

# A framework for Interpreting Variable Penetration Rate CPTu Tests in Mine Tailings

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## ABSTRACT

Cone penetration testing with pore pressure measurements (CPTu) is widely used in tailings engineering, with most interpretation methods formulated for fully drained or undrained responses. However, mine tailings often exhibit partially drained behavior, posing significant interpretation challenges as limited efforts have investigated this response. This study advances the understanding of partially drained responses in mine tailings by conducting variable penetration rate CPTu tests (0.2 cm/s to 15 cm/s) in a tailings storage facility (TSF). Complementary field and laboratory tests — including shear wave velocity measurements, vane shear testing, and triaxial testing — further support the assessments. A salient aspect of the evaluated TSF is its use of both conventional and thickened tailings, enabling comparisons across different depositional methods. The study highlights key interpretation challenges, particularly the uncertainties in defining drained and undrained responses. Notably, conventional tailings exhibit greater variability due to their higher susceptibility to segregation and layering, leading to a broader range of partially drained responses than thickened tailings. A framework that integrates numerical simulations of the CPTu penetration process and laboratory testing is presented to address the highlighted challenges and to constrain parameters of interest, such as the tailings' state and the operative coefficient of consolidation. The framework's application is showcased using the collected information.

## INTRODUCTION

Cone penetration testing with pore pressure measurements (CPTu) is widely used in tailings engineering. Conventionally, the CPTu test consists of pushing a 10 cm<sup>2</sup> or 15 cm<sup>2</sup> probe at a standard rate of 2 cm/s. At this rate, penetration is expected to produce fully drained responses (i.e., immediate dissipation of excess pore pressures) in sandy materials with high hydraulic conductivity and fully undrained responses (i.e., no dissipation of excess pore pressures) in clayey materials with low hydraulic conductivity. However, the response of intermediate materials, such as mine tailings, is more complex. Whether they behave in a drained, undrained, or partially drained manner during CPTu penetration depends on multiple factors, including cone geometry, penetration rate, and mechanical properties (Oliveira et al. 2011; DeJong et al. 2012; Dienstmann et al. 2018; Ayala et al. 2023). The distinctive mechanical properties of mine tailings further complicate their penetration response (e.g., Macedo and Vergaray 2022).

This study presents insights from variable rate CPTu testing conducted at an active TSF where two distinct types of mine tailings — conventional and high-density thickened tailings (hereinafter referred to as thickened tailings) — are deposited, providing a unique opportunity to examine penetration rate effects across different depositional methods. These materials exhibit contrasting solid contents, typically 25–40% for conventional tailings and 40–65% for thickened tailings, which influence their penetration response. Conventional tailings tend to form large ponds, undergo greater segregation (Watson et al. 2010), and deposit under different energy conditions compared to thickened tailings (Reid and Jefferies 2018; Macedo et al. 2024). The study specifically addresses the challenges of interpreting drained and undrained conditions in the investigated TSF and introduces a framework that integrates experimental testing and numerical simulations to analyze variable-rate CPTu data. Field-scale studies on variable rate CPTu testing in mine tailings remain scarce (as discussed in the next section), highlighting this study’s contribution to improving the understanding of tailings response under varying penetration rates and drainage conditions.

## PREVIOUS STUDIES

Several studies have investigated variable-rate CPTu tests and partially drained responses, primarily focusing on natural soils. These efforts include research on sandy materials (Krage et al. 2014b; Suzuki and Lehane 2015; Martinez et al. 2016b; Chow et al. 2018; Tian and Lehane 2022), clayey materials (Lehane et al. 2009; Sheng et al. 2014; Ceccato et al. 2016; Ceccato and Simonini 2017; Orazalin and Whittle 2018), clay-sand mixtures (Kim et al. 2008; Jaeger et al. 2010; Salgado and Prezzi 2014; Doan and Lehane 2018), and silts (Martinez et al. 2016a; Martinez et al. 2016b; Price et al. 2019; Zhang et al. 2022). Most of these studies have been conducted in controlled environments, such as centrifuge tests (Lehane et al. 2009; Jaeger et al. 2010; Chow et al. 2018; Orazalin and Whittle 2018; Price et al. 2019; Zhang et al. 2022) and calibration chamber tests (Kim et al. 2008; Salgado and Prezzi 2014; Doan and Lehane 2018; Tian and Lehane 2022), with fewer investigations conducted at the field scale (Kim et al. 2008; Martinez et al. 2016a; Orazalin and Whittle 2018). Some studies have also incorporated numerical simulations, primarily using analytical models such as cavity expansion (Sheng et al. 2014; Suzuki and Lehane 2015; Orazalin and Whittle 2018; Zhang et al. 2022). More recent efforts have employed advanced numerical frameworks capable of simulating large deformations in the penetration process, such as the material point method (MPM) (Ceccato et al. 2016; Ceccato and Simonini 2017; Yost et al. 2022) and the particle finite element method (PFEM) (Monforte et al. 2021; Oliynyk et al. 2022).

Previous efforts have introduced the backbone rate effect curve concept to interpret variable-rate penetration data. These curves relate normalized CPTu responses to a normalized penetration rate, typically defined as  $V_h = vd/c_h$ , where  $v$  is the penetration rate,  $d$  is cone diameter, and  $c_h$  is the horizontal coefficient of consolidation. Figure 1 illustrates this concept using normalized CPTu tip resistance  $Q = (q_t - \sigma_v)/\sigma'_v$ , where  $q_t$  is the CPTu corrected tip resistance, and  $\sigma_v$  and  $\sigma'_v$  are the total and effective vertical stresses. In loose contractive materials,  $Q$  reaches a maximum value,  $Q_D$ , under drained conditions at low

79  $V_h$ , and a minimum value,  $Q_U$ , under undrained conditions at high  $V_h$ . The opposite trend  
80 occurs in dilative materials (e.g., [Ayala et al. 2023](#)). In natural soils, drained conditions  
81 typically correspond to  $V_h$  values below 0.1-0.3, while undrained conditions occur at  $V_h$  ex-  
82 ceeding 30-100 ([Randolph and Hope 2004](#); [Schnaid 2005](#); [DeJong and Randolph 2012](#)); The  
83 ratio  $Q_D/Q_U$  generally ranges from 2 to 6 for clayey soils with greater variability in silty  
84 materials ([DeJong et al. 2012](#)).

85 Compared to natural soils, previous efforts investigating CPTu rate effects in mine tailings  
86 remain limited. [Oliveira et al. \(2011\)](#) proposed a physics-based analytical model to estimate  
87 backbone rate effect curves and applied it to silty tailings data obtained from variable-rate  
88 penetration tests using a 0.9 mm miniature cone in centrifuge experiments. Their results  
89 indicate that the ratio of drained tip resistance,  $q_{t,D}$ , to undrained tip resistance,  $q_{t,U}$  varies  
90 from 3 to 4, with the transition from undrained to partially drained conditions occurring at  
91  $V_h = 50$ . Although not explicitly stated, interpreting their data suggests that the transition  
92 to a fully drained response occurs at  $V_h = 0.5$ . [Dienstmann et al. \(2018\)](#) analyzed variable-  
93 rate CPTu data from the Fazenda Brasileiro TSF in Brazil. Their findings suggest partially  
94 drained conditions in the range of  $V_h = 0.01$  to 10. Using a poroelastic analytical solution  
95 and CamClay simulations, they highlighted that the  $Q_D/Q_U$  ratio (approximately 11 for  
96 their materials) is primarily influenced by stiffness and strength. However, their tip resis-  
97 tance simulations differ significantly from the field data, likely due to complexities in the field  
98 and modeling limitations. [Schnaid et al. \(2020\)](#) introduced an alternative normalization for  
99 penetration velocity, defined as  $\bar{V}_h = vt_{50}/(d\sqrt[4]{I_r})$  where  $t_{50}$  represents the time to reach 50%  
100 consolidation in dissipation tests and  $I_r = G/Su$  is the rigidity index defined based on the  
101 operative shear modulus ( $G$ ) and the undrained shear strength ( $Su$ ). They applied this ap-  
102 proach to data from [Sosnoski \(2016\)](#), collected at the same TSF investigated by [Dienstmann](#)  
103 [et al. \(2018\)](#). The motivation for this normalization was to mitigate uncertainties introduced  
104 by  $c_h$ . Despite analyzing the same TSF, [Schnaid et al. \(2020\)](#) reported a  $Q_D/Q_U$  ratio of  
105 approximately 20, contrasting with the value of 11 reported by [Dienstmann et al. \(2018\)](#).

1106 This suggests substantial  $Q_D/Q_U$  variability even within the same TSF or that the signifi-  
1107 cant scatter in the two datasets influenced the reported ratios. Notably, the  $Q_D/Q_U$  values  
1108 they reported are significantly higher than those typically observed in natural soils, which  
1109 rarely exceed six (DeJong and Randolph 2012). More recently, Dienstmann et al. (2024)  
1110 combined Monte Carlo simulations and cavity expansion analyses to assess the variability in  
1111 backbone rate effect curves using data from the same TSF examined by Dienstmann et al.  
1112 (2018) and Schnaid et al. (2020). Additionally, Ayala et al. (2023) proposed a method for  
1113 estimating the state parameter  $\psi$  (Been and Jefferies 1985) in partially drained conditions  
1114 by integrating cavity expansion simulations using the NorSand model (Jefferies 1993) with  
1115 backbone rate effect curves.

## 1116 SITE INVESTIGATIONS

1117 The investigated site is the TSF of a gold mine that has been producing and depositing  
1118 tailings since the 1990s. Throughout its operation, the TSF has stored two types of tailings:  
1119 conventional tailings from 1990 to 2010 and thickened tailings thereafter. The conventional  
1120 tailings were deposited with a solid content of approximately 50%, while the thickened tail-  
1121 ings had a higher solid content of around 72%. Figure 2 presents the particle size distribution  
1122 for collected samples of both tailings types. The thickened tailings exhibit a narrower range  
1123 due to their reduced segregation tendencies. Both conventional and thickened tailings clas-  
1124 sify as low-plasticity silts, with fine contents (FC) generally exceeding 70% and plasticity  
1125 indices (PI) ranging from 0% to 2%. Table 1 summarizes representative index properties for  
1126 the examined tailings.

1127 The field investigations included CPTu tests with shear wave ( $V_s$ ) and compression wave  
1128 ( $V_p$ ) velocity measurements as well as dissipation tests. The CPTu tests were conducted at  
1129 the standard penetration rate of 2 cm/s and at non-standard rates of 0.2, 10, and 15 cm/s,  
1130 following the layout shown in Figure 3. Vane shear testing supplemented the CPTu tests, and  
1131 borehole samples were recovered for triaxial testing, which will be discussed later. Variable  
1132 rate CPTu tests (designated as CPTu02, CPTu10, and CPTu15) were conducted within

133 1.5 m of the central standard CPTu (CPTu2). The numerical values in the CPTu labels  
 134 correspond to the penetration rates, e.g., CPTu02 refers to a penetration of 0.2 cm/s. The  
 135 spacing between CPTu tests was kept below half of the average horizontal correlation length  
 136 of the deposited tailings (both conventional and thickened), which [Macedo et al. \(2024\)](#)  
 137 estimated at approximately 3.2 m based on 15 additional standard CPTu tests conducted  
 138 for spatial variability assessment.

### 139 **General characterization and response at the standard CPTu penetration rate**

140 Figure 4 presents the CPTu responses from the standard penetration push (CPTu2),  
 141 which extended to a depth of 20 m. The corrected tip resistance,  $q_t$ , sleeve friction,  $f_s$ ,  
 142 and excess pore pressure,  $u_2$ , distinguish the boundary between conventional and thickened  
 143 tailings at approximately 8.8 m, with thickened tailings overlaying the conventional deposit.  
 144 The first 2 m corresponds to an access pad, so this data is not shown. Figure 4 also includes  
 145 the variation of  $V_s$ ,  $V_p$ , and the soil behavior type index ( $I_c$ ) proposed by [Robertson \(2016\)](#).  
 146  $I_c$  is estimated as  $I_c = \sqrt{(3.47 - \log Q_{tn})^2 + (\log F_r + 1.22)^2}$ , where  $Q_{tn} = \frac{(q_t - \sigma_v)}{P_a} \left(\frac{P_a}{\sigma'_v}\right)^n$  is  
 147 the normalized tip resistance,  $F_r = \frac{f_s}{(q_t - \sigma_v)} \times 100\%$  is the normalized friction ratio,  $P_a$  is the  
 148 atmospheric pressure, and  $n = 0.381I_c + 0.05 \left(\frac{\sigma'_v}{P_a}\right) - 0.15$ . The figure also presents normalized  
 149 CPTu responses, the modified Soil Behavior Type index,  $I_B$ , proposed by [Robertson \(2016\)](#),  
 150 defined as  $I_B = 100(Q_{tn} + 10)/(70 + Q_{tn}F_r)$ , and the CPTu chart proposed by [Robertson](#)  
 151 [\(2016\)](#) with the collected data. The endpoints of the dissipation tests, marked as circles in the  
 152 pore pressure plot of Figure 4, indicate a groundwater level at 6 m. A similar interpretation  
 153 applies to dissipation tests from other CPTu locations not shown in the figure.

154  $V_p$  transitions to values indicative of full saturation ( $V_p > 1500$  m/s) at approximately 7.5  
 155 m. Since  $V_p$  is highly sensitive to small variations in saturation, this suggests that materials  
 156 between 6.0 and 7.5 m are likely to be nearly but not fully saturated.  $V_s$  values, around 200  
 157 m/s, indicate relatively soft materials, which is expected for mine tailings. The thickened  
 158 tailings exhibit  $q_t$  values below 5 Mpa and  $f_s$  values under 50 kPa, with relatively uniform  
 159 characteristics (as observed in the  $F_r$  variation), particularly below 5 m. This uniformity

160 is consistent with their non-segregating nature.  $I_c$  values range from 1.8 to 2.6, suggesting  
161 the materials behave as sandy silt and silty sand mixtures, with the [Robertson \(2016\)](#) chart  
162 classifying them primarily as contractive sand-like and transitional. The conventional tailings  
163 exhibit higher  $q_t$  (generally between 5 and 10 MPa) and higher  $f_s$  (typically 50 to 100  
164 kPa) compared to the thickened tailings. Their more segregating nature results in greater  
165 fluctuations in  $q_t$  and  $f_s$ , which is also reflected in more  $F_r$  variations.  $I_c$  remains below  
166 2.5 in most of the profile, except for some layers where it reaches values up to 3.1. The  
167 conventional tailings predominantly behave as sands to silty sands; the [Robertson \(2016\)](#)  
168 chart classifies them as contractive sand-like and transitional, with some dilative lenses.

### 169 **Responses in variable rate CPTus**

170 Figure 5 compares the  $q_t$ ,  $f_s$ , and  $u_2$  data collected from the variable rate CPTus (CPTu02,  
171 CPTu10, CPTu15) with the standard CPTu (CPTu2). Within the thickened tailings,  $q_t$   
172 in CPTu02 is approximately 4 MPa, exceeding the values recorded in the CPTus pushed  
173 at higher penetration rates.  $q_t$  in CPTu10 and CPTu15 remains similar, around 2.5 MPa,  
174 indicating that undrained conditions likely occur at penetration rates exceeding 10 cm/s. The  
175 slowest CPTu (CPTu02) records the lowest  $u_2$  among the four CPTus but does not align with  
176 the hydrostatic pore pressure profile, suggesting that thickened tailings have not yet reached  
177 fully drained conditions at 0.2 cm/s. The  $u_2$  in CPTu10 and CPTu15 are generally lower  
178 than those in CPTu2, suggesting that viscosity effects may have influenced pore pressures  
179 at high penetration rates; consistent with observations by ([Wroth 1984](#); [Lehane et al. 2009](#);  
180 [Chow et al. 2018](#)).

181 In the conventional tailings (below 8.8 m), the responses are more complex due to their  
182 greater segregation and variability. However, a general trend of decreasing  $q_t$  with increasing  
183 penetration rate is still observed. At some depths, such as around 9.5 m  $q_t$  in the standard  
184 CPTu closely matches that of the slow CPTu (CPTu02), suggesting that drained conditions  
185 may have been achieved at the standard and lower penetration rates. The  $q_t$  values for  
186 CPTu10 and CPTu15 vary at certain depths, making the assessment of undrained conditions

187 more challenging compared to thickened tailings. The  $u_2$  values of the slow CPTu02 generally  
188 converge to the hydrostatic pore pressure profile, suggesting that the conventional tailings  
189 exhibit drained behavior at this push rate.  $u_2$  generally increases as the pushing rate increases  
190 up to 10 cm/s, after which it tends to decrease. As discussed previously, this reduction may  
191 be linked to viscosity effects at higher penetration rates.

## 192 Dissipation tests and $c_h$ estimation

193 Estimating  $V_h$  requires calculating  $c_h$ , which depends on  $t_{50}$  and  $Ir = G/Su$ , where  $G$   
194 is the operative shear modulus that can be linked to  $G_{max}$ . We estimate  $t_{50}$ ,  $G_{max}$ , and  
195  $Su$  using dissipation tests, CPTu-based shear wave velocity measurements, triaxial tests on  
196 recovered samples, and vane shear tests.

197 Dissipation tests were conducted at regular intervals on all CPTUs. Figure 6 presents  
198 normalized excess pore pressure dissipation curves below the groundwater level, plotted  
199 as  $\Delta u_2/u_{2,max}$  versus time, where  $\Delta u_2$  represents excess pore pressure and  $u_{2,max}$  is the  
200 maximum excess pore pressure recorded during dissipation. The curves are shown as a  
201 function of penetration rate (excluding 0.2 cm/s CPTus, as their initial pore pressure was  
202 close to hydrostatic) for tests conducted on thickened and conventional tailings. For the  
203 standard CPTu pushed at 2 cm/s, the dissipation curves for both thickened and conventional  
204 tailings fall within a relatively narrow range. In contrast, the curves show more variability  
205 for the CPTus pushed at 10 cm/s and 15 cm/s, particularly in the conventional tailings,  
206 likely due to their higher heterogeneity. The dissipation curves for the higher penetration  
207 rates decay more rapidly, suggesting partial consolidation effects in the standard 2 cm/s  
208 CPTu. Similar behavior was observed by [DeJong et al. \(2012\)](#) in cavity expansion analyses  
209 conducted by [Silva et al. \(2006\)](#) and experimental data on Kaolin from [Schneider et al.  
210 \(2007\)](#). This phenomenon occurs because partial consolidation during penetration slows the  
211 subsequent dissipation of pore pressure, leading to an overestimation of  $t_{50}$  compared to  
212 interpretations assuming fully undrained penetration, as also noted in the [Silva et al. \(2006\)](#)  
213 and [Schneider et al. \(2007\)](#) datasets. Since the fastest penetration rates are expected to

214 induce undrained conditions, the dissipation curves from these tests serve as the basis for  $t_{50}$   
215 interpretation. Figure 6 indicates  $t_{50}$  ranging from 3 to 7 s in the thickened tailings and 1  
216 to 8 s in the conventional tailings, with the lower range corresponding to the sandier units.

217 Figure 7a presents the results of vane shear tests conducted at a rotation rate of 0.1  
218 degrees/s on both thickened and conventional tailings. The tests indicate that  $Su$  values  
219 range from 50 to 70 kPa in the thickened tailings and from 40 to 110 kPa in the conventional  
220 tailings. Figure 7b shows the  $Su/\sigma'$  ratio estimated from laboratory triaxial tests, suggesting  
221 a consistent value of 0.2 for both thickened and conventional tailings. Section 4 provides a  
222 more detailed discussion of the available triaxial test results, and supplemental material A  
223 shows the interpretation of the strength ratios.

224 Figure 8 compares  $Su$  values estimated from vane shear and triaxial tests with those  
225 derived from CPTu data using  $Su = (q_t - \sigma_v)/N_{kt}$  and the CPTu pushed at 15 cm/s.  
226 An operational  $N_{kt} = 18$  is selected because it allows a reasonable consistency between  
227 vane shear and CPTu-based estimates. The potential range of  $Su$  values from vane shear,  
228 laboratory, and CPTu will be used in subsequent analyses. Figure 8 presents the variation  
229 of  $G_{max}$ , estimated from the measured  $V_s$  values using  $G_{max} = \rho V_s^2$ , where  $\rho$  is the density  
230 derived from CPTu data using the [Robertson and Cabal \(2022\)](#) correlation. The average  
231  $G_{max}$  values for thickened and conventional tailings are 65 MPa and 100 MPa, respectively.  
232 A curve fitting the  $G_{max}$  data,  $G_{max} = 60[p'/P_a]^{0.7}$ , where  $p'$  is the mean effective stress, is  
233 also included.

234 Using the plausible variations in  $Su$  and  $G_{max}$ , the  $G_{max}/Su$  ratio is estimated at depths  
235 where dissipation tests were conducted, with results shown in Figure 8d. Estimates also con-  
236 sider the [Krage et al. \(2014b\)](#) procedure, which uses an operative  $G$ . To evaluate  $G_{max}/Su$ ,  
237 the estimates were scaled by a factor of 3.84, following [Krage et al. \(2014b\)](#). The results  
238 indicate. The results indicate  $G_{max}/Su$  values ranging from 50 to 3000, with no significant  
239 distinction between thickened and conventional tailings.

240  $c_h$  is evaluated using  $t_{50}$  estimates at each depth and two approaches: [Teh and Houlsby](#)

241 (1991) with  $c_h = 0.245a^2\sqrt{I_r}/t_{50}$ , and Mayne et al. (2023) with  $c_h = 0.028a^2I_r^{0.75}/t_{50}$ . Since  
 242 the operative  $I_r$  in Teh and Houlsby (1991) is typically based on the secant shear modulus,  
 243  $G_{50}$  (Krage et al. 2014a),  $I_r$  is scaled by  $G_{50}/G_{max}$ . The Mayne et al. (2023) approach  
 244 considers the operative  $I_r$  based on the shear modulus at peak conditions,  $G_{peak}$ , so  $I_r$  is  
 245 scaled by  $G_{peak}/G_{max}$ .  $G_{50}/G_{max}$  and  $G_{peak}/G_{max}$  are estimated from available laboratory  
 246 tests (supplemental material A) and are, on average, 0.45 and 0.26 for thickened tailings and  
 247 0.30 and 0.19 for conventional tailings. Figure 8e presents the resulting  $c_h$  variations.

### 248 Assessment of rate effects and uncertainties

249 Using the previously discussed  $c_h$  estimates,  $Q$  backbone rate effect curves can now  
 250 be constructed. Figure 9 presents these curves at different depths for both thickened and  
 251 conventional tailings, using average  $c_h$  values. Following Dienstmann et al. (2018),  $Q$  values  
 252 at each depth are computed as the average over 10 cm intervals. The analysis for thickened  
 253 tailings focuses on the 6.0 m to 8.8 m depth interval (Figure 9a), which lies below the  
 254 groundwater table. Conventional tailings exhibit greater variability; hence, different layers  
 255 are analyzed based on the  $F_r$  variation (Figure 4). The considered depth intervals are: 8.8 –  
 256 9.8 m (Figure 9b), 9.8 – 12.2 m (Figure 9c), and 12.2 – 13.0 m (Figure 9d). Depths below 13  
 257 m are excluded since the slow CPTu at 0.2 cm/s did not reach those depths. At depths with  
 258 significant layering, such as 9.8 – 12.2 m, increased variability in  $Q$  is observed. However,  
 259 the expected trend of decreasing  $Q$  with increasing  $V_h = 0.1$  remains. In more homogeneous  
 260 depths, particularly within thickened tailings, the backbone rate effect curves exhibit clearer  
 261 trends.

262 Empirical upper and lower boundaries are included using the DeJong et al. 2012 for-  
 263 mulation, which estimates  $Q$  using  $Q/Q_U = 1 + (Q - Q_U)/(1 + (V/V_{50})^c)$ , where  $V_{50}$  and  
 264  $c$  are fitting parameters and the remaining variables are as defined before. Figure 9 shows  
 265 the estimated upper and lower boundaries. A distinct trend emerges in the drained and  
 266 undrained behavior of the two tailings types. In thickened tailings, the definition of drained  
 267 conditions remains uncertain, while in conventional tailings, there is more uncertainty in

determining undrained conditions, particularly in the depth intervals of 8.8 - 9.8 m and 12.2 - 13.0 m. At a penetration rate of 0.2 cm/s, conventional tailings reach drained conditions at  $V_h = 0.1$ , but achieving fully undrained conditions may require  $V_h > 10$ , which exceeds the fastest CPTu penetration rate used. In contrast, thickened tailings require lower penetration rates,  $V_h < 0.1$ , than the slowest CPTu to reach drained conditions, while undrained conditions occur at  $V_h$  of about 30, corresponding to the fastest penetration rate. Representative depths at 7.35 m (thickened tailings) and 12.60 m (conventional tailings) are selected to further illustrate uncertainties. Figure 10 presents backbone curves derived using the DeJong et al. (2012) functional form. In thickened tailings, various combinations of  $V_{50}$  and  $c$  are possible for the collected data, leading to uncertainties in  $Q_D$  and  $Q_D/Q_U$  as Figure 10a shows. For conventional tailings, a range of  $Q_U$  values (2 to 10), informed by Figure 9, produces backbone curves that align well with the collected data, suggesting a plausible  $Q_D/Q_U$  ratio between 2.5 and 10, as illustrated in Figure 10b.

## INTERPRETATIONS INTEGRATING NUMERICAL SIMULATIONS AND LABORATORY TESTING

This section presents a framework that incorporates numerical simulations of the CPTu penetration process to aid in interpreting variable penetration rate CPTus when uncertainties exist in reaching drained or undrained conditions. Figure 11 outlines the general framework and its sequential steps. Step 1 has already been addressed in the previous section, which highlights the uncertainties in defining drained or undrained responses. The following subsections will demonstrate Steps 2 to 4 using the collected data and representative depths at 7.35 m for the thickened tailings and 12.60 m for the conventional tailings.

### CPTu penetration modeling and constitutive model

We conduct numerical simulations with a focus on large deformations using the geotechnical particle finite element method (G-PFEM). G-PFEM has been applied in various geotechnical problems, including granular flow, landslides, and contact problems (e.g., Zhang et al. 2013; Cante et al. 2014; Cremonesi et al. 2011; Franci et al. 2020; Ciantia 2024; Monforte

295 [et al. 2017b](#); [Previtali et al. 2023](#)), as well as CPTu penetration simulations ([Monforte et al.](#)  
 296 [2021](#); [Oliynyk et al. 2022](#); [Ciantia et al. 2022](#)). [Cremonesi et al. \(2020\)](#) provide a detailed com-  
 297 parison between G-PFEM and the traditional finite element method (FEM). Unlike FEM,  
 298 G-PFEM treats nodes as "particles" that act as discrete material points carrying information  
 299 on velocity, displacement, and stress. These particles dynamically update the mesh using  
 300 different re-meshing boundary condition treatment techniques, such as Delaunay Tessellation  
 301 and the alpha-shape method ([Cremonesi et al. 2020](#)). We use the G-PFEM implementation  
 302 in the multiphysics platform Kratos ([Monforte et al. 2017a](#)) with the GiD package ([Ribó](#)  
 303 [et al. 1998](#)) for pre- and post-processing. G-PFEM can accommodate advanced constitu-  
 304 tive models; we use CASM (Clay and Sand Model) initially proposed by [Yu \(1998\)](#), which  
 305 has been previously used in several CPTu penetration-focused efforts ([Monforte et al. 2021](#);  
 306 [Monforte et al. 2023](#); [Boschi et al. 2024](#)). Figure 12 illustrates the key features of CASM  
 307 in the  $p'$ - $\nu$  and  $p'$ - $q$  spaces, where  $\nu = e + 1$  is the specific volume, with  $e$  being the void  
 308 ratio. The supplemental material B provides a summary of CASM's constitutive equations.  
 309 CASM extends the Cam Clay model ([Roscoe and Burland 1968](#)) by incorporating the state  
 310 parameter ( $\psi$ , [Been and Jefferies 1985](#)). The model defines a reference consolidation line  
 311 (RCL) parallel to the critical state line (CSL), separated by a distance  $r$ . The CSL has a  
 312 slope  $\lambda$  and an altitude  $\Gamma$  (Figure 12a). The RCL corresponds to a reference state parameter  
 313 ( $\psi_r$ ), which relates to  $r$  as  $\psi_r = (\lambda - \kappa) \ln r$ , where  $\kappa$  is the recompression curve slope. The  
 314 yield surface shape in  $p'$ - $q$  space is controlled by parameter  $n$  (Figure 12b), and the CSL in  
 315 this space has a slope  $M_{tc}$  for triaxial compression conditions. A hardening law similar to  
 316 that of the Cam Clay model governs the evolution of the yield surface (supplemental material  
 317 B), which depends on the initial mean pressure ( $p'_0$ ), the initial specific volume ( $\nu_{init}$ ),  $\lambda$ , and  
 318  $\kappa$ . Plastic volumetric strain generation is controlled by a non-associative flow rule and the  
 319 constitutive parameter  $m$ . Elasticity is characterized by  $G$  and the bulk modulus  $K$ , which  
 320 can be estimated from  $\kappa$  as in Cam Clay. CASM parameters include  $\Gamma$ ,  $\lambda$ ,  $\kappa$ ,  $M_{tc}$ ,  $n$ ,  $r$ , and  
 321  $G$ , all of which can be calibrated from experimental tests. Additionally, forward predictions

322 require the initial state parameter  $\psi_0$ , estimated as  $\psi_0 = \nu_{init} - \Gamma + \lambda \ln(p')$ . The next section  
323 discusses the calibration of the required parameters based on the available testing.

### 324 **Laboratory testing and model calibration**

325 The CASM parameters are calibrated using triaxial test data for both thickened and  
326 conventional tailings. The testing program includes seven triaxial tests on thickened tailings  
327 (Figure 7a) and five tests on conventional tailings (Figure 7b). The supplemental material  
328 A provides additional details on the triaxial tests. Using the terminology from [Macedo and](#)  
329 [Vergaray \(2022\)](#), the undrained response in thickened tailings varies from partial softening,  
330 where  $q$  decreases after peak to a nonzero value (observed in TXCU1 and TXCU2), to  
331 limited flow, where the response transitions from contractive to dilative after significant  
332 shearing (observed in TXCU3). The drained responses exhibit hardening, where  $q$  increases  
333 monotonically in initially loose samples with a positive initial  $\psi$  (TXCD1 and TXCD2). In  
334 contrast, initially dense samples (negative initial  $\psi$ ) show a peak in  $q$ , indicative of maximum  
335 dilation, followed by softening. Conventional tailings exhibit similar response patterns, but  
336 all tests were conducted on initially loose samples, placing them above the CSL (Figure 7b).  
337 The critical state lines (CSLs) in the  $p' - e$  and  $p' - q$  spaces are estimated by fitting the test  
338 endpoints, yielding  $\lambda$ ,  $\Gamma$ , and  $M_{tc}$  values summarized in Table 2, which are directly used as  
339 CASM parameters. The initial pre-shearing states of both tailings are used to estimate the  
340 reference consolidation lines (RCLs), from which  $\psi_r$  values of 0.1 (thickened tailings) and 0.09  
341 (conventional tailings) are obtained. These values are used to estimate  $r$ . The calibration  
342 of  $n$ ,  $m$ , and  $G$  follows an iterative forward approach, where parameter adjustments are  
343 made by comparing experimental and numerical responses. This approach is commonly  
344 used in constitutive model calibration (e.g., [Shuttle and Jefferies 2016](#)). Table 2 summarizes  
345 the final calibrated CASM parameters. Figures 7a and b compare the experimental results  
346 with CASM numerical simulations, showing that the simulations reproduce the experimental  
347 patterns and are considered satisfactory. The calibrated parameters will be used for CPTu  
348 penetration simulations.

## CPTu penetration simulations and constraining of backbone rate effect curves

The CPTu penetration process is simulated using the axisymmetric mesh shown in Figure 14, following procedures similar to those described by Monforte et al. (2018) and Monforte et al. (2021). The mesh dimensions are 0.66 m by 1.31 m, corresponding to 30 and 60 times the radius ( $R$ ) of a 15 cm<sup>2</sup> cone. Boundary conditions constrain radial displacements ( $u_r$ ) at the lateral boundaries and both radial and vertical displacements ( $u_y$ ) at the bottom boundary. Pore pressures ( $u_w$ ) are also fixed at the bottom boundary to prevent excess pore pressure generation. The cone is treated as a rigid body, and its interaction with the soil is modeled using a contact model based on the penalty method (Wriggers and Laursen 2006). Normal stresses develop as part of the contact model, while tangential stresses are computed using procedures outlined by Wriggers (1995) and Wriggers and Laursen (2006), with slip-yield conditions following Monforte et al. (2018). This contact model has been widely applied in previous CPTu penetration studies (e.g., Monforte et al. 2021), and further details can be found in Monforte et al. (2018). The mesh discretization employs linear triangular elements, with refinement in the region surrounding and beneath the cone (extending approximately 25R) using an average element size of 4 mm. Element sizes increase further from the cone's influence zone, reaching approximately 50 mm near the boundaries. Vertical stresses are initialized based on the in situ stress conditions at the analyzed depths (7.35 m for thickened tailings and 12.60 m for conventional tailings) by applying a distributed vertical load at the top boundary. Horizontal stresses are initialized, assuming a  $K_0$  value of 0.70. At the start of the simulation, the cone is embedded at a depth of  $10R$ , after which the penetration simulation begins. Following the methodology of Monforte et al. (2021), Ceccato et al. (2016), and Ceccato and Simonini (2017), the cone advances at a constant velocity of 2 cm/s in all simulations. However, hydraulic conductivity is varied across six orders of magnitude, ranging from  $10^{-5}$  to  $10^{-10}$  cm/s, to simulate drained and undrained conditions. Consistent with Monforte et al. (2018), the mesh refinement criterion is governed by plastic shear strain evolution. When an element exceeds a plastic shear strain of 0.01%, additional nodes are

376 introduced, and node information is updated accordingly.

377 Figure 15 presents typical contours of mean stresses, deviatoric stresses, and excess pore  
378 pressures under drained, partially drained, and undrained conditions for thickened tailings,  
379 using  $\psi_0 = 0.025$  and the parameters in Table 2 for illustration. The drained simulations  
380 produce negligible excess pore pressures, whereas excess pore pressures increase within the  
381 cone’s influence zone as the response transitions to undrained conditions. Mean stresses  
382 are higher in drained simulations and decrease near the cone as the response becomes more  
383 undrained. Conversely, deviatoric stresses follow an inverse trend, increasing as the response  
384 transitions from undrained to drained. The response patterns in conventional tailings follow  
385 similar trends and are omitted for brevity. Overall, the results qualitatively align with vari-  
386 able rate CPTu simulations from previous studies (e.g., [Monforte et al. 2021](#); [Oliynyk et al.](#)  
387 [2022](#)). Figure 16 illustrates the typical variation of  $Q$  extracted from numerical simulations  
388 using the same input parameters while varying hydraulic conductivity ( $k$ ) between  $10^{-5}$  and  
389  $10^{-10}$  cm/s. The results for both thickened and conventional tailings show that as  $k$  increases  
390 (i.e.,  $V_h$  decreases),  $Q$  approaches  $Q_D$ , and as  $k$  decreases (i.e.,  $V_h$  increases),  $Q$  approaches  
391  $Q_U$ .

392 The missing parameter needed to estimate backbone rate effect curves is  $\psi$ . We propose  
393 an iterative procedure to determine  $\psi$ : (1) select  $\psi$  range and conduct simulations for drained  
394 or undrained conditions using the upper and lower bounds of the selected range; (2) compare  
395 the numerically obtained  $Q_D$  or  $Q_U$  with field-measured values; (3) interpolate to update  $\psi$   
396 based on the difference between numerical and field values of  $Q_D$  or  $Q_U$  from step 2; and  
397 (4) repeat steps 1 to 3 until the numerical  $Q_D$  or  $Q_U$  matches the field values, defining  $\psi$  as  
398 the value that achieves this match. Figure 17 illustrates this procedure. For the thickened  
399 tailings, we use  $Q_U$  because undrained conditions are reached at the fastest penetration rate,  
400 as previously discussed. The initial  $\psi$  range is set between 0.00 and 0.05, and simulations  
401 at  $\psi = 0.00$  and  $\psi = 0.05$  define the range indicated by the horizontal arrow at 7.35  
402 m in Figure 17. Based on the difference between the numerical and field  $Q_U$ , the next

403 iteration interpolates  $\psi = 0.025$ ; the numerically updated  $Q_U$  now matches the field  $Q_U$  and  
 404 is therefore selected. For the conventional tailings, we follow the same procedure but use  $Q_D$   
 405 since drained conditions are reached in the field. The initial  $\psi$  range is again set between  
 406 0.00 and 0.05, with  $Q_D$  results indicated by the horizontal arrow at 12.60 m in Figure 17.  
 407 Coincidentally,  $\psi$  is also estimated as 0.025 at this depth. Using the estimated  $\psi$  values at  
 408 each depth and the calibrated parameters in Table 2, we proceed with numerical simulations  
 409 across a range of  $V_h$  values to construct the backbone rate effect curves.

410 The  $c_h$  required to estimate  $V_h$  from numerical simulations is [Monforte et al. \(2021\)](#):

$$c_h = \frac{\sigma'_{v0}(1 + e_0)k}{\lambda\gamma_w}$$

411 where  $\gamma_w$  is the water unit weight, and the remaining variables are as previously defined.  
 412 This expression implies that  $c_h$  is governed by conditions along the virgin compression curve.  
 413 An alternative approach replaces  $\lambda$  with  $\kappa$ , in which case  $c_h$  reflects conditions along the re-  
 414 compression line, where elasticity is typically assumed ([Mahmoodzadeh et al. 2014](#)). Given  
 415 the complex stress conditions when the CPTu penetrates, [Mahmoodzadeh et al. \(2014\)](#)  
 416 recommends using an operative  $c_h$ , which accounts for both  $\lambda$  and  $\kappa$  according to:

$$c_{op} = \frac{1 - \mu}{1 + \mu} \frac{(1 + 2K_0)\sigma'_{v0}(1 + e_0)k}{\lambda^{(1-\alpha)}\kappa^\alpha\gamma_w}$$

417 where  $\mu$  is the Poisson ratio, and  $\alpha$  represents the tradeoff between  $\lambda$  and  $\kappa$  in controlling  
 418 compressibility effects. Figure 18 presents backbone rate effect curves using operative  $c_h$   
 419 values derived from  $\lambda$ ,  $\kappa$ , and the  $\lambda$ - $\kappa$  tradeoff, following [Mahmoodzadeh et al. \(2014\)](#) with  
 420  $\alpha = 0.5$ ,  $\mu = 0.3$ , and  $K_0 = 0.7$ . The numerical simulations estimate  $Q$ , while  $V_h$  is  
 421 computed as  $V_h = vd/c_h$ . The curves based solely on  $\lambda$  and  $\kappa$  establish upper and lower  
 422 boundaries, respectively, with the  $\lambda$ - $\kappa$  tradeoff curve positioned between them, closer to  
 423 the  $\kappa$ -based curve. The experimental backbone curves at 7.35 m (thickened tailings) and  
 424 12.60 m (conventional tailings) are shown in Figure 18, considering the variation of field-

425 based  $c_h$  from Figure 8e and the  $Q$  range (estimated as the variation within 10 cm). The  
426 experimental curve shapes at low and high  $V_h$  are guided by the numerical simulations for  
427 the thickened and conventional tailings, respectively. These simulations constrain  $Q_D$  for the  
428 thickened tailings and  $Q_U$  for the conventional tailings and the range of field backbone rate  
429 effect curves, which aids in identifying the operative field  $c_h$ . For instance, in the thickened  
430 tailings at 7.35 m depth, numerical simulations constrain  $c_h$  within 1.25–2.50 cm<sup>2</sup>/s, while in  
431 the conventional tailings at 12.6 m, the field  $c_h$  is constrained to 4.25–8.50 cm<sup>2</sup>/s. The results  
432 also suggest that partially drained conditions occur for  $V_h$  between 1–30 in the thickened  
433 tailings and 2–200 in the conventional tailings. The estimated  $Q_D/Q_U$  ratios are 3.2 for the  
434 thickened tailings and 3.0 for the conventional tailings. The framework discussed in this  
435 section provides a systematic approach to constraining  $Q_D/Q_U$ ,  $\psi$ , operative  $c_h$ , and the  
436 range of partially drained responses, particularly when uncertainty exists regarding whether  
437 drained or undrained conditions are achieved in the field.

## 438 CONCLUSIONS

439 This study utilized variable rate CPTu tests (ranging from 0.2 cm/s to 15 cm/s), com-  
440 plemented by laboratory testing and additional field data from a TSF containing two dis-  
441 tinct tailings types (thickened and conventional), to advance the understanding of partially  
442 drained responses in mine tailings. Previous field-scale studies on partially drained responses  
443 in mine tailings are scarce and, to the best of our knowledge, have been limited to the Fazenda  
444 Brasileiro TSF in Brazil. Expanding case studies of variable rate CPTu tests on mine tail-  
445 ings, as done in this study, is encouraged and would complement similar ongoing efforts in  
446 natural silts (e.g., [Paniagua et al. 2021](#)).

447 The results highlight greater variability in backbone rate effect curves for conventional  
448 tailings, leading to more uncertainties in assessing partially drained responses compared to  
449 thickened tailings. This increased uncertainty stems from the more segregating nature and  
450 layering in conventional tailings, which are directly linked to their deposition process. Addi-  
451 tionally, the findings underscore challenges in interpreting drained and undrained responses

452 at the examined CPTu penetration rates. These challenges are associated with (1) the vari-  
453 ability in key parameters such as  $I_r$  and  $c_h$ , which affect partially drained responses, and (2)  
454 the penetration rates achievable in the field.

455 This study introduced a framework that integrates numerical simulations of CPTu pen-  
456 etration with laboratory testing to support the interpretation of variable rate CPTu data  
457 (Figure 11). The framework was demonstrated using the CASM model and G-PFEM but  
458 can also incorporate other constitutive models, such as Norsand (Jefferies and Been 2015),  
459 and alternative large deformation numerical schemes, such as MPM. We advocate for the  
460 use of critical state soil mechanics models, as they provide a balance between robustness  
461 and calibration effort and are already widely applied in tailings engineering. The Norsand  
462 model, for example, has been used in forensic investigations of recent failures, including  
463 Fundão (Morgenstern et al. 2016), Feijão (Robertson et al. 2019), and Cadia (Morgenstern  
464 et al. 2019).

465 We also believe that robust large deformation schemes to interpret CPTu tests like G-  
466 PFEM and MPM should be preferred over traditional approaches, such as cavity expansion,  
467 due to their advantages in simulating complex penetration processes. With the increasing  
468 availability of computational resources and advancements in large deformation numerical  
469 techniques (e.g., Ceccato et al. 2024), we advocate for their adoption in engineering practice  
470 as they can bring useful insights, as showcased in this study, to interpret partially drained  
471 CPTu responses.

## 472 DATA AVAILABILITY STATEMENT

473 Some or all data, models, or code that support the findings of this study are available  
474 from the corresponding author upon reasonable request.

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## List of Tables

668

1 Average particle size distribution properties and Atterberg Limits for the conventional and thickened tailings . . . . . 27

669

670

2 Calibrated CASM parameters for the considered thickened and conventional tailings . . . . . 28

671

**TABLE 1. Average particle size distribution properties and Atterberg Limits for the conventional and thickened tailings**

Property	Conventional tailings	Thickened tailings
Sand fraction (%)	28.70	24.70
Silt fraction (%)	67.70	70.90
Clay fraction (%)	3.60	4.40
Specific gravity ( $G_s$ )	3.31	3.38
Liquid limit ( $LL$ )	22	22
Plasticity index ( $PI$ )	2	2

**TABLE 2. Calibrated CASM parameters for the considered thickened and conventional tailings**

Parameter	Thickened tailings	Conventional tailings
$\Gamma$	2.174	2.217
$\lambda$	0.065	0.068
$\kappa$	0.032	0.034
$M_{tc}$	1.55	1.55
$n$	1.5	1.5
$r$	6.8	6.0
$m$	2.4	2.4
$\psi_r$	0.10	0.09
$G$	14 MPa	14 MPa

672

## List of Figures

673	1	Illustration of partially drained effects on contractive and dilative materials.	31
674	2	Range of particle size distributions for thickened and conventional tailings. .	32
675	3	Schematic representation for the location of variable penetration rate CPTus	
676		on the investigated TSF . . . . .	33
677	4	Variation of $q_t$ , $f_s$ , $u_2$ , $I_c$ , $V_s$ , $V_p$ , $Q$ , $F_r$ , and $I_B$ ; for CPTu2 pushed at the	
678		standard penetration rate of 2 cm/s. The CPTu data is also shown on the	
679		SBTn chart proposed by Robertson (2016) . . . . .	34
680	5	Variation of $q_t$ , $f_s$ and $u_2$ for CPTus pushed at 0.2 cm/s, 2 cm/s, 10 cm/s,	
681		and 15 cm/s. The CPTu data is also plotted on the SBTn chart proposed by	
682		Robertson (2016) for illustrative purposes. . . . .	35
683	6	Normalized excess pore pressure evolution from dissipation tests performed at	
684		CPTus pushed at 2cm/s, 10 cm/s, and 15 cm/s. Responses are shown for a)	
685		thickened tailings and b) conventional tailings. . . . .	36
686	7	(a) Responses from vane shear testing (VST). (b) Estimation of peak strength	
687		undrained ratio ( $Su/\sigma'_v$ ) from undrained triaxial tests . . . . .	37
688	8	Variation of (a) $Su$ , (b) $V_s$ , (c) $G_{max}$ , (d) $G_{max}/Su$ , (e) $c_h$ versus depth. See	
689		the text for additional details. . . . .	38
690	9	Range of potential backbone rate effect curves for (a) thickened tailings be-	
691		tween 6.0 - 6.8 m, and conventional tailings between (b) 8.8 - 9.8 m, (c) 9.8 -	
692		12.8 m, and (d) 12.2 - 13.0 m. . . . .	39
693	10	Plausible backbone rate effect curves for (a) thickened tailings at 7.35 m, and	
694		(b) conventional tailings at 12.6 m. The different curves are fitted to the field	
695		data using the functional form from DeJong et al. (2012) . . . . .	40
696	11	General framework to interpret variable penetration rate CPTus . . . . .	41

697	12	Clay and Sand Model (CASM) ingredients (a) features in the $p'$ - $e$ space, (b)	
698		yield surface shape and variation. Additional details are discussed in the text	
699		and electronic supplement. . . . .	42
700	13	Comparisons of numerical responses obtained from CASM and experimental	
701		responses for (a) thickened tailings, (b) conventional tailings . . . . .	43
702	14	Mesh discretization and boundary conditions for the G-PFEM based CPTu	
703		penetration simulations . . . . .	44
704	15	Distribution of (a) $p'$ , (b) $q$ , and (c) excess pore pressure, $\Delta u$ (bottom) at	
705		the end of penetration. The left, middle, and right columns correspond to	
706		drained, partially drained, and undrained responses, respectively . . . . .	45
707	16	Variation of $Q$ versus depth obtained from PFEM-based CPTu penetration	
708		simulations for (a) thickened tailings and (b) conventional tailings considering	
709		different $k$ . . . . .	46
710	17	Illustration of the interpolation procedure to estimate $\psi$ . The horizontal ar-	
711		rows at 7.35 m and 12.60 m represent the range of responses for $\psi = 0.0 - 0.05$	
712		used to inform the next iteration with $\psi = 0.025$ . . . . .	47
713	18	Constraining of field-based backbone rate effect curves by using PFEM-based	
714		numerical simulations. Notice the narrower range obtained from numerical	
715		simulations. Results shown for (a) thickened tailings at 7.35 m and (b) con-	
716		ventional tailings at 12.60 m. . . . .	48

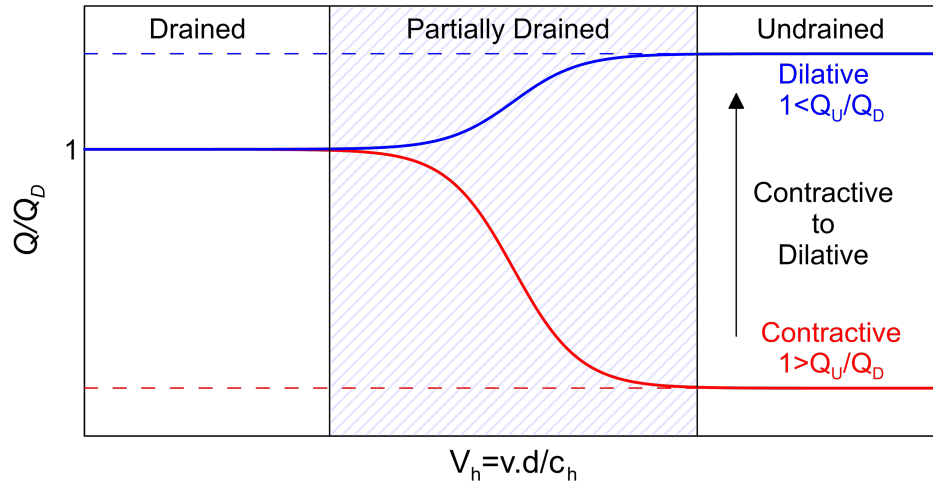


FIG. 1. Illustration of partially drained effects on contractive and dilative materials.

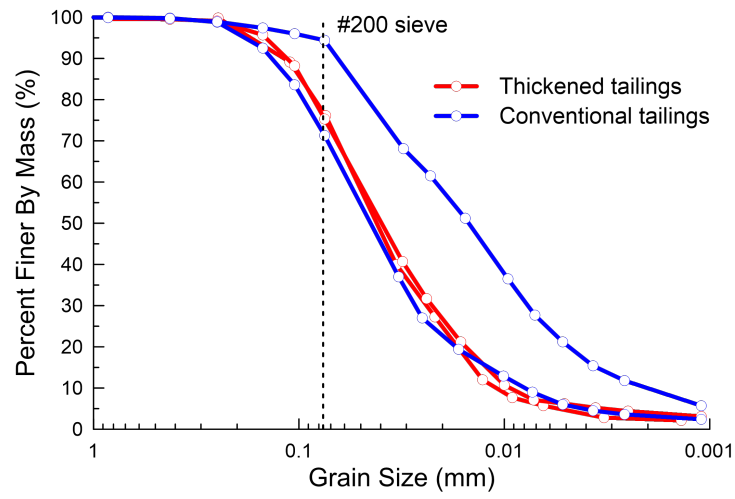
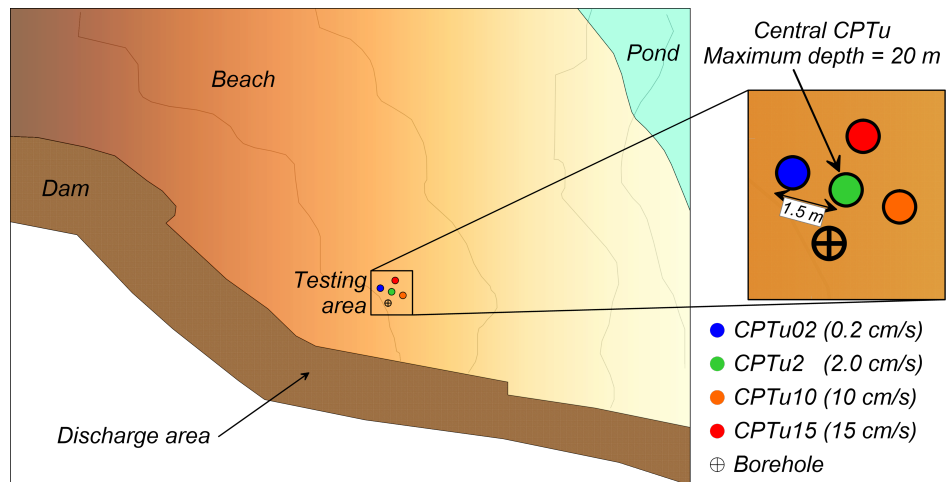
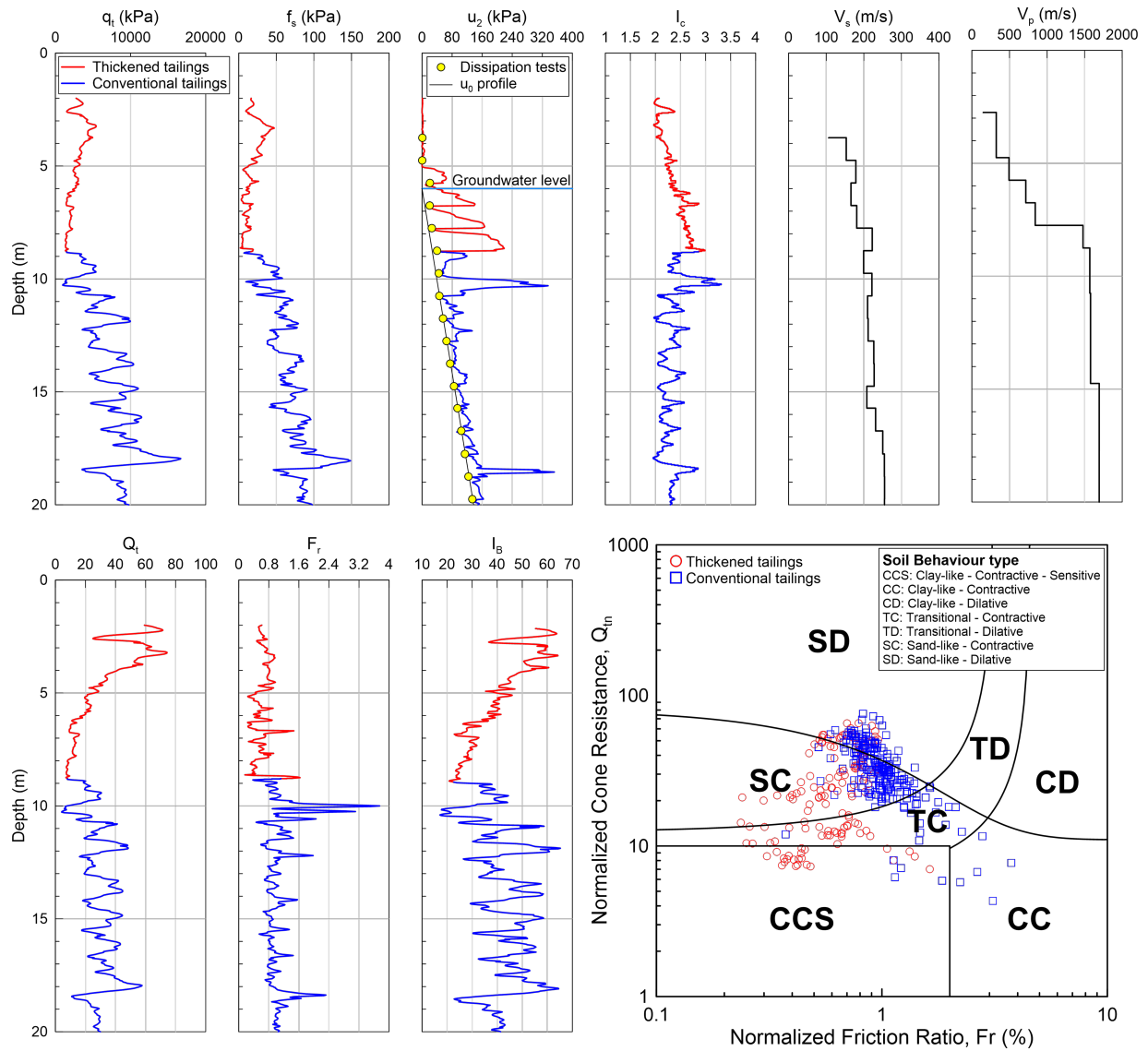


FIG. 2. Range of particle size distributions for thickened and conventional tailings.



**FIG. 3. Schematic representation for the location of variable penetration rate CPTs on the investigated TSF**



**FIG. 4. Variation of  $q_t$ ,  $f_s$ ,  $u_2$ ,  $I_c$ ,  $V_s$ ,  $V_p$ ,  $Q_c$ ,  $F_r$ , and  $I_B$ ; for CPTu2 pushed at the standard penetration rate of 2 cm/s. The CPTu data is also shown on the SBTn chart proposed by Robertson (2016)**

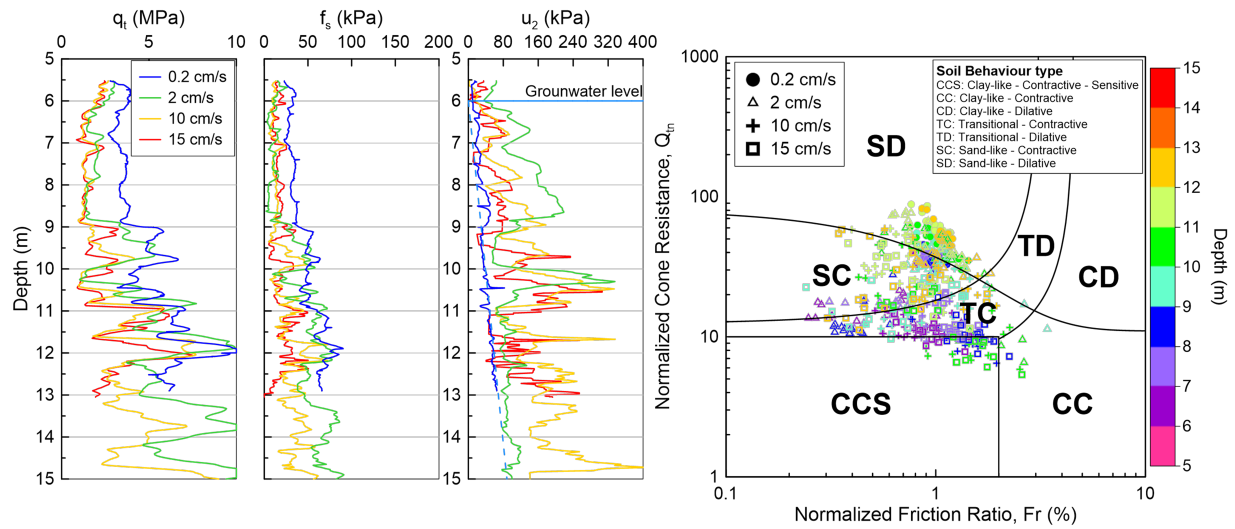
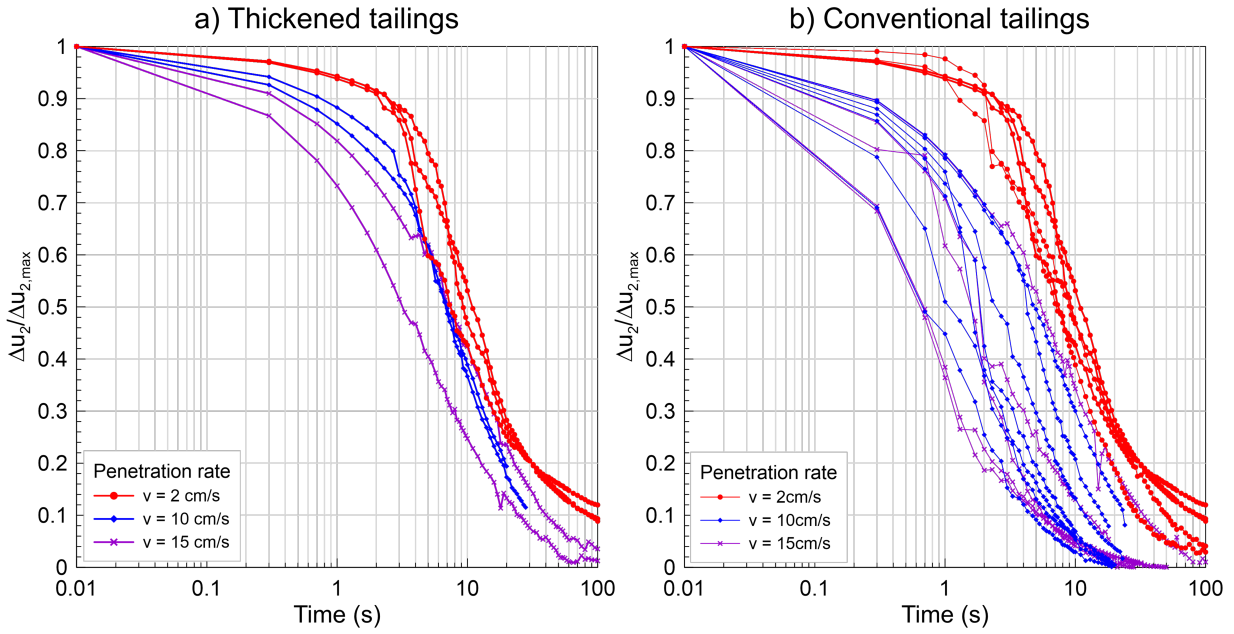
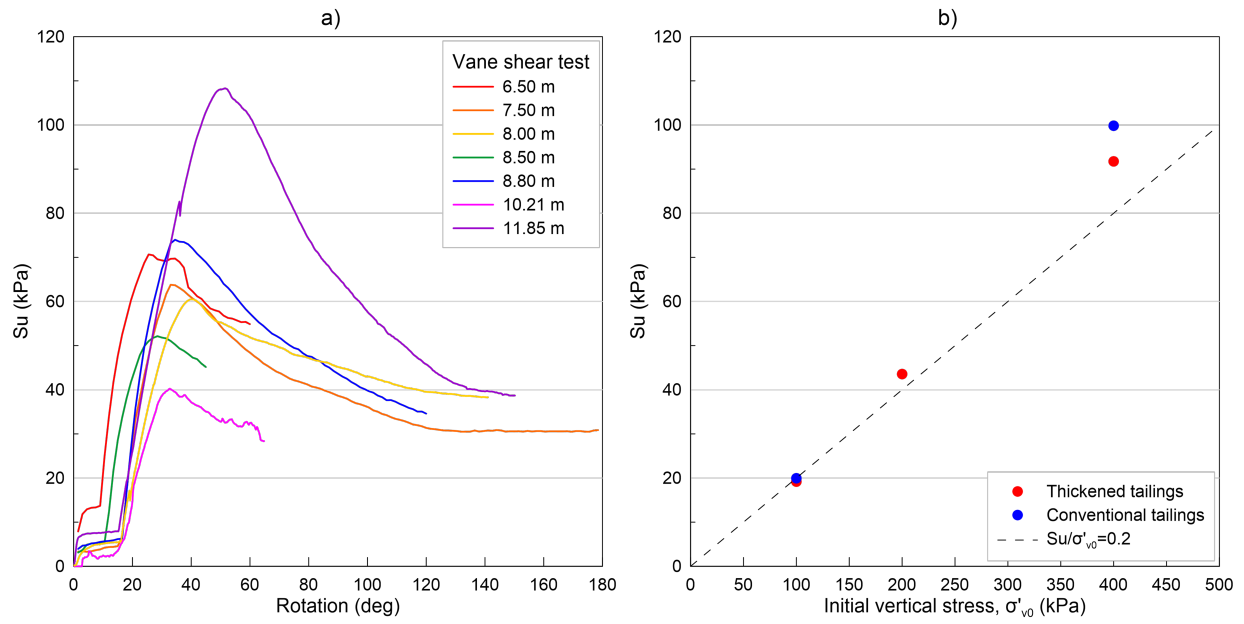


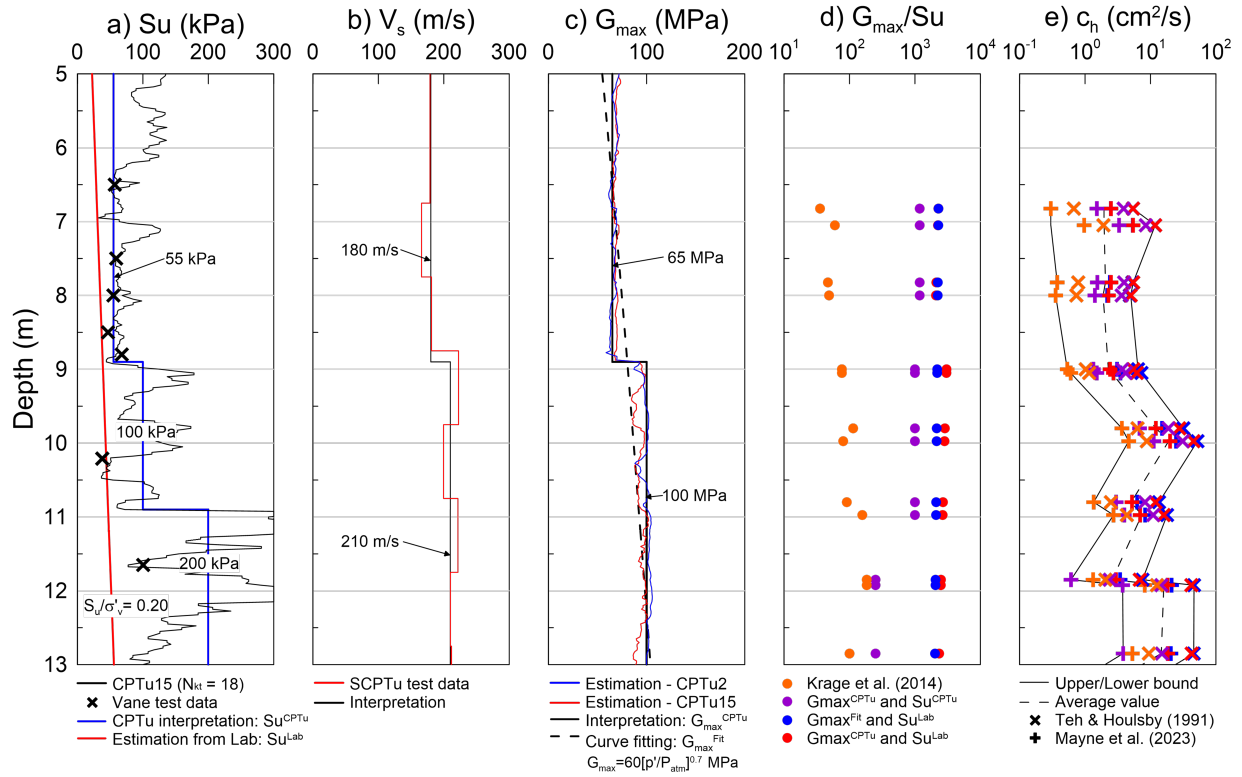
FIG. 5. Variation of  $q_t$ ,  $f_s$  and  $u_2$  for CPTu pushed at 0.2 cm/s, 2 cm/s, 10 cm/s, and 15 cm/s. The CPTu data is also plotted on the SBTn chart proposed by Robertson (2016) for illustrative purposes.



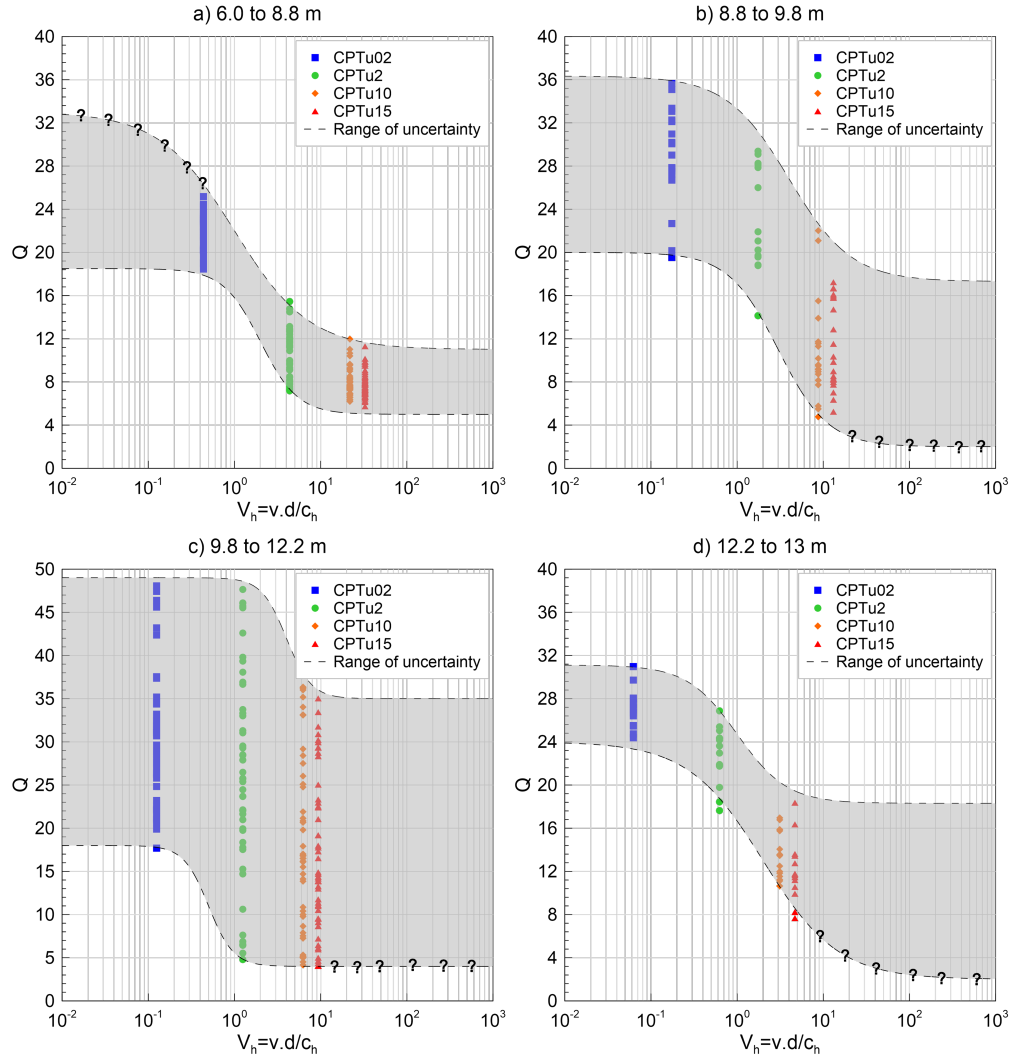
**FIG. 6.** Normalized excess pore pressure evolution from dissipation tests performed at CPTus pushed at 2cm/s, 10 cm/s, and 15 cm/s. Responses are shown for a) thickened tailings and b) conventional tailings.



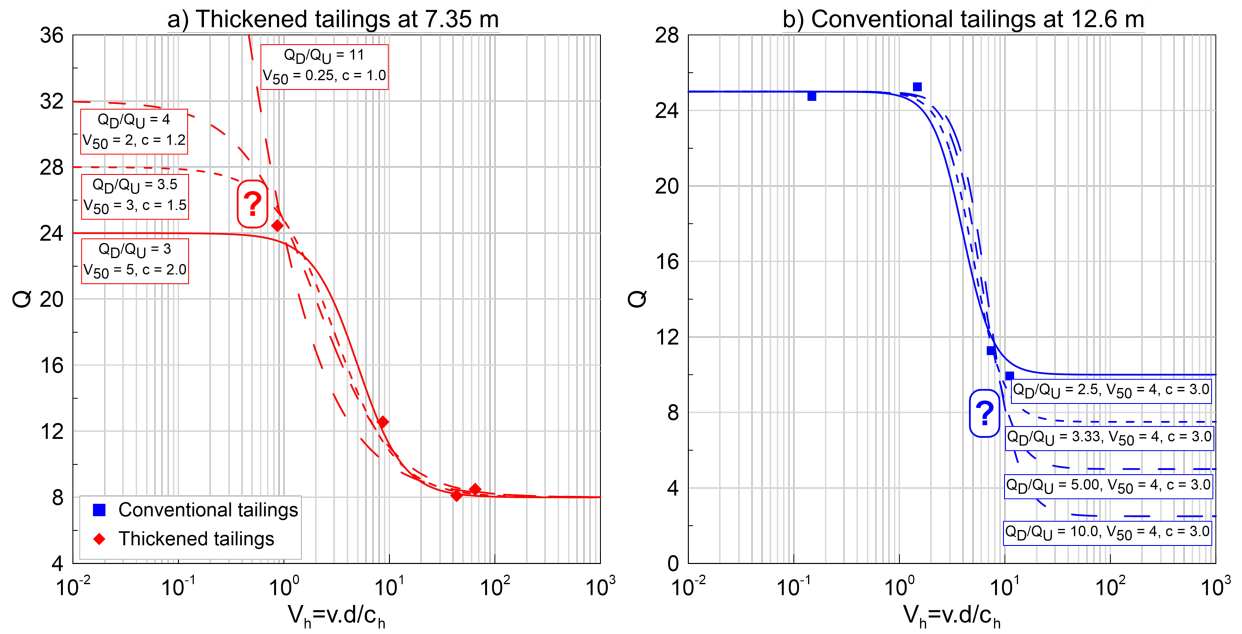
**FIG. 7. (a) Responses from vane shear testing (VST). (b) Estimation of peak strength undrained ratio ( $S_u/\sigma'_v$ ) from undrained triaxial tests**



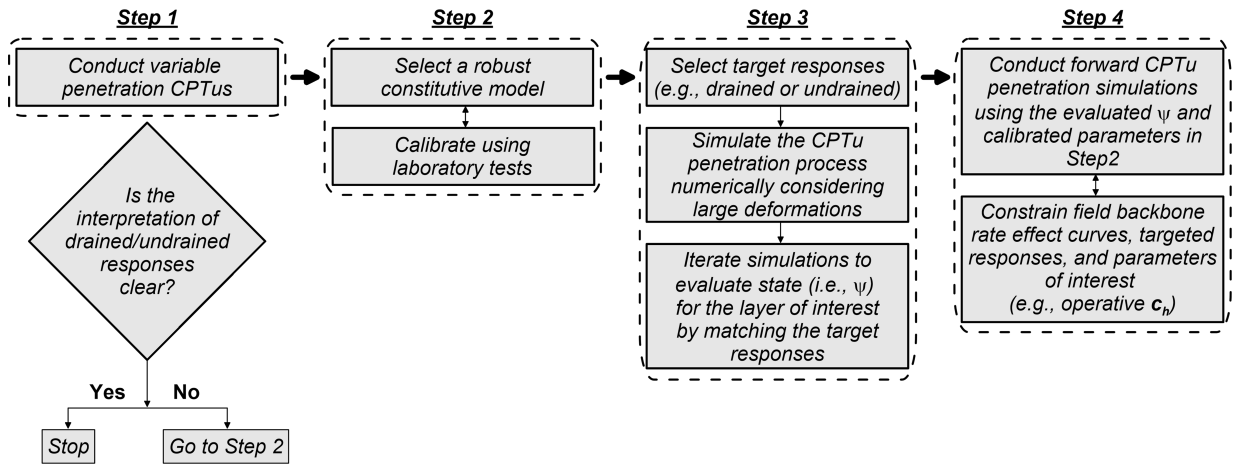
**FIG. 8. Variation of (a)  $S_u$ , (b)  $V_s$ , (c)  $G_{max}$ , (d)  $G_{max}/S_u$ , (e)  $c_h$  versus depth. See the text for additional details.**



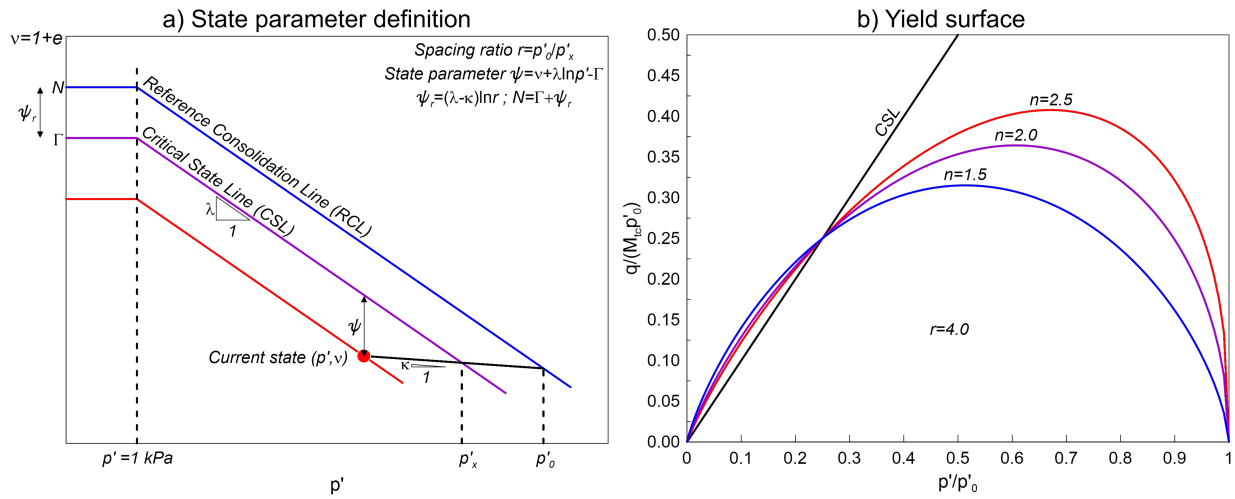
**FIG. 9.** Range of potential backbone rate effect curves for (a) thickened tailings between 6.0 - 6.8 m, and conventional tailings between (b) 8.8 - 9.8 m, (c) 9.8 - 12.8 m, and (d) 12.2 - 13.0 m.



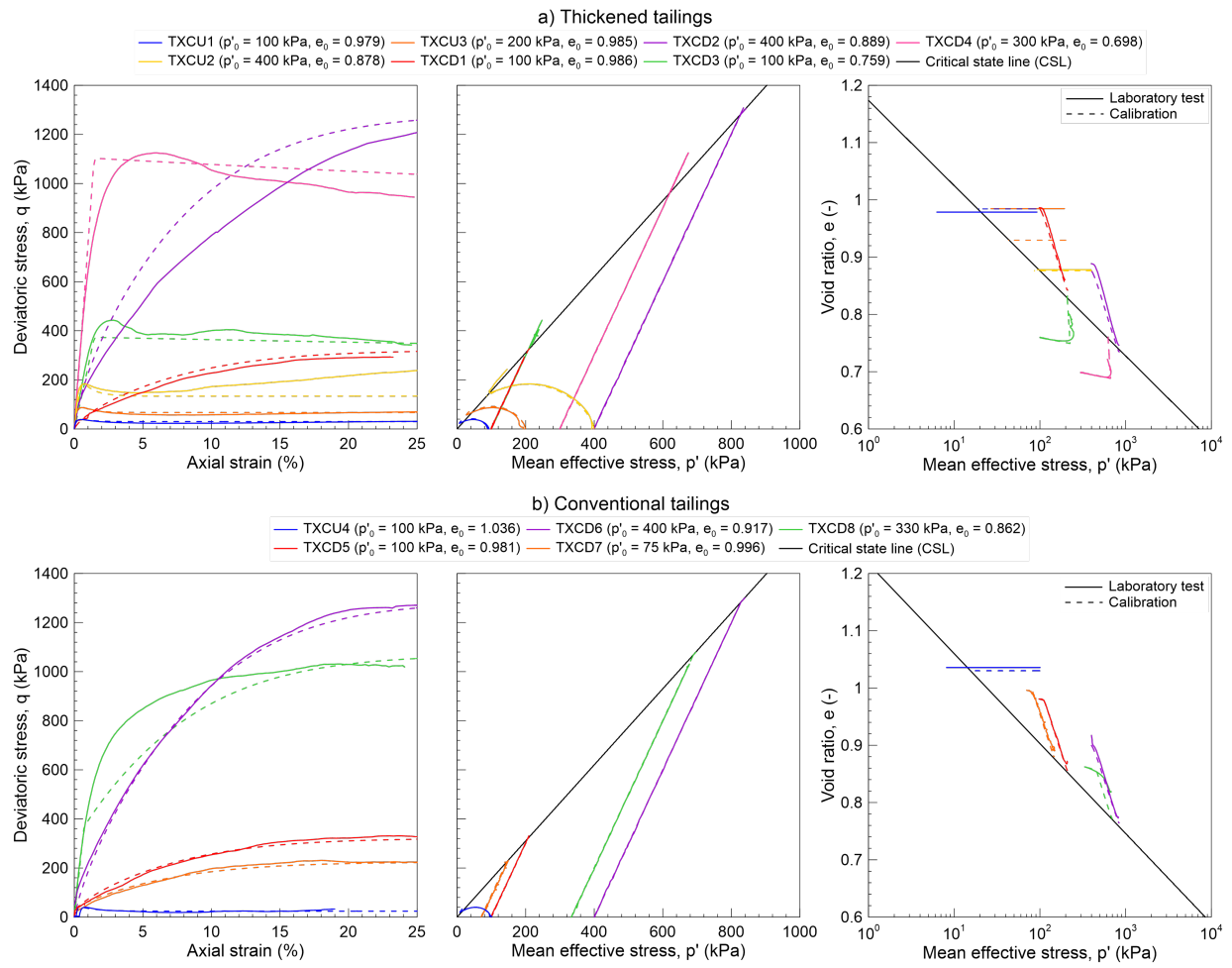
**FIG. 10. Plausible backbone rate effect curves for (a) thickened tailings at 7.35 m, and (b) conventional tailings at 12.6 m. The different curves are fitted to the field data using the functional form from DeJong et al. (2012)**



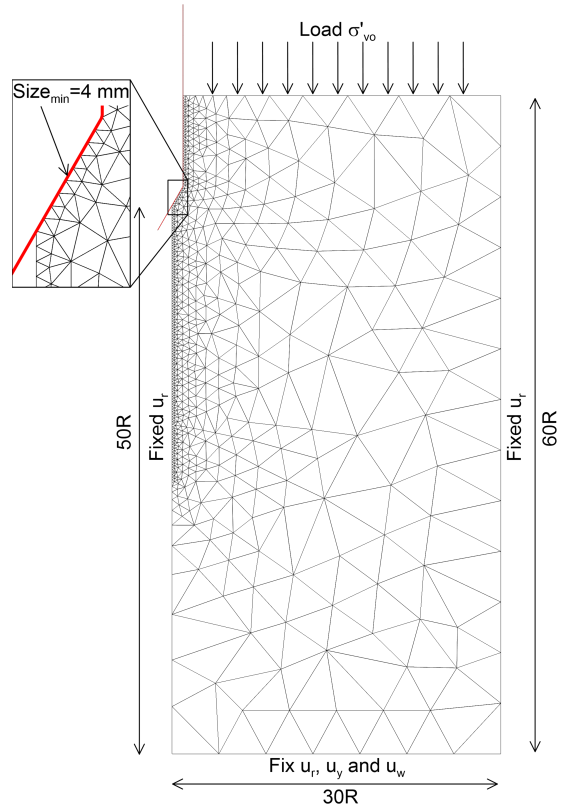
**FIG. 11. General framework to interpret variable penetration rate CPTus**



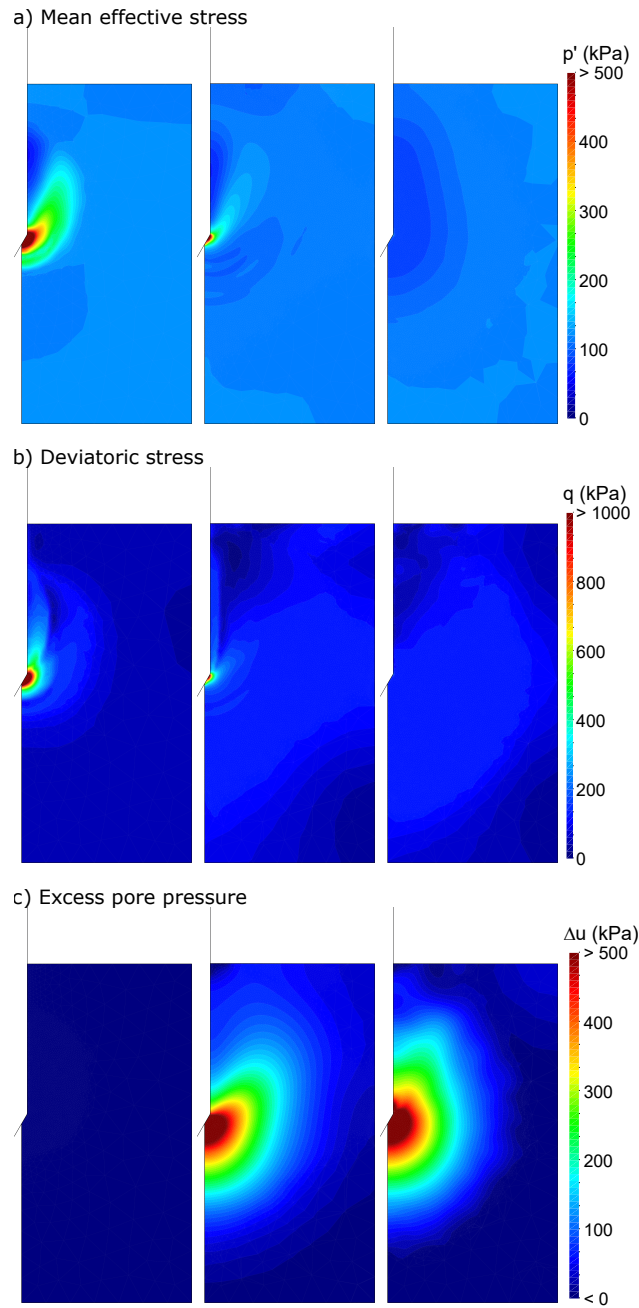
**FIG. 12. Clay and Sand Model (CASM) ingredients (a) features in the  $p'$ - $e$  space, (b) yield surface shape and variation. Additional details are discussed in the text and electronic supplement.**



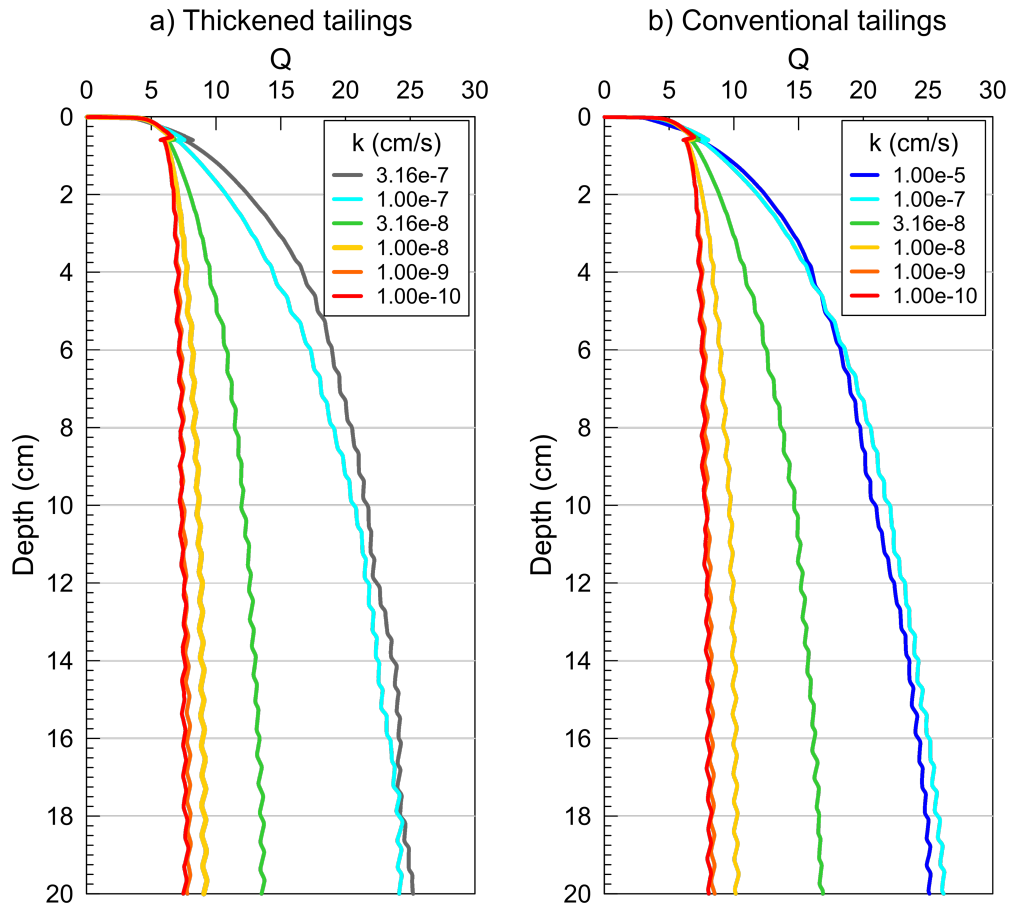
**FIG. 13. Comparisons of numerical responses obtained from CASM and experimental responses for (a) thickened tailings, (b) conventional tailings**



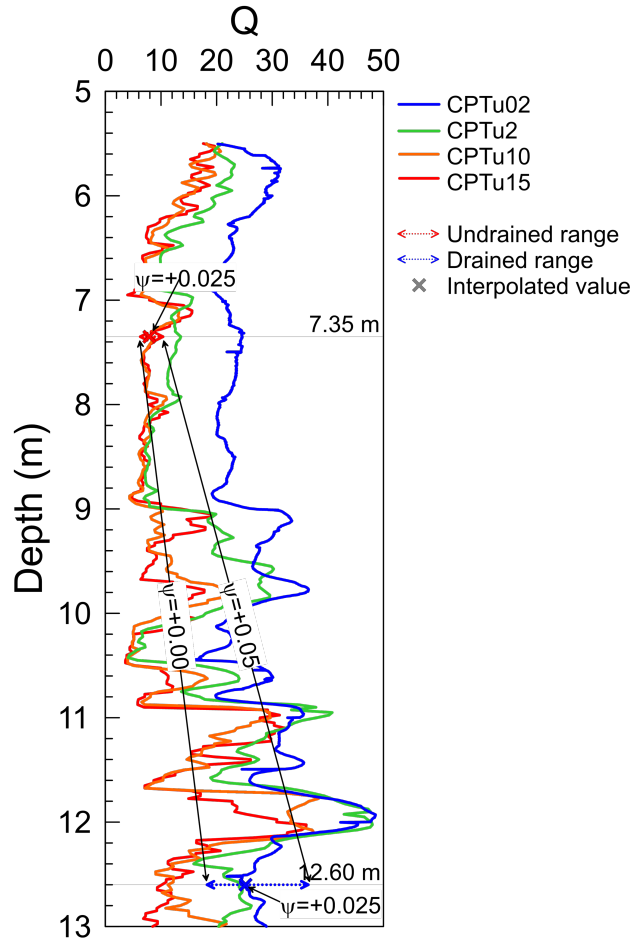
**FIG. 14. Mesh discretization and boundary conditions for the G-PFEM based CPTu penetration simulations**



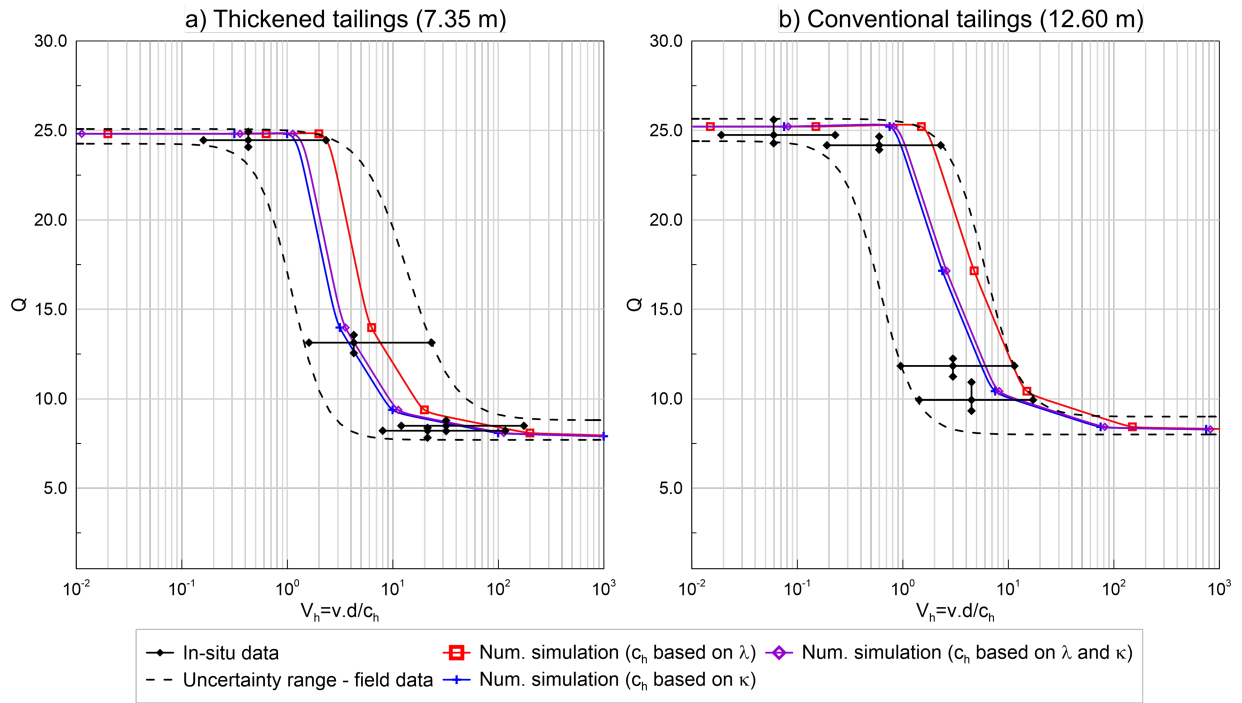
**FIG. 15. Distribution of (a)  $p'$ , (b)  $q$ , and (c) excess pore pressure,  $\Delta u$  (bottom) at the end of penetration. The left, middle, and right columns correspond to drained, partially drained, and undrained responses, respectively**



**FIG. 16.** Variation of  $Q$  versus depth obtained from PFEM-based CPTu penetration simulations for (a) thickened tailings and (b) conventional tailings considering different  $k$



**FIG. 17.** Illustration of the interpolation procedure to estimate  $\psi$ . The horizontal arrows at 7.35 m and 12.60 m represent the range of responses for  $\psi = 0.0 - 0.05$  used to inform the next iteration with  $\psi = 0.025$



**FIG. 18. Constraining of field-based backbone rate effect curves by using PFEM-based numerical simulations. Notice the narrower range obtained from numerical simulations. Results shown for (a) thickened tailings at 7.35 m and (b) conventional tailings at 12.60 m.**