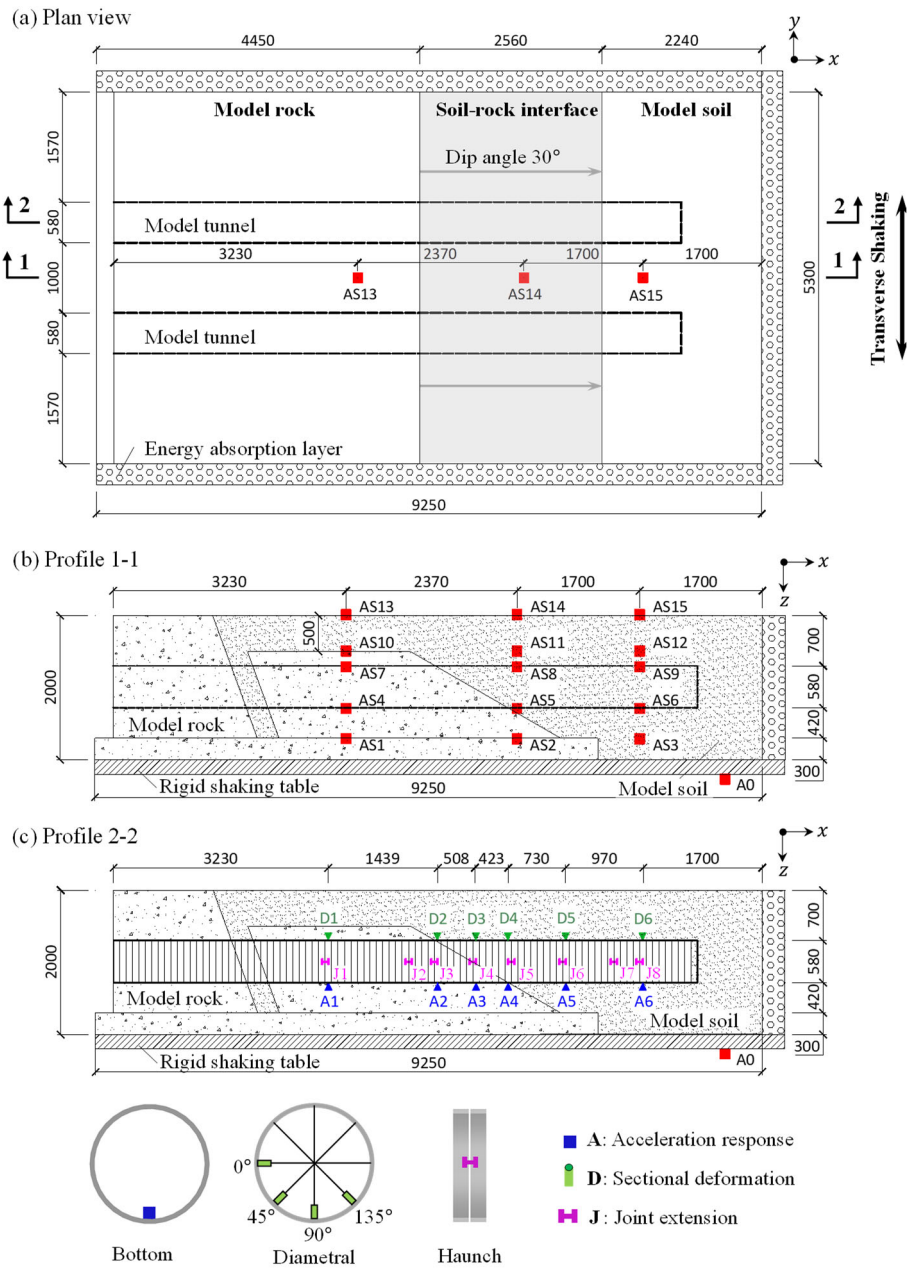
193 A long tunnel expresses discrepant responses at the location where it crosses the strata, with significant differences in  
 194 geological deposits. Fig. 9 shows the test results for the tunnels crossing the soil-rock interface. This typical seismic  
 195 scenario was simulated using a large-scale shaking table test considering the relative stiffness of the ground tunnel as  
 196 the dominant factor. Accordingly, a refined segmental lining was designed to mimic the structural features of the  
 197 prototype shield-driven tunnel. Transverse and longitudinal excitations, including artificial, real, and sinusoidal waves,  
 198 were applied. Initially, the local site effect was analyzed using a free-field model to characterize spatial site conditions.

199 The resulting discrepant responses of the embedded tunnels were examined. The following section presents an  
200 analytical method for addressing the combined effects of variations on both site and structure.



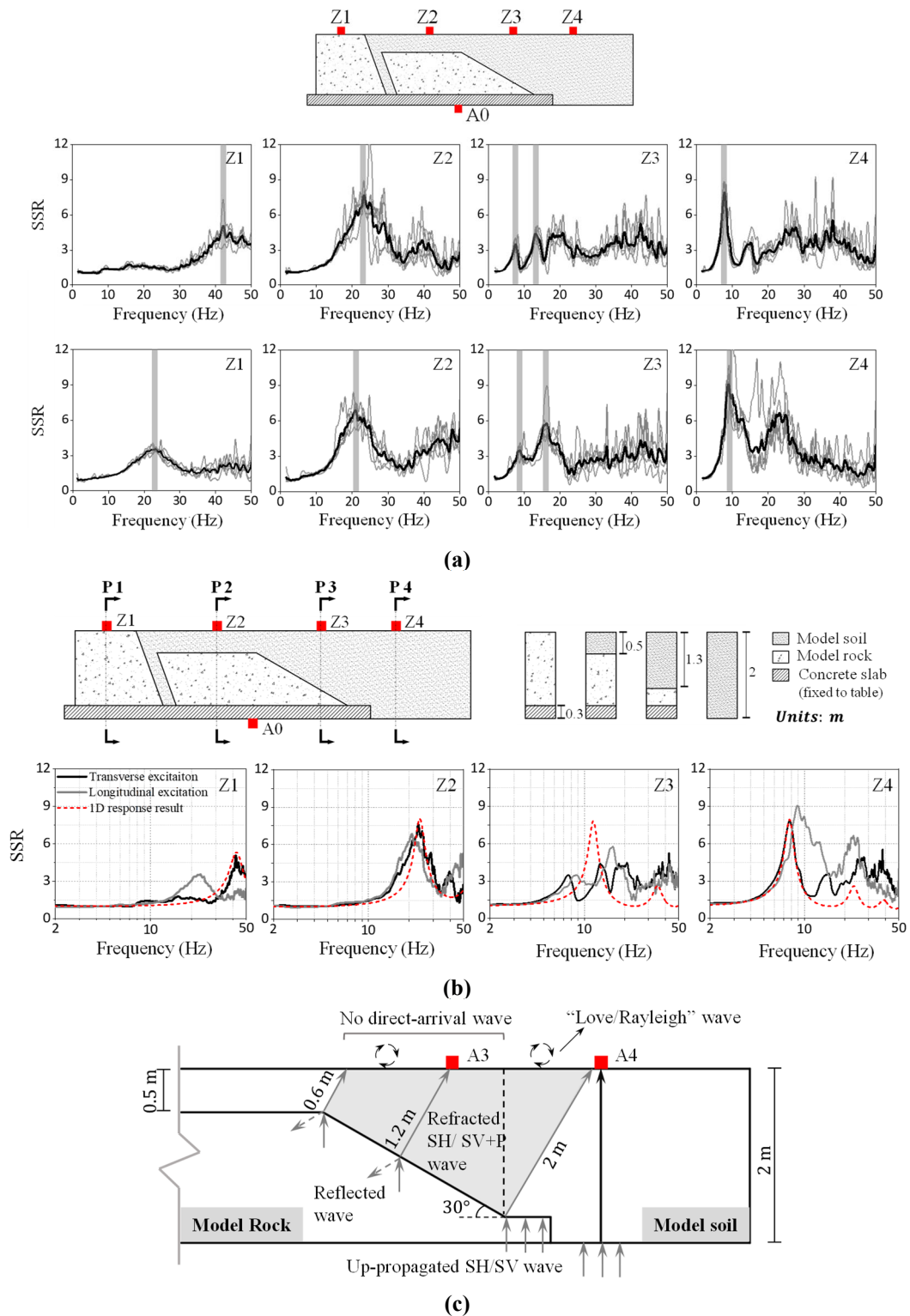
201 **Figure 9** Shaking table test of tunnel crossing soil-rock interface.

202 The dynamic responses of the tunnel in the soil-rock strata were studied according to the instrument scheme, as  
203 shown in Fig. 10. There are 15 accelerometers aligned as a matrix in the vertical longitudinal center plane, namely,  
204 AS1–AS15 in Profile 1-1. A0 was attached to the shaking table to record the actual output. The twin tunnels were  
205 placed symmetrically in the soil-rock strata, with a clear spacing of 1 m and buried depth of 0.7 m. Three types of  
206 sensors were used in the model tunnel. Six accelerometers, numbered A1–A6, were installed at the bottom of the model  
207 tunnel. Linear variable displacement transducers were arranged on six lining rings, labelled D1–D6, to monitor the  
208 sectional deformation along four diametral directions. The extensions of the eight circumferential joints were also  
209 measured using displacement gauges J1 to J8. The following discussion mainly focuses on cases of transverse  
210 sinusoidal excitation.



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**Figure 10** Instruments on the ground-tunnel model: (a) plan view; (b) Profile 1-1: sensors in the model ground; and (c) Profile 2-2: sensors on the model tunnel (Unit: mm).



214 **Figure 11** Local site effect: (a) Micro-zones; (b) Comparison of SSR results between the experimental and 1D response; and (c)  
 215 Mechanism of wave propagation at the interference.

216 **2.3.1 Local site effect of the soil-rock strata**

217 The standard spectral ratio (SSR) method was used to identify site characteristics. The SSR refers to the spectral ratio of  
 218 a single record to that of a reference-site record<sup>23</sup>. The first peak of the SSR corresponds to the fundamental frequency,  
 219 and its amplitude refers to the amplification effect with respect to the reference site. As shown in Fig. 11(a), the site was  
 220 separated into four micro zones to install the accelerometers, denoted as Z1–Z4, and the signals collected at the shaking  
 221 table were used as the reference record A0. Fig. 11(a) shows the average SSR results caused by five earthquake

222 sequences excited along both the transverse and longitudinal directions. All results clearly imply a spatial variety of site  
 223 characteristics caused by the undulation of the underlying bedrock.

224 To clarify the local site effect caused by variations in strata conditions, the experimental results were compared with  
 225 the one-dimensional response results, assuming uniform site conditions. The 1D responses can be theoretically  
 226 calculated using Kramer's method<sup>24</sup>:

$$227 \quad SSR = \frac{1}{\cos k_1 h_1 \cos k_2 h_2 - \alpha \sin k_1 h_1 \sin k_2 h_2} \quad (3)$$

$$228 \quad \alpha = \rho_1 V_{d1} / \rho_2 V_{d2} \quad (4)$$

$$229 \quad V_{dn} = V_{sn}(1 + i\xi_n); (n = 1,2) \quad (5)$$

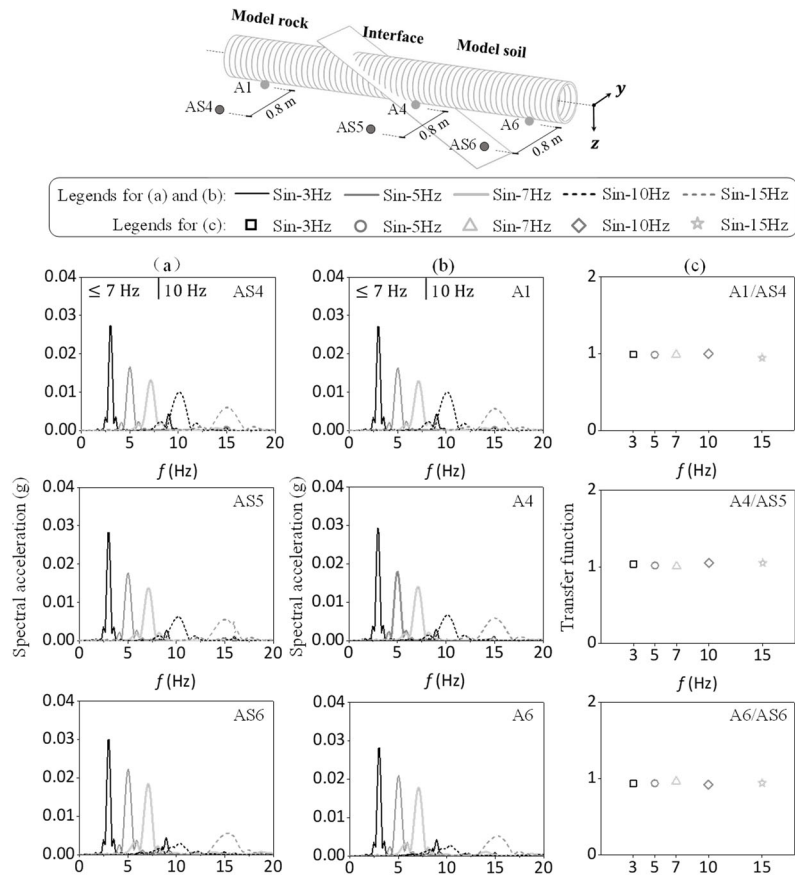
$$230 \quad k_n = 2\pi f / V_{dn}; (n = 1,2), \quad (6)$$

231 where  $V_{s1}$  and  $V_{s2}$  are the shear wave velocities of model soil and model rock, respectively;  $i = \sqrt{-1}$ ;  $h_1$  and  $h_2$  are the  
 232 thickness of model soil and model rock, respectively;  $\xi_1$  and  $\xi_2$  are the damping ratios of model soil and model rock,  
 233 respectively;  $\rho_1$  and  $\rho_2$  are the densities of model soil and model rock, respectively; and  $f$  is the excitation frequency.  
 234 The experimental and calculated results are compared in Fig. 11(b). They fit well in the Z2 zone, indicating only a 1D  
 235 response. Nevertheless, there are two anomalous phenomena when examining the local site effects in Z3 and Z4. One  
 236 was the double peak observed at Z3 and its complete mismatch with the 1D response. The other is an additional  
 237 amplification in a specific frequency range at Z4. This can be attributed to the scattered wave generated at the strata  
 238 interface, which causes an interference effect with the up-propagating waves<sup>25</sup>, as illustrated in Fig. 11(c). Local site  
 239 conditions are likely to cause nonuniform soil–structure interactions when a long tunnel crosses the soil–rock interface.

### 240 2.3.2 Dynamic responses of the tunnel in soil-rock strata

241 Figure 12 shows the spectral acceleration of the three accelerometer pairs as well as their transfer functions (TFs). TF is  
 242 defined as the tunnel-to-ground spectral ratio. As shown in Fig. 12(c), all the TF values were close to 1, indicating  
 243 nearly identical movements of the tunnel and surrounding ground. Given that the strata behave differently on either side  
 244 of the interface, these discrepancies could be transferred to the tunnel. For example, as shown in Figs. 12(a) and (b),  
 245 when the excitation frequencies were lower than 7 Hz, the soil responded more intensely than the rock. These results  
 246 were reversed when the excitation frequency was increased to 10 Hz.

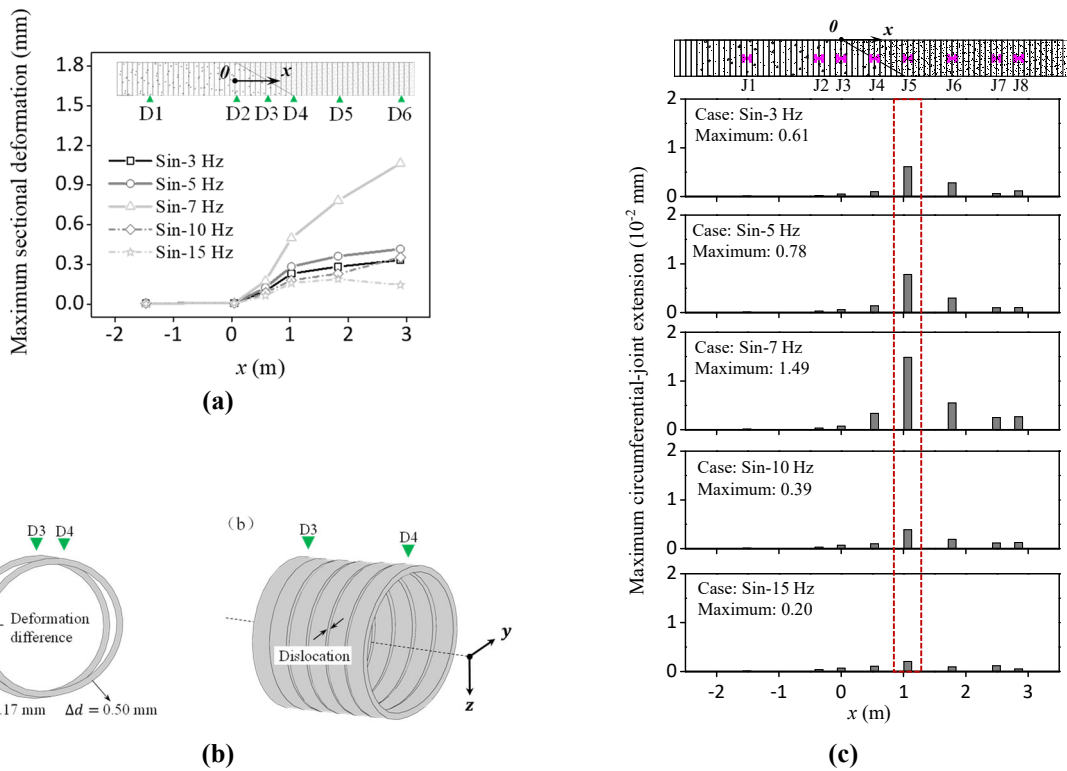
247 These discrepancies may reflect both the sectional deformation and joint extension of the tunnel. The maximum  
 248 sectional deformations of each section were collected from D1 to D6, and the results are shown in Fig. 13(a). The  
 249 deformations between D1 and D2 are relatively negligible, but they become significantly larger in the soil deposit, with  
 250 a maximum of 1.06 mm at D6 in the Sin-7 Hz case. The sharp increase in sectional deformation from the rock stratum  
 251 to the soil deposit, exemplified by D3 and D4 in Fig. 13(b), is likely to induce significant transverse dislocations  
 252 between adjacent lining rings near the soil-rock interface. Longitudinally, the segmental tunnel mostly coordinates  
 253 discrepant movement between soil and rock strata through the joints. Thus, the largest extension of the circumferential  
 254 joint is expected to occur near the interface, where the relative displacement between the two strata is the most acute.  
 255 The results aligned with this expectation, as shown in Fig. 13(c). In each excitation case, the largest extension always  
 256 occurred near the soil–rock interface at J5. When the excitation frequency was 7 Hz, which was close to the  
 257 fundamental frequency of the model soil, the significant relative displacement between the soil and rock led to an  
 258 extreme joint extension value.



259

260

**Figure 12** Acceleration responses of the ground-tunnel mode: (a) ground; (b) tunnel; and (c) tunnel-to-ground transfer functions.



261

262

**Figure 13** Displacement and deformation: (a) Maximum sectional deformations from D1 to D6; (b) Deformation difference between D3 and D4; and (c) Maximum circumferential-joint extensions.



263 **3. Tunnel in Liquefiable Ground**

264 **3.1 n-g Tests**

265 A tunnel crossing the ground with liquefiable soil is unavoidable. Case investigations have reported the uplifting or  
 266 damage of underground structures after earthquakes. To reveal this situation, the mechanism and potential numerical  
 267 simulation of ground liquefaction have been studied, first in the VELACS project<sup>26</sup> and then in LEAP<sup>27</sup>. Recently  
 268 Mudahusai at al.<sup>28</sup> investigated the potential uplift of a tunnel with a centrifuge facility. At the elemental level, Seed and  
 269 Idris<sup>29</sup> provide proof of liquefaction. However, directly applying the results of element tests to a real project remains a  
 270 challenging task because the physical properties of soils vary with the dimensions of the ground, even if they comprise  
 271 uniform liquefied saturated soil.

272 **3.2 1-g Tests**

273 A temptation to reveal the mechanism of underground structures in liquefiable ground (TUNLIQ) was recently  
 274 conducted by a joint Sino-German team. One of the tasks was to develop 1-g shaking-table tests for both free-field and  
 275 site-structure models. To achieve a reasonable goal, a new laminar container was developed<sup>30</sup>.

276 Two tests were conducted on the same liquefiable ground prepared by dry pluviation followed by water saturation.  
 277 The only difference between the two tests was the loading frequency, as listed in Table 6.

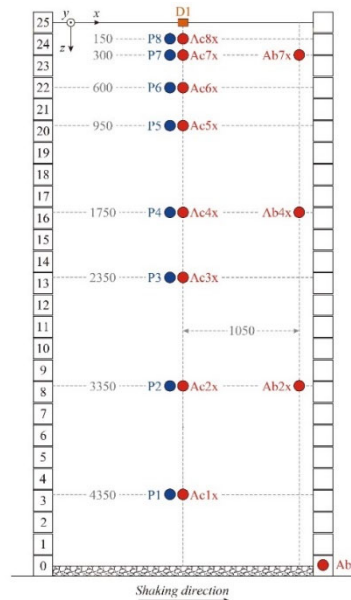
278 **Table 6** Loading cases of shaking table tests: liquefaction of the free-field model.

Test No.	Shaking Event	Frequency (Hz)	PBA (g)	Cycles	Notes
Test 1	T1-E1	2	0.15	20	
Test 2	T2-E1	4			

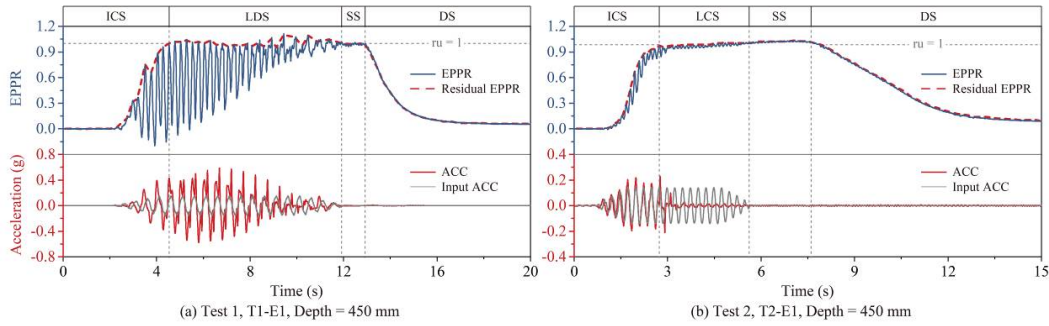
279



(a)



(b)



280  
281

**Figure 14** Liquefaction of saturated sand ground: **(a)** Shaking table test for liquefiable ground; **(b)** Instrumentation layout; and **(c)** Time history of EPPR and acceleration at a location 450-mm below ground.

282

To capture the characteristics of the model ground, sensors including accelerometers and pore pressure gauges were positioned at the target locations, as shown in Fig. 14 (b). The recorded excess pore water pressure (EPWP) can be expressed as the excess pore pressure ratio (EPPR). The time history of the EPPR at the specified observation point can be drawn and matched with the recorded acceleration at the corresponding location and the input acceleration from the table, as shown in Fig. 14(c), for the location 450-mm below the ground. It can be seen that there are distinct behaviors of liquefaction between the two tests, although the only difference is the frequency of excitation.

287

To manifest the phenomenon, liquefaction can be divided into the following stages:

288

(1) Initial contractive stage (ICS): characterized by predominantly contractive behavior of the soil skeleton and the corresponding accumulation of EPWP in saturated soil. Under cyclic loading, the response of the EPPR exhibits a spiked shape. The positive part of a spike indicates the contraction of the soil skeleton, whereas the negative part implies the dilation of the soil. The transition from the ICS to the subsequent stage occurs once the residual EPPR reaches 1.0. From Fig. 14 (c), the larger oscillation of the EPPR in Test 1 indicates that both the contraction and dilation of the soil under a lower frequency are stronger than that in Test 2, as shown in Fig. 14(c). Correspondingly, the amplitude of the acceleration in Test 1 was more pronounced and lasted for more cycles than that in Test 2.

294

(2) Liquefied dilative stage (LDS): Under cyclic shearing, the soil experiences alternating contractions and dilations, while the EPPR remains approximately 1.0. At this stage, the soil skeleton loses and regains its shear stiffness throughout the repeated contractive-dilative cycles, which facilitates the development of large strains. This type of liquefaction is referred to as ‘cyclic mobility’ liquefaction. It should be noted that the LDS was developed only in Test 1.

299

(3) Liquefied contractive stage (LCS): represents contraction-dominated soil behavior with minimal dilation spikes during continuous cyclic loading. When the effective stress was maintained at zero, the soil loses its strength completely and becomes flowable. Thus, the liquefaction that occurred in LCS is defined as ‘cyclic instability,’ which is only observed in Test 2.

304

(4) Seepage stage (SS): the stage when the EPPR maintains at 1.0 after the LDS or LCS although there is no input of excitation. This stage was encountered only in shallow areas and can be attributed to the continuous supply of pore water by the upward seepage of pore water from deeper zones. The SS period in Test 2 was longer than that in Test 1.

307

(5) Dissipation stage (DS): primarily characterized by the dissipation of the EPWP. Clearly, the DS of Test 1 was significantly shorter than that of Test 1.

309

It can be concluded from the above discussion that ‘cyclic instability’ of ground will result from high-frequency excitation but ‘cyclic mobility’ from low-frequency excitation.

311

### 3.2.1 Free-field liquefaction under multiple shakings

312

Previous field observations and model tests have shown that the resistance of a field to liquefaction can vary significantly under multiple shaking events. To investigate the effect of frequency on the liquefaction behavior of soil deposits during consecutive earthquakes, two parallel 1-g shaking table tests were conducted. Identical soil models comprising Fujian medium sand were prepared in the biLSB using a sand pluviator, as shown in Fig. 14 (a), where four identical excitations were applied sequentially after the excess pore pressure from the previous events had fully dissipated. The only difference between the two tests was the loading frequency.

317

To facilitate a comparison of liquefaction resistance between liquefied and non-liquefied areas, two factors were analyzed: the liquefaction resistance was defined by  $N_L$ , representing the number of loading cycles required to trigger the initial liquefaction. In non-liquefied areas, the resistance is indicated by the maximum excess pore pressure  $r_{u,max}$ . Fig. 15 shows a comparison of the liquefaction resistance across each shaking event.

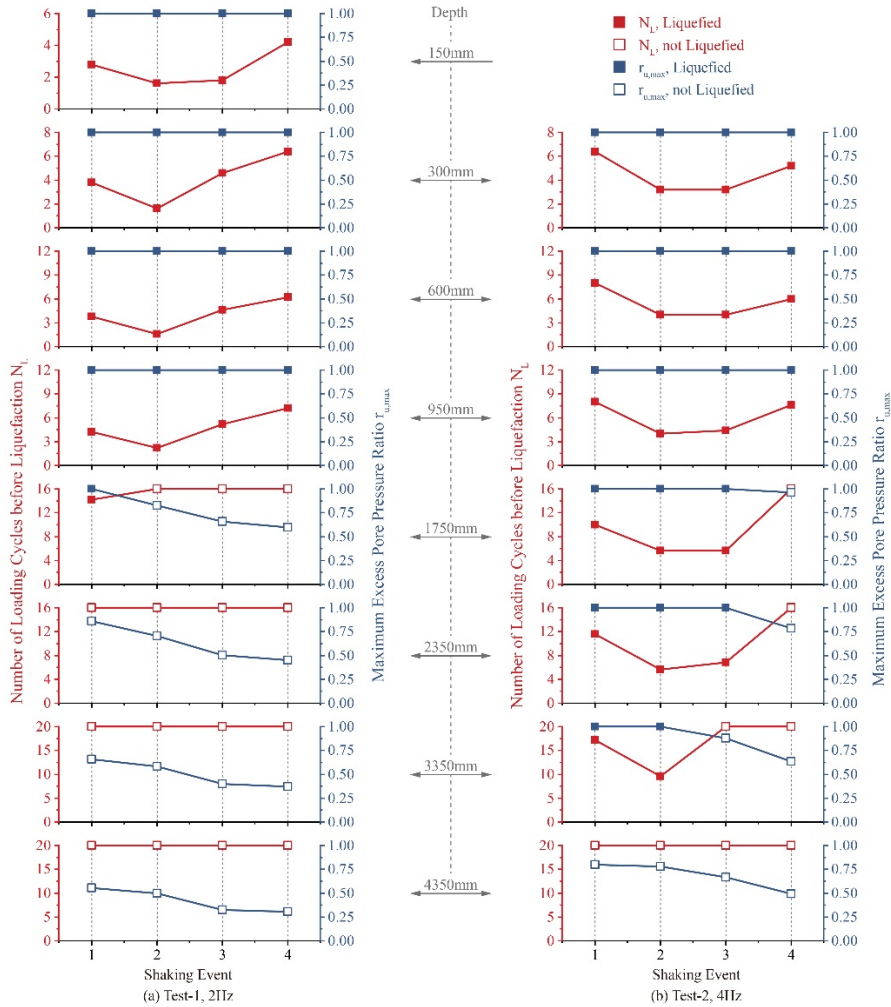
322

In the first shaking event, a comparison of  $N_L$  revealed that fewer loading cycles were required to trigger liquefaction at lower loading frequencies. However, a higher loading frequency induced liquefaction across significantly deeper

324

325 zones. These differences were attributed to the compound effects of the loading frequency, which influenced both the  
 326 local loading amplitudes and relative drainage conditions. Despite variations in soil behavior, the evolution of  
 327 liquefaction resistance across multiple shaking cycles was consistent in both tests: the resistance to reliquefaction in the  
 328 liquefied area significantly decreased during the second shaking event and began to recover from the third event onward,  
 329 whereas the resistance in the unliquefied area increased monotonically with each event.

330 In conclusion, it is crucial to consider the frequency effect of the input motion on the dynamic response of a soil  
 331 deposit during earthquakes. For liquefiable soil layers, which often coincide with the depths of the underground  
 332 transportation infrastructure, aftershocks may cause more severe damage because the field resistance to liquefaction can  
 333 be further reduced even after the initial liquefaction has occurred.



334 **Figure 15** Liquefaction under multiple shakings: (a) Test-1, 2 Hz; and (b) Test-2, 4 Hz.  
 335

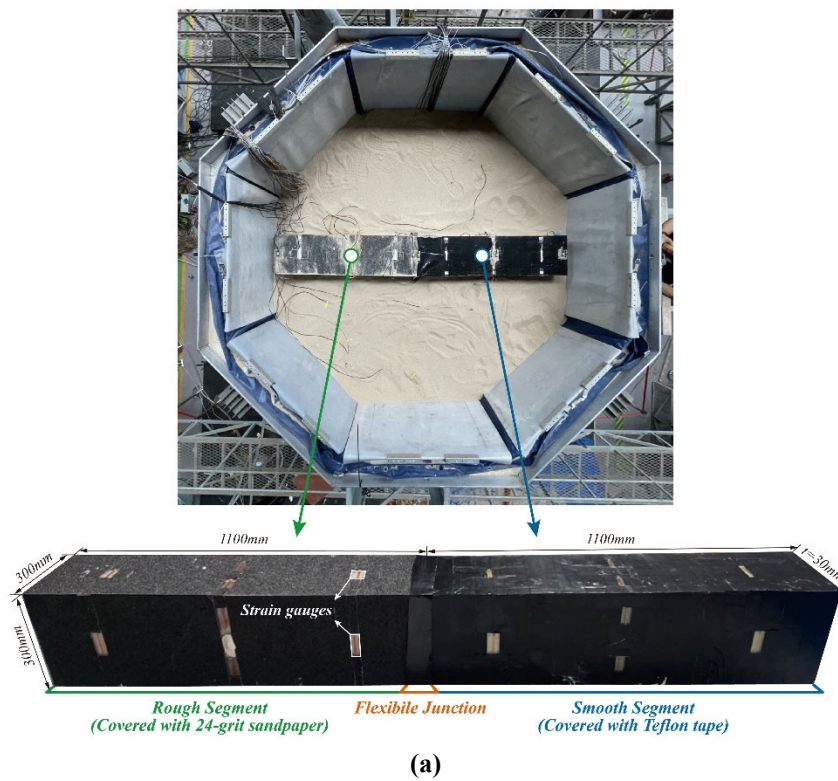
336 **3.2.2 Distinct tunnel uplifting behavior during liquefaction under multiple shakings**

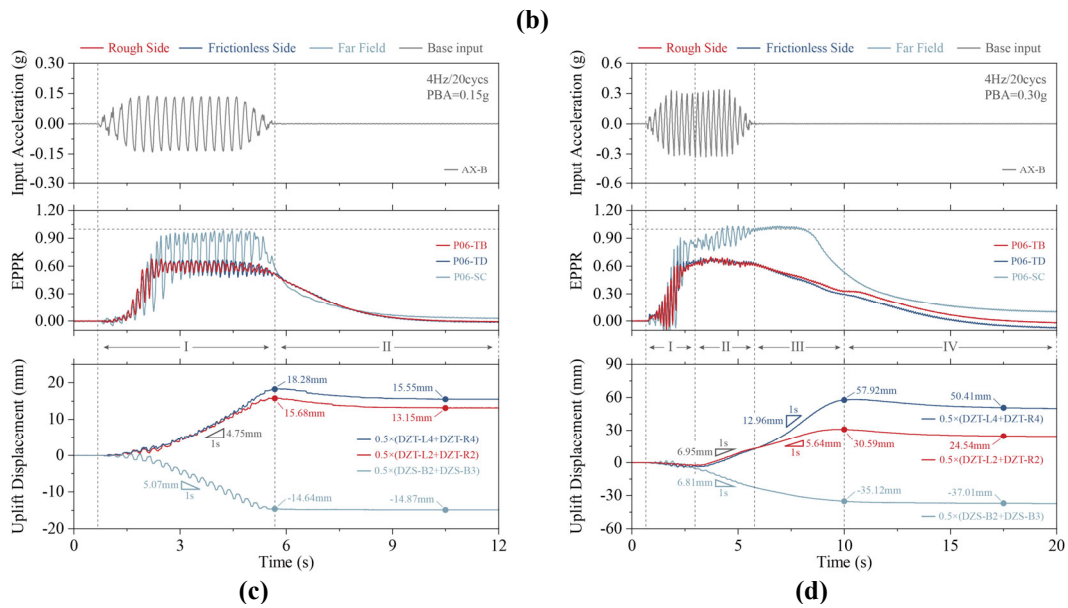
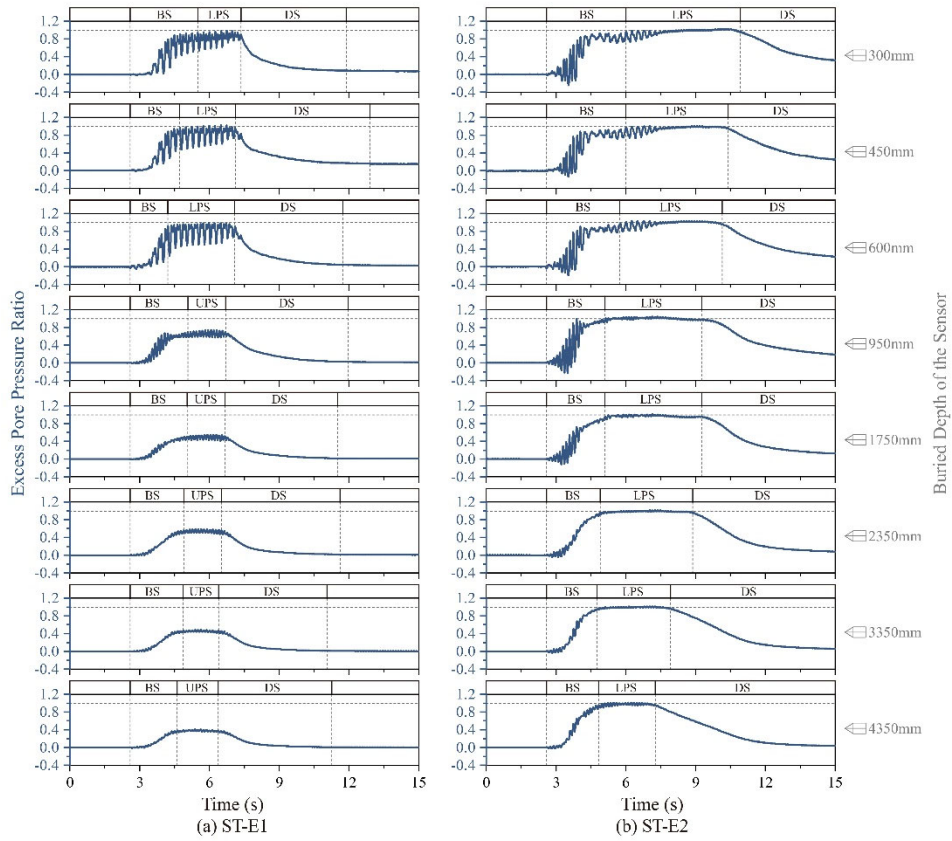
337 During soil liquefaction, the interaction between soil and structure (SSI) is influenced not only by the macroscopic  
 338 parameters of the structure, but also by the microscopic characteristics of the soil-structure interface. To examine how  
 339 the structural surface roughness affects the SSI during ground liquefaction, a site tunnel 1-g shaking table test was  
 340 conducted. As depicted in Fig. 16(a), the model tunnel was segmented into two sections: the left side was covered with  
 341 sandpaper to create a nonslip interface, while the right side was coated with Teflon tape to simulate a nearly frictionless  
 342 interface. The tunnel had an overall density of 900 kg/m<sup>3</sup> and was embedded 300-mm deep in a soil model with a  
 343 relative density of 50%. The site-tunnel model was subjected to two seismic motions, each with a frequency of 4 Hz but  
 344 differing in amplitude, as listed in Table 7.

345 **Table 7** Loading cases of shaking table tests: liquefaction of the site-tunnel model.

Case	Frequency	Peak Base Acceleration	Number of cycles
ST-E1	4	0.15g	20
ST-E2	4	0.30g	20

346 The pore pressure responses for the two shaking events are compared in Fig. 16 (b). This shows that in ST-E1, only a  
 347 part of the field underwent liquefaction owing to the limited loading amplitude. In contrast, the liquefaction affected the  
 348 entire ST-E2 field. Figures 16(c) and 16(d) compare the vertical displacements of the tunnel and ground surface,  
 349 revealing that the uplift behavior of the tunnel varies with the surface roughness. In ST-E1 (Fig. 16 (c)); despite partial  
 350 liquefaction, the tunnel experienced significant uplift. This uplift occurred in two stages: Stage 1, where the uplift was  
 351 rapid and steady during the seismic input; and Stage 2, where the uplift slowed as the excess pore pressure (EPP)  
 352 dissipated and the soil consolidated. The smooth segment of the tunnel exhibited slightly more uplift than the rough  
 353 segment. In ST-E2 (Fig. 16(d)), the increased loading amplitude led to significant variations in the uplift behavior. Four  
 354 distinct stages of vertical displacement were identified. In Stage 1, the tunnel initially settled as excess pore pressures  
 355 accumulated. During Stage 2, both tunnel segments experienced uplift at similar rates owing to full liquefaction. The  
 356 most pronounced difference in uplift rate between the segments occurred in Stage 3, where the smooth segment uplifted  
 357 2.3 times faster than the rough segment as EPPs decreased. This disparity is attributed to the increased frictional  
 358 resistance resulting from the recovery of the effective normal stress owing to pore pressure dissipation during this stage.  
 359 Finally, in Stage 4, the tunnel settles as the resistance exceeds the upward forces.  
 360 In summary, the tunnel uplift behavior varied with the structural surface roughness and amplitude of the input  
 361 motions. Surface roughness has a pronounced effect on tunnel uplift, particularly during reconsolidation after  
 362 liquefaction.





363 **Figure 16** Distinct tunnel uplifting behavior during liquefaction under multiple shakings: (a) Model tunnel; (b) Pore pressure  
 364 responses in shaking events ST-E1 and ST-E2; (c) Uplifting behavior in ST-E1; and (d) Uplifting behavior in ST-E2.

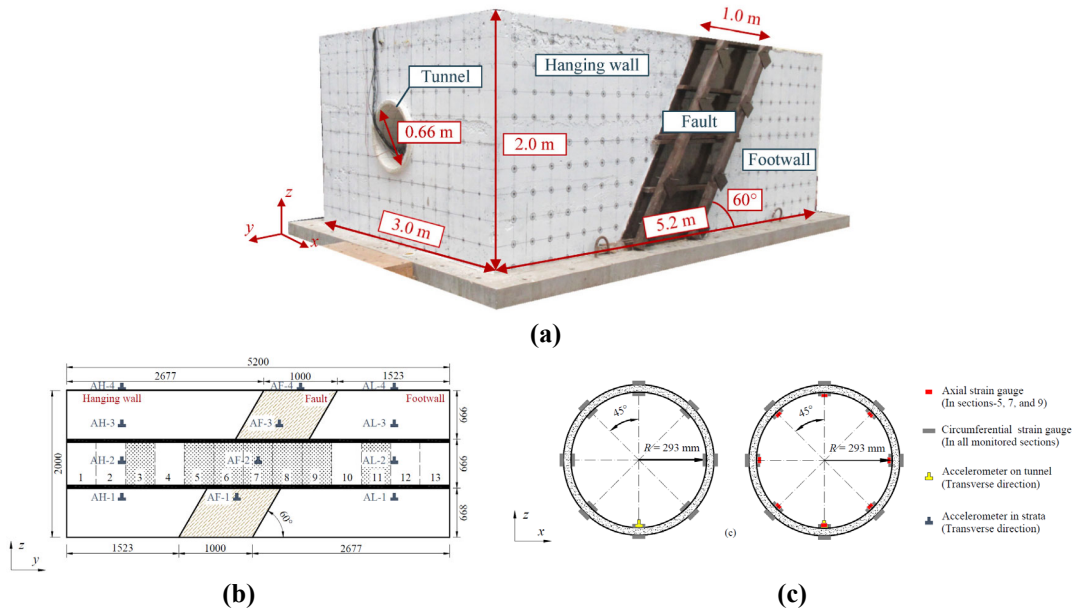
365 **4. Tunnel crossing Fault**

366 Seismological studies have indicated that the zones in which tunnels cross faults are particularly vulnerable to seismic  
 367 damage. Over the past 30 years, a considerable number of fault-crossing tunnels have experienced damage during  
 368 earthquakes, including the 1999 Chi-Chi earthquake<sup>31</sup>, 2004 Niigata earthquake<sup>32</sup>, 2008 Wenchuan earthquake<sup>33</sup>, 2016  
 369 Kumamoto earthquake<sup>34</sup>, 2022 Menyuan earthquake<sup>35</sup>, and 2023 Turkey earthquake<sup>36</sup>. During these seismic events,  
 370 most fault-crossing tunnels suffered severe damage, such as lining collapse, primarily owing to the impact of fault  
 371 movement.

372 Extensive research has been conducted on the failure mechanisms of tunnels crossing active faults and subjected to  
 373 fault ruptures<sup>37–39</sup>. However, even if faults do not rupture during earthquakes, tunnels may sustain damage. Several

374 studies have addressed this issue<sup>40-42</sup>. Evidence indicates that essential differences exist between these two conditions.  
 375 Tunnels crossing ruptured faults are primarily damaged by violent fault dislocations, whereas tunnels crossing faults  
 376 without ruptures may experience differential movements induced by the fault site effect.

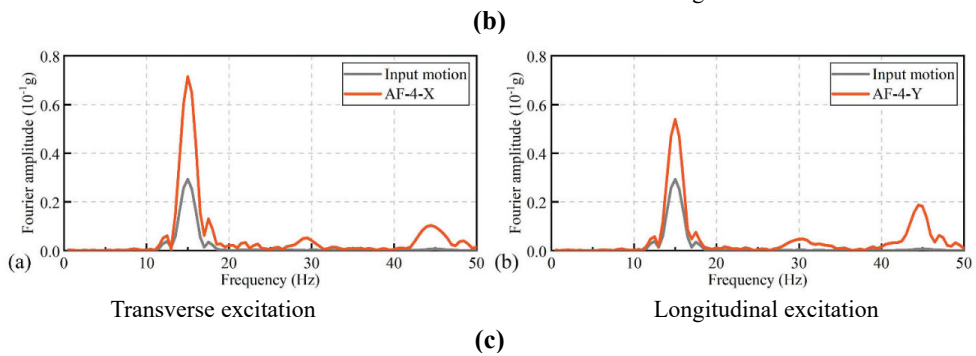
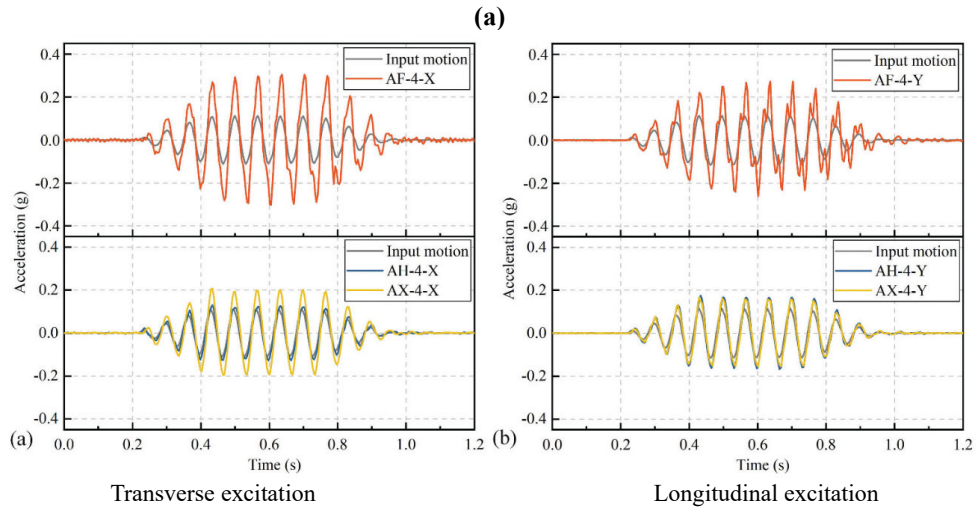
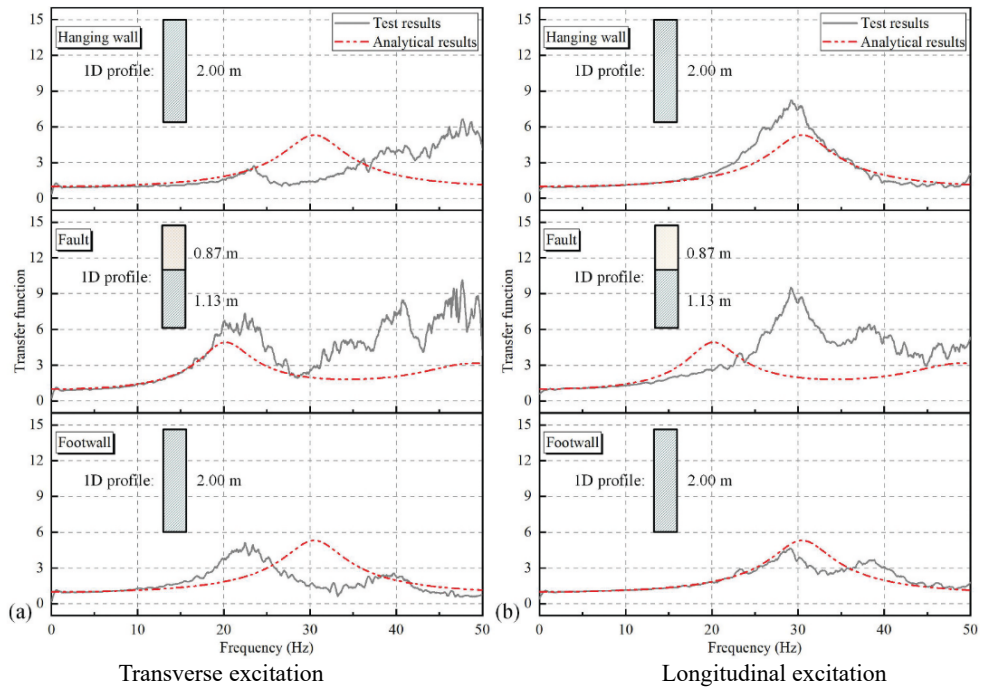
377 To this end, a large-scale physical model was developed to consider a scenario in which a model tunnel crosses an  
 378 unruptured fault under seismic vibrations, as shown in Fig. 17, along with the layout of the instrumentation. The local  
 379 site effect of the fault site<sup>43</sup>, as well as the deformation pattern and failure mechanism of the fault-crossing tunnel<sup>44,45</sup>,  
 380 were investigated using this shaking table test.

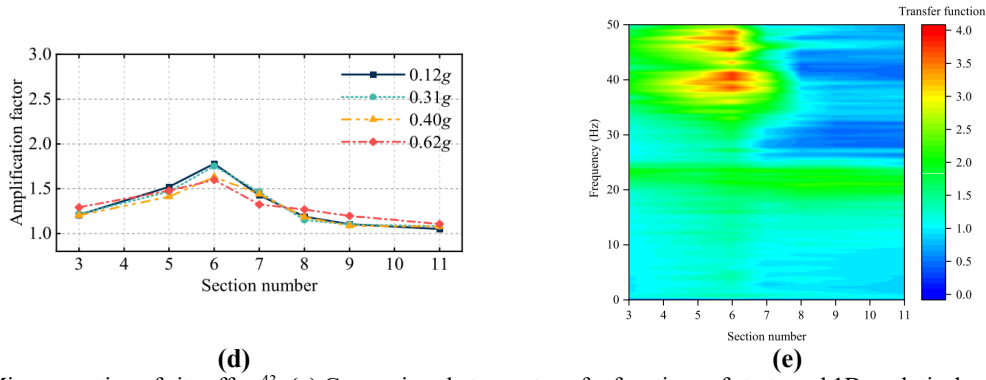


381 **Figure 17** Testing model<sup>44,45</sup>: (a) Physical model; (b) Instrumentations (longitudinal profile); and (c) Instrumentations (cross-  
 382 sectional profile of tunnel).

#### 383 4.1 Fault site effect and acceleration response of tunnel

384 Figure 18 (a) plots the TFs of the fault site in the tests against the analytical solution of the one-dimensional site. The  
 385 hanging wall and the footwall, although homogeneous in the vertical direction, have significant discrepancies from the  
 386 one-dimensional site responses. The fault exhibits some similarities with the one-dimensional site response under  
 387 transverse excitation, but with a more pronounced amplification effect. Under longitudinal excitation, the fault exhibits  
 388 completely different response from the one-dimensional site response. The accelerograms of the ground surface of the  
 389 fault site in sinusoidal wave cases are shown in Fig. 18(b). A significant alteration of the accelerogram waveform  
 390 relative to the input seismic motion could be found, attributed to frequency dispersion and waveform conversion, as  
 391 shown in Fig. 18(c). The generation of components at 30 Hz and 45 Hz, which were not observed in the original signal,  
 392 indicates the presence of harmonic distortion. This provides strong evidence of the non-linearity of the strata within the  
 393 fault.



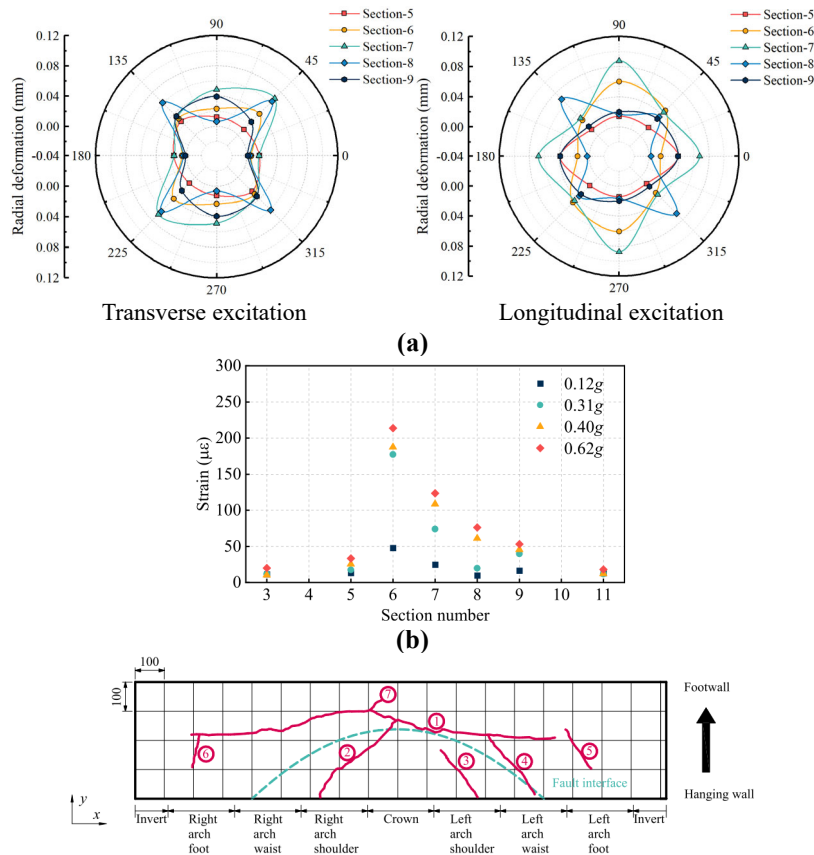


394 **Figure 18** Micro-zonation of site effect<sup>43</sup>: (a) Comparison between transfer functions of strata and 1D analytical results: transverse  
 395 and longitudinal excitation; (b) Accelerograms of strata in sinusoidal wave cases: transverse and longitudinal excitation; (c) Fourier  
 396 spectra of strata within fault in sinusoidal wave cases: transverse and longitudinal excitation; (d) Acceleration amplification factors  
 397 of the tunnel; and (e) Transfer functions of the tunnel.

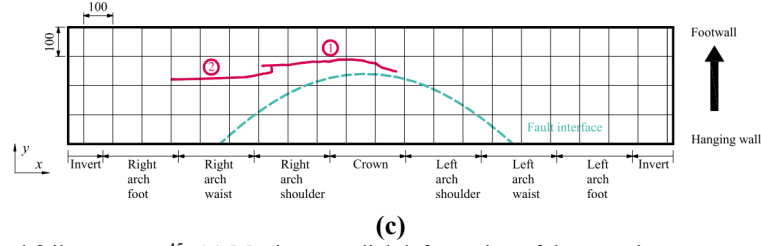
398 Figure 18(d) shows the acceleration amplification factors of the tunnel. In all the test cases, the curves peaked near  
 399 the fault. The strongest accelerations of the tunnel were always registered in section-6, which intersects the interface of  
 400 the fault and hanging wall. Figure 18(e) shows the contours of the transfer functions of the tunnel sections in the white  
 401 noise case. Generally, sections of the tunnel in the hanging wall exhibited higher amplifications than those in the  
 402 footwall, and the responses in section-6 were the most amplified.

#### 403 4.2 Deformation pattern and failure mechanism

404 The maximum radial deformation of the tunnel is shown in Fig. 19(a). The tunnel exhibits shearing deformation under  
 405 transverse excitation and vertical crush deformation under longitudinal excitation. Figure 19(b) shows the maximum  
 406 strain in the tunnel. The largest strains were found in section-6, followed by sections-5 and 7, and the strains of the  
 407 tunnel sections in the hanging wall exceeded those in the footwall.







408 **Figure 19** Deformation and failure pattern<sup>45</sup>: (a) Maximum radial deformation of the tunnel: transverse and longitudinal excitation;  
 409 (b) Maximum strain of the tunnel; and (c) Lining cracks of the tunnel.

410 The structural integrity of the tunnel was assessed meticulously at the end of each test. It can be expected that  
 411 section-6, which had the strongest accelerations and the largest strains, also had the most cracks. As shown in Fig. 19(c),  
 412 the lining exhibited seven cracks. The primary crack aligned with the fault interface and extended to approximately  
 413 1300 mm in length. On both the interior and exterior, cracks mostly initiated from the crown and developed towards the  
 414 invert while maintaining an orientation roughly parallel to the fault interface.

### 415 4.3 Analytical model

416 A pseudo-static analytical model was established based on the shaking table test data to further explore the deformation  
 417 pattern and failure mechanism of the tunnel. The fault-rock-tunnel system was simplified as a Timoshenko beam on  
 418 Winkler foundations, as shown in Fig. 20(a). At a certain moment  $t$ , the governing equation for a Timoshenko beam on  
 419 a Winkler foundation is

$$420 \quad \frac{\partial^4 u_t}{\partial x^4} - \frac{K_h}{K_t} \frac{\partial^2 u_t}{\partial x^2} + \frac{K_h}{E_t I_t} u_t = -\frac{K_h}{K_t} \frac{\partial^2 u_g}{\partial x^2} + \frac{K_h}{E_t I_t} u_g, \quad (7)$$

421 where  $E_t$  is the elastic modulus of the tunnel;  $I_t$  is the moment of inertia of the tunnel cross-section;  $u_t$  is the horizontal  
 422 transverse displacement of the tunnel;  $u_g$  is the horizontal displacement of the ground at the depth of the tunnel;  $K_h$  is  
 423 the spring stiffness of the Winkler foundations, and  $K_t$  is the transverse shear stiffness of the Timoshenko beam  
 424 calculated as follows:

$$425 \quad \begin{cases} K_h = \frac{16\pi G_g(1-\nu_g)D}{4H(3-4\nu_g)} \\ K_t = G_t A_t \frac{2(1+\nu_t)}{4+3\nu_t} \end{cases} \quad (8)$$

426 The boundary and continuity conditions of the tunnel are:

$$427 \quad \begin{cases} \lim_{x \rightarrow -\infty} u_t = u_{g1} \\ \lim_{x \rightarrow +\infty} u_t = u_{g2} \\ \lim_{x \rightarrow 0^-} u_t = \lim_{x \rightarrow 0^+} u_t, \lim_{x \rightarrow L^-} u_t = \lim_{x \rightarrow L^+} u_t \\ \lim_{x \rightarrow 0^-} \theta = \lim_{x \rightarrow 0^+} \theta, \lim_{x \rightarrow L^-} \theta = \lim_{x \rightarrow L^+} \theta \\ \lim_{x \rightarrow 0^-} M = \lim_{x \rightarrow 0^+} M, \lim_{x \rightarrow L^-} M = \lim_{x \rightarrow L^+} M \\ \lim_{x \rightarrow 0^-} Q = \lim_{x \rightarrow 0^+} Q, \lim_{x \rightarrow L^-} Q = \lim_{x \rightarrow L^+} Q \end{cases} \quad (9)$$

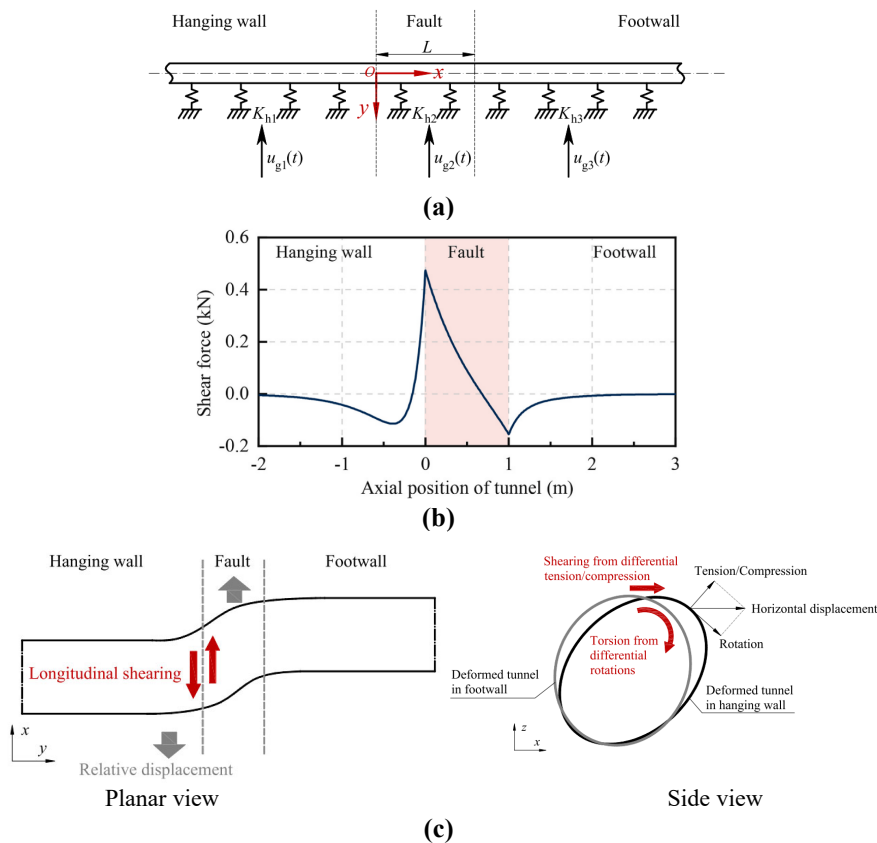
428 The deflection angle  $\theta$ , the bending moment  $M$ , and the shear force  $Q$  can be easily derived from the following  
 429 equations:

$$430 \quad \begin{cases} M = -E_t I_t \left( \frac{\partial^2 u_t}{\partial x^2} - \frac{\partial \beta}{\partial x} \right) \\ Q = K_t \beta \\ \theta = \frac{\partial u_t}{\partial x} - \beta \end{cases} \quad (10)$$

431 The displacement of the fault-crossing tunnel can be obtained by incorporating a general solution with boundary and  
 432 continuity conditions. The shear forces in the tunnel derived from the analytical solution are shown in Fig. 20(b).  
 433 Neither was symmetrical about the fault. In particular, the shear force increased sharply at the interface between the  
 434 fault and the hanging wall. This explains the localized damage to the tunnel in the area. The longitudinal non-uniform  
 435 deformations of the fault site are the primary cause of the shearing of the tunnel, as illustrated in Fig. 20(c). The  
 436 difference between the tunnel cross-sections is fundamentally the relative horizontal displacement at two different  
 437 heights of the cross-section. The differential tensions/compressions and rotations inevitably result in shear-torsional

438 deformation of the tunnel, as illustrated in Fig. 20(c). This deformation pattern was the most prominent at the crown of  
 439 the tunnel and corresponded to the concentration of cracks at the crown.

440 Although a series of studies have been conducted on the seismic response of tunnels crossing non-ruptured faults,  
 441 several critical issues remain unresolved. First, the failure mechanisms of tunnels under the coupled effects of intense  
 442 seismic vibrations and fault ruptures, as well as the corresponding mitigation strategies, require further investigation.  
 443 When an active fault ruptures, the dynamic interaction between the fault dislocation and the stress waves generated by  
 444 the rupture creates a coupling effect. Simply considering either fault dislocation or seismic vibration is insufficient for  
 445 accurately revealing the failure mechanisms of tunnels. Second, the impact of cascading fault ruptures on the seismic  
 446 response of tunnels presents a significant challenge. Compared with a single fault, the seismic mechanism of cascading  
 447 fault ruptures is more complex. The failure mechanisms of tunnels under such scenarios represent a current scientific  
 448 frontier issue. Finally, the development of analytical methods to determine the seismic response of tunnel-crossing  
 449 faults remains challenging. The complexity of the wave field at the fault site during earthquakes, combined with the  
 450 highly nonlinear mechanical behavior of fractured rock masses within the fault, makes it difficult to determine the free-  
 451 field response of the fault site. This poses severe challenges for the analytical methods for tunnel-crossing faults.



452 **Figure 20** Analytical model of fault-crossing tunnel<sup>45</sup>: (a) Analytical model; (b) Shear forces of the tunnel; and (c) Longitudinal and  
 453 transverse deformation patterns of fault-crossing tunnel.

## 454 5. Closing Remarks

455 A series of large-scale shaking table tests were conducted on scenarios of long tunnels, such as under travelling waves,  
 456 conjunction structures between the shaft and tunnel, variation of rock-soil ground, uplift in liquefiable ground, and  
 457 crossing faults. The results were examined in contrast to numerical or analytical solutions and the following conclusions  
 458 were drawn.

### 459 5.1 Travelling wave

460 The propagation of travelling waves exhibit spatial variation in any domain of the ground, which is indicated by the  
 461 spectrum representing the impact of wave superposition, whether on uniform ground or sloped ground. Comparing the  
 462 uniform excitation and the same intensity of non-uniform excitation, no significant difference in the magnitude of  
 463 acceleration was observed at a measuring spot. The differential displacement of the tunnel under non-uniform excitation  
 464 is propagated from one end to the other in times of that of the uniform excitation. The joint dislocations thus propagated.  
 465 Non-uniform excitation from earthquakes should be considered in the aseismic design of long tunnels.

## 466 **5.2 Structural variation**

467 Discrepant responses due to structural variations were directly revealed by the test, and the data were interpreted using  
468 the classic pseudo-static model. Based on this, a dynamic analytical model for the shaft-tunnel junction was developed  
469 by combining the beam-spring model and the dynamic model for rigid caissons. The dynamic model was validated  
470 using 3-dimensional numerical computations. Its applicability was further extended to incorporate the travelling-wave  
471 effect, where the spatial displacement field was calculated using the stiffness matrix method for layered media. The  
472 newly proposed method yielded satisfactory results for the displacements of the shaft and internal forces of the tunnel.  
473 It also quantitatively clarifies the soil-structure interaction mechanism of the tunnel-shaft junction.

## 474 **5.3 Variation of ground**

475 The site characteristics of strata with longitudinally varying geological conditions exhibited spatial variations that were  
476 identified using the standard spectral ratio (SSR) method. These spatial variations were specified by comparison with  
477 1D theoretical analysis results. The amplification effect observed in soft ground can be explained by the interference  
478 effect resulting from the scattered waves generated at the strata interface. The tunnel portions follow the nonuniform  
479 movements of the varying strata, thereby reflecting the resulting discrepant responses, as revealed by the acceleration  
480 data. The tunnel deformation was negligible in the rock stratum, whereas it was significantly greater in the soil deposit.  
481 Notably, the sharp increase in the sectional deformation when transitioning from the rock stratum to the soil deposit is  
482 likely to induce significant transverse dislocations between adjacent lining rings. Circumferential joint extensions were  
483 concentrated near the strata interface and their magnitudes were determined by the relative displacement between the  
484 two strata. Based on the test data, the influence of the stratum interface was primarily limited to the region within three  
485 times the tunnel diameter.

## 486 **5.4 Liquefiable ground**

487 Liquefaction is associated with the accumulation of pore water pressure owing to the volumetric contraction of soils  
488 under undrained cyclic loading conditions. For cohesionless soils, the development of excess pore water pressure  
489 induces a loss of grain contact, which ultimately leads to the disappearance of shear stiffness. The results from the 1-g  
490 shaking table tests show that the dynamic behavior of the soil is significantly influenced by the frequencies of the input  
491 seismic motions. This variation can be attributed to the combined effects of the localized strain amplitude and relative  
492 drainage conditions. Owing to the viscous movement of liquefied soils and the dynamic migration of pore fluids,  
493 underground structures often exhibit uplift behavior during liquefaction. The experimental findings also revealed that  
494 the surface roughness of the structure played a critical role in the tunnel uplift, with smoother surfaces experiencing  
495 significantly greater uplift during liquefaction.

## 496 **5.5 Crossing fault**

497 The fault exhibits a higher acceleration response than the strata on both its sides. A significant alteration in the  
498 accelerogram waveform relative to the input seismic motion was observed on the surface of the fault, which could be  
499 attributed to frequency dispersion and waveform conversion. The maximum acceleration of the tunnel was located at  
500 the interface between the fault and hanging wall, whereas the maximum strain of the tunnel also appeared in this area.  
501 After seismic excitation, several cracks parallel to the fault interface were observed on both the interior and exterior of  
502 the tunnel and were mainly distributed near the interface between the fault and hanging wall. An analytical model was  
503 established to further investigate the deformation patterns and failure mechanisms of the tunnel. The sharply increased  
504 shear force at the interface between the fault and hanging wall, which was derived from the analytical solution, explains  
505 the localized damage to the tunnel in the area. The differential tensions/compressions and rotations inevitably result in  
506 shear-torsional deformation of the tunnel, which is the primary culprit behind the shearing of the tunnel.

507 Although these investigations clarified the most critical situations of long tunnels under seismic action, there are still  
508 some cases to be explored. One of the unveiled scenarios is a tunnel crossing a potential rupture fault. Other aspects  
509 include measures for improving the resilience of tunnels in mitigating seismic hazards. This is one method of achieving  
510 sustainable development.

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