

# Conceptual Framework for Multi-State Systems in Smart Factories using Reliability-Redundancy Allocation

Ahmad Attar

Industrial Engineering Faculty, IAU, South Tehran Branch, Tehran, Iran

\*Corresponding author: *st\_a\_attar@azad.ac.ir*

**Abstract**—In the era of Industry 4.0, smart factories integrate cyber-physical systems, IoT, and data analytics to enhance operational efficiency and resilience. Multi-state systems (MSS), where components exhibit multiple performance levels beyond binary failure states, are pivotal in modeling the dynamic reliability of these complex environments. This paper proposes a conceptual framework for reliability-redundancy allocation in MSS within smart factories, extending traditional models to incorporate non-exponential distributions, repairability, and real-time data-driven actions. Building on discrete event simulation and genetic algorithms, the framework addresses challenges like predictive maintenance and adaptive redundancy. Key elements include an updated characteristics triangle with a digital dimension, multi-objective optimization for availability and cost, and integration with digital twins. An illustrative example from a smart assembly line demonstrates the framework’s applicability. The study highlights opportunities for enhanced system resilience and identifies future research directions in AI-enhanced optimization.

**Index Terms**—Multi-State Systems; Smart Factories; Reliability-Redundancy Allocation; Industry 4.0; Discrete Event Simulation; Genetic Algorithm.

## I. INTRODUCTION

Smart factories, a cornerstone of Industry 4.0, represent interconnected ecosystems where machines, processes, and humans collaborate through advanced technologies like IoT, big data, and AI. [19] These systems demand high reliability to minimize downtime and ensure sustainable operations, especially amid dynamic uncertainties such as variable demands or cyber threats. [16] Traditional reliability models often assume binary states (functional or failed) and exponential distributions, which are inadequate for the multi-faceted degradation in smart manufacturing. [1] Multi-state systems (MSS) offer a more realistic approach, allowing components to operate at intermediate performance levels, reflecting gradual wear or partial failures. [7] Reliability-redundancy allocation optimizes both component reliability and redundancy to achieve desired system performance under constraints like cost and availability.

Attar et al. [9] has explored MSS with non-exponential distributions using simulation and metaheuristics, but integration with Industry 4.0 elements remains limited. [9] This paper introduces a conceptual framework that extends reliability-redundancy allocation for MSS in smart factories. It incorporates real-time data for dynamic distributions, predictive actions via IoT, and multi-objective optimization. The framework builds on the “characteristics triangle” (state, reparability, distribution) by adding a digital layer for sensor-driven insights. [18] The rest of the paper is organized as follows: Section II reviews literature, Section III presents the framework, Section IV provides an illustrative example, Section V discusses implications, and Section VI concludes.

## II. LITERATURE REVIEW

Reliability optimization in manufacturing has evolved from binary to multi-state models. Early studies focused on redundancy allocation for series-parallel systems with exponential assumptions. [11] Extensions to MSS incorporated multiple states and repairability, using universal generating functions (UGF) or simulation for availability estimation. [6], [8] For non-exponential distributions, discrete event simulation (DES) combined with genetic algorithms (GA) has been effective, addressing computational challenges through efficient estimation techniques. In Industry 4.0, reliability engineering faces new challenges like data abundance and system complexity. [16] Data-driven approaches leverage IoT for condition monitoring, enabling predictive maintenance and dynamic reliability models. [18] Frameworks for smart manufacturing emphasize cyber-physical integration, with digital twins simulating real-time states for optimization. [19] Maintenance optimization in this context uses metaheuristics and reinforcement learning to handle multi-state components and uncertainties. Recent works on MSS in manufacturing include quality-reliability dependencies and mission reliability modeling using extended networks. [8], [20] Redundancy optimization for multi-performance MSS considers reliability constraints and

supplier selection. [7], [10] However, a unified conceptual framework linking MSS reliability-redundancy allocation to smart factory dynamics is lacking, particularly with non-exponential, data-updated distributions. [1] This paper fills this gap by proposing an integrated framework.

### III. CONCEPTUAL FRAMEWORK

The proposed framework extends the reliability-redundancy allocation model for non-exponential MSS to smart factories. It comprises three core elements: an enhanced characteristics model, a simulation-optimization engine, and Industry 4.0 integration.

#### A. Enhanced Characteristics Triangle

The original "characteristics triangle" (See Figure III-C.) includes component state (binary/multi-state), reparability, and failure/repair distributions. [13] We add a fourth dimension: digital connectivity, encompassing IoT sensors for real-time data collection and AI for distribution updates (e.g., Weibull parameters refined via machine learning). [18] This allows dynamic actions, such as predictive repairs triggered by condition monitoring, extending technical/organizational actions to include automated interventions.

#### B. Multi-Objective Optimization Model

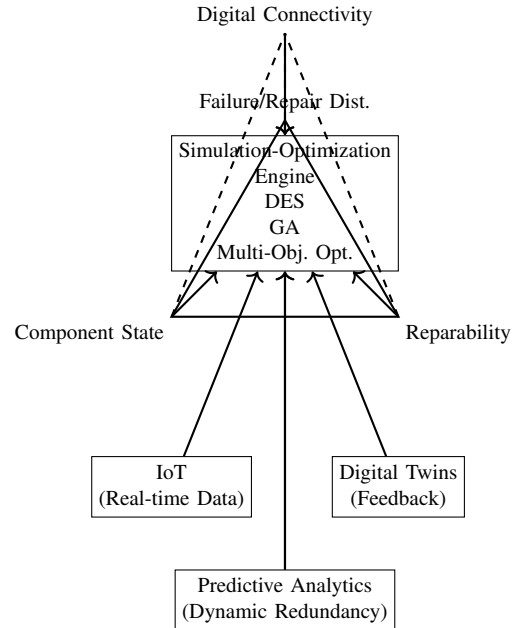
The model optimizes availability (A) and cost (C) for a series-parallel MSS: Maximize  $w_1 \cdot A(X) - w_2 \cdot C(X)$  s.t.  $A(X) \geq A_{min}$ ,  $C(X) \leq C_{max}$  Where X includes redundancy levels, component versions, and actions. Availability is estimated using achieved availability ([9]), converging to steady-state. [9] Non-exponential TTF/TTR are updated via sensor data. GA solves the model, with chromosomes representing X, evaluated through DES. [7] This approach builds on previous simulation-based optimization techniques for repairable MSS. [15]

#### C. Industry 4.0 Integration

IoT enables state/event/condition data for simulation inputs. [18] Digital twins mirror physical systems for what-if analyses, reducing simulation time. Predictive analytics adjust redundancy dynamically, e.g., adding virtual redundancies via cloud resources. [1] The framework uses middleware for data flow, ensuring compatibility in cyber-physical environments. [19] Fig. 1 shows the conceptual Framework overview with triangle, optimization loop, and I4.0 layers.

### IV. ILLUSTRATIVE EXAMPLE

Consider a smart assembly line with two subsystems: robotic arms (subsystem 1, 3 states) and conveyors (subsystem 2, 2 states). Components follow Weibull distributions, updated via IoT sensors. Demand: 1000



Conceptual Framework for Multi-State Systems in Smart Factories

units/hour. Using the framework, GA optimizes redundancy and actions (e.g., sensor-based maintenance). Simulation in Enterprise Dynamics yields  $A = 0.96$ ,  $C = 550$ , improving on static models by 5 via dynamic updates. [7] Table 1 shows optimal design.

TABLE I  
OPTIMAL DESIGN

Subsystem	Version	Redundancy	Actions
1	2	4	IoT monitoring, predictive repair Cloud redundancy
2	3	3	

### V. DISCUSSION

The framework enhances resilience in smart factories by enabling adaptive allocation, reducing downtime through predictive insights. [?] Challenges include data privacy and computational scalability; opportunities lie in AI integration for real-time GA. [16] Compared to traditional models, it better handles I4.0 complexities like multi-performance metrics. [7] Dynamic demand adjustments, as studied in related inventory optimization, [5] could further enhance scalability. Implications for managers: Invest in IoT for data-driven reliability.

### VI. CONCLUSION

This conceptual framework advances MSS reliability-redundancy allocation for smart factories, bridging traditional engineering with I4.0 technologies. Future work could empirically validate with real datasets or extend to cyber-security redundancies. [1]

## REFERENCES

- [1] Tordeux, A., et al. (2019). Emerging Challenges for Dependability Analysis in Industry 4.0. *STU Mechanical Engineering*, 21(5), 206-211.
- [2] Friederich, J., et al. (2021). Requirements for Data-driven Reliability Modeling and Simulation of Smart Manufacturing Systems. *Proceedings of the 2021 Winter Simulation Conference*. DOI: 10.1109/WSC52266.2021.9715410.
- [3] Cachada, A., et al. (2021). Predictive Maintenance in Industry 4.0: Current Themes. *Procedia Computer Science*, 180, 1153-1162.
- [4] Wang, Z., et al. (2016). Redundancy Allocation for Multistate Systems With Component Dependencies and Load Sharing. *Journal of Mechanical Design*, 138(11), 111403.
- [5] Attar, A., Raissi, S., & Khalili-Damghani, K. (2016). Simulation–optimization approach for a continuous-review, base-stock inventory model with general compound demands, random lead times, and lost sales. *Simulation*, 92(6), 547-564.
- [6] Tian, Z., Levitin, G., & Zuo, M. J. (2009). A joint reliability–redundancy optimization approach for multi-state series–parallel systems. *Reliability Engineering & System Safety*, 94(10), 1568-1576.
- [7] Ding, Y., et al. (2021). Redundancy Optimization for Multi-Performance Multi-State Series-Parallel Systems. *Reliability Engineering & System Safety*. DOI: 10.1016/j.res.2021.107873.
- [8] Lisnianski, A., et al. (2020). *Modern Dynamic Reliability Analysis for Multi-state Systems*. Springer.
- [9] Attar, A., et al. (2015). Multi-Objective Reliability-Redundancy Allocation for Non-Exponential Multi-State Repairable Components. *IIEC2015*.
- [10] Guilani, P. P., et al. (2020). Redundancy allocation problem with multi-state component systems. *Reliability Engineering & System Safety*, 193, 106629.
- [11] Tian, Z., et al. (2008). Reliability-Redundancy Allocation for Multi-State Series-Parallel Systems. *IEEE Transactions on Reliability*, 57(2), 303-310.
- [12] Su, C., & Li, Y. (2019). Dynamic reliability analysis of a multi-state manufacturing system. *Eksplotacja i Niezawodność – Maintenance and Reliability*, 21(3), 451-462.
- [13] Tian, Z., et al. (2009). A joint reliability–redundancy optimization approach for multi-state series–parallel systems. *Reliability Engineering & System Safety*, 94(10), 1568-1576.
- [14] Cachada, A., et al. (2021). Predictive Maintenance in Industry 4.0: Current Themes. *Procedia Computer Science*, 180, 1153-1162.
- [15] Attar, A., Raissi, S., & Khalili-Damghani, K. (2017). A simulation-based optimization approach for free distributed repairable multi-state availability-redundancy allocation problems. *Reliability Engineering & System Safety*, 157, 177-191.
- [16] Farsi, M. A., & Zio, E. (2019). Industry 4.0: Some Challenges and Opportunities for Reliability Engineering. *International Journal of Reliability, Risk and Safety: Theory and Application*. DOI: 10.30699/ijrrs.2.1.4.
- [17] Tordeux, A., et al. (2019). Emerging Challenges for Dependability Analysis in Industry 4.0. *STU Mechanical Engineering*, 21(5), 206-211.
- [18] Friederich, J., et al. (2021). Requirements for Data-driven Reliability Modeling and Simulation of Smart Manufacturing Systems. *Proceedings of the 2021 Winter Simulation Conference*. DOI: 10.1109/WSC52266.2021.9715410.
- [19] Zheng, P., et al. (2018). Smart manufacturing systems for Industry 4.0: Conceptual framework, scenarios, and future perspectives. *Frontiers of Mechanical Engineering*.
- [20] Zhang, A., et al. (2020). Modeling Product Manufacturing Reliability with Quality Variations. *Sensors*, 20(19), 5677. DOI: 10.3390/s20195677.