

## **Influence of salinity on the behaviour of frozen soils**

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## **Abstract**

Salinity strongly affects the freezing and mechanical behaviour of soils, but systematic studies combining thermodynamic interpretation with strength testing are limited. This study examines the influence of NaCl on the freezing process and unconfined compressive strength of saturated sands. Freezing curves were recorded at  $-10\text{ }^{\circ}\text{C}$  and  $-25\text{ }^{\circ}\text{C}$ , and unfrozen water content was measured using nuclear magnetic resonance (NMR). Results show that increasing salinity lowers both the supercooling temperature and the equilibrium freezing point in accordance with the NaCl–H<sub>2</sub>O phase diagram. At  $-25\text{ }^{\circ}\text{C}$ , a second plateau in the freezing curves was observed, reflecting eutectic solidification of residual brine. Even small salt additions caused disproportionate strength reductions: at  $-10\text{ }^{\circ}\text{C}$ , 0.5% NaCl reduced strength to about one-quarter of the salt-free value. At eutectic conditions, strength partially recovered as brine solidified, though the ice–soil skeleton incorporated salt crystals, producing a response distinct from fresh water soils. NMR tests confirmed a near-linear increase of unfrozen water with salinity, while the strength–liquid relation was strongly nonlinear. The novelty of this work lies in combining freezing curve analysis with direct strength testing of saline sands.

## **Keywords chosen from ICE Publishing list**

Ground freezing; temperature effects; thermal behaviour; testing & evaluation; Strength & testing of materials; Sands; NMR relaxometry; Cold/Arctic region geotechnics; Coastal engineering

## 1 **1 Introduction**

2 The presence of dissolved salts profoundly modifies the freezing behaviour of soils. Salts not  
3 only depress the equilibrium freezing point (Atkins, 1996; Haghghi et al., 2008) through  
4 colligative and osmotic effects but also alter the soil freezing characteristic curve (SFCC),  
5 increase the fraction of unfrozen water retained at subzero temperatures, and influence ice  
6 segregation, salt migration, and cryo-concentration during freezing (Banin & Anderson, 1974;  
7 Zhou et al., 2018; Amankwah et al., 2021; Luo et al., 2023). Understanding soil freezing  
8 under saline conditions is essential for two major contexts:

- 9 1. Artificial ground freezing (AGF), widely used for temporary ground support in urban  
10 tunnelling, shaft sinking, and cross-passage construction. Here, groundwater salinity  
11 can significantly delay or complicate soil freezing. For example, during the  
12 construction of cross-passages of the Port Said tunnels beneath the Suez Canal,  
13 groundwater salinities of ~3.8% NaCl required substantially lower refrigeration  
14 temperatures than anticipated (Orth et al., 2021; Rizos et al., 2022).
- 15 2. Permafrost regions, where naturally saline soils or anthropogenic inputs (e.g., drilling  
16 muds, industrial brines, landfill leachates) modify thawing and refreezing behaviour,  
17 with implications for climate-driven permafrost degradation (Wan et al., 2015; Ying et  
18 al., 2025).

19 While it is well known that salts reduce the freezing point of pore water, the consequences  
20 for the mechanical strength of frozen soils remain less systematically investigated. The soil's  
21 load-bearing capacity depends largely on the volume and microstructure of the ice phase. At  
22 subzero temperatures above the eutectic point of a salt solution, a significant proportion of  
23 pore brine remains unfrozen, which weakens the ice–soil matrix (Arenson & Segoy, 2004;  
24 Tilston et al., 2010). Conversely, once the eutectic temperature is crossed, the residual brine  
25 solidifies in a second freezing stage, resulting in a distinct strengthening mechanism  
26 (Journaux et al., 2023; Gao et al., 2024).

27 A further complication is that different salts produce markedly different freezing point  
28 depressions and precipitation behaviours. For instance, NaCl brine has a eutectic  
29 temperature of  $-21.15\text{ }^{\circ}\text{C}$ , whereas divalent salts have lower temperatures (Loomis, 1896;  
30 Wan et al., 2021). Moreover, salt precipitation during freezing may introduce discontinuities  
31 or temperature jumps that influence the unfrozen water content and hence mechanical  
32 response (Ying et al., 2025).

33 Despite extensive thermodynamic studies of saline freezing processes, relatively few  
34 experimental investigations directly link salinity, freezing curves, and soil strength in a  
35 controlled laboratory setting. This gap is particularly relevant for coarse-grained soils where  
36 pore-size effects are minimized, allowing clearer isolation of salinity-driven phenomena (Xiao  
37 et al., 2018). The present study addresses this gap by systematically testing narrow-graded  
38 sand specimens saturated with NaCl solutions of varying concentrations. Freezing curves  
39 were recorded, and unconfined compression tests were performed at two subzero  
40 temperatures ( $-10\text{ }^{\circ}\text{C}$  and  $-25\text{ }^{\circ}\text{C}$ ) to evaluate how salinity affects both the freezing process  
41 and the mechanical strength of frozen soil.

42 Additionally, while earlier works have described freezing point depression and unfrozen  
43 water retention in saline soils, few studies combine phase diagram-based interpretation with  
44 direct mechanical testing on frozen saline sands. The results provide new insights into how  
45 even small salt contents dramatically reduce strength at moderate subzero temperatures,  
46 while complete freezing at eutectic conditions alters the ice-soil matrix in a fundamentally  
47 different way. These findings have direct implications for the design and safety assessment  
48 of saline ground freezing projects and for predicting the mechanical response of saline  
49 permafrost.

50

## 51 **2 Literature review**

52 Salts influence the freezing of soils primarily by altering the thermodynamic properties of  
53 pore water and secondarily by modifying the microstructural arrangement of ice and brine.

54 These effects can be described using classical phase diagrams, complemented by pore-  
55 scale observations and constitutive modelling.

56

## 57 **2.1 Freezing point depression and water activity**

58 When a salt crystal such as NaCl dissolves in water, hydration shells form around the ions.  
59 These hydration complexes disrupt the hydrogen-bond network of liquid water, lowering the  
60 chemical potential of the system and thereby decreasing the freezing temperature (Atkins,  
61 1996). The reduction in free energy is also expressed as a decrease in water activity, which  
62 is nearly linear with increasing NaCl concentration (Banin & Anderson, 1974; Haghghi et al.,  
63 2008). Wan et al. (2021) further showed that for Na<sub>2</sub>SO<sub>4</sub>, the relationship is nonlinear: water  
64 activity decreases at low concentrations, but above ~0.4 mol/L it remains nearly constant  
65 despite higher concentrations.

66 As already shown, the extent of freezing point depression depends strongly on the type of  
67 salt. Loomis (1896) classified electrolytes into two groups: monovalent salts such as NaCl  
68 and KCl, which produce relatively moderate freezing point depression, and divalent salts  
69 such as MgCl<sub>2</sub> or Na<sub>2</sub>SO<sub>4</sub>, which can cause much stronger depressions. For example, a  
70 20% NaCl solution freezes at about -17 °C, while a 20% MgCl<sub>2</sub> solution can depress  
71 freezing to nearly -30 °C. This strong ion-specific effect is consistent with more recent  
72 experimental results (Wan et al., 2015; Wan et al., 2021).

73

## 74 **2.2 Eutectic mixtures and two-stage freezing**

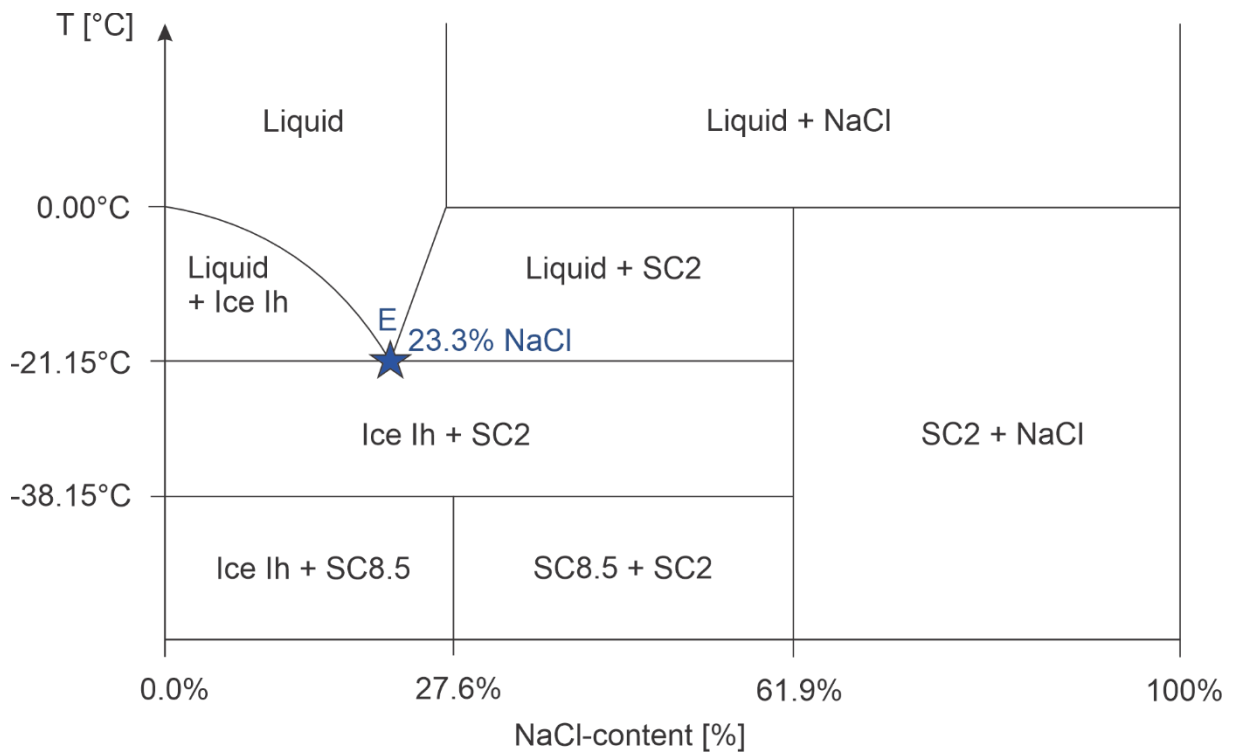
75 The freezing process of saline water is best understood using phase diagrams. Figure 1  
76 illustrates the NaCl-H<sub>2</sub>O phase diagram. The eutectic composition is reached at 23.3% NaCl  
77 and 76.7% H<sub>2</sub>O, at which the entire solution freezes at -21.15 °C. This is the lowest possible  
78 freezing point for the NaCl-H<sub>2</sub>O system.

79 Above the eutectic temperature, freezing occurs in two stages. Initially, relatively pure water  
80 freezes, forming ice crystals and leaving behind a more saline brine. As cooling continues,  
81 the brine becomes increasingly concentrated, and its freezing temperature decreases further.

82 Eventually, when the eutectic concentration and temperature are reached, the brine itself  
83 solidifies into a mixture of ice and salt crystals (Atkins, 1996; Banin & Anderson, 1974). If the  
84 initial solution is already saturated, solid NaCl crystals are expelled during cooling until the  
85 eutectic mixture is reached. At the eutectic temperature, simultaneous crystallization of ice  
86 and brine occurs. This two-stage freezing explains the persistence of liquid brine at moderate  
87 subzero temperatures (e.g.,  $-10\text{ }^{\circ}\text{C}$ ) and its eventual disappearance once the eutectic point  
88 is crossed (Ying et al., 2025).

89 During this procedure various kinds of crystal structures will form. We will concentrate here  
90 on the left hand side of the diagram where the salt is fully dissolved in a solution (i.e., for salt  
91 concentrations lower than 27.6%, beyond which the solution is regardless of the temperature  
92 supersaturated and salt crystals precipitate). The common form of pure water ice is a  
93 hexagonal crystal structure in which water molecules are arranged tetrahedrally in hydrogen  
94 bonds – called Ice Ih in Figure 1. Depending on temperature and pressure also the sodium  
95 chloride hydrate crystals build up differently. At a pressure of 1 bar there are two species of  
96 NaCl hydrates that are relevant in the context of this research. Sodium chloride dihydrate  
97  $\text{NaCl}\cdot 2\text{H}_2\text{O}$  (SC2) forms at locations where the temperature is lowered from  $0\text{ }^{\circ}\text{C}$  to the  
98 eutectic temperature of  $-21.15\text{ }^{\circ}\text{C}$  and the NaCl content lies above 23.3 %. Brine crystallises  
99 as disodium chloride decaheptahydrate  $2\text{NaCl}\cdot 17\text{H}_2\text{O}$  (SC8.5) at temperatures below -  
100  $38.15\text{ }^{\circ}\text{C}$  for these salt concentrations. Different pores will have different salt concentrations  
101 due to salt migration through diffusion and hence, depending on the NaCl concentration  
102 there will be pure Water ice (Ice Ih) co-existing with SC8.5, or SC8.5 with SC2 (Journaux et  
103 al., 2023). This affects thermodynamic aspects as well as the mechanical properties of the  
104 soil.

105



106

107 **Fig. 1.** H<sub>2</sub>O-NaCl phase diagram at 1 bar. The blue star shows the eutectic point (E) (after Journaux et  
 108 al., 2023)

109

### 110 2.3 Pore-scale processes and microstructure

111 In saline soils, the freezing behaviour is further complicated by pore-scale processes. As  
 112 water freezes, ice initially forms in larger pores, while capillary and adsorptive forces delay  
 113 freezing in finer pores due to a lowering of the so-called ice entry point (Andersland &  
 114 Ladanyi, 2004). In saline soils, this size-dependent freezing is combined with solute  
 115 redistribution. For example, Na<sub>2</sub>SO<sub>4</sub> solutions may crystallize within pores, partially blocking  
 116 them and altering the effective pore size distribution (Wan et al., 2015). This mechanism  
 117 further decreases the freezing point due to enhanced adhesive forces in narrower pores.  
 118 Arenson & Segó (2004) visualized freezing in coarse sands with fluorescent tracers. Their  
 119 microstructural observations revealed that increasing salinity increases the amount of  
 120 unfrozen pore liquid and promotes the formation of interconnected brine channels. These  
 121 concentrated brine pathways, in turn, influence ice crystal morphology: instead of forming  
 122 continuous ice, saline freezing often produces fragile “ice needles” emanating from mineral  
 123 grains, which significantly reduces the mechanical stability of the frozen soil.

124 More recent studies using micro-CT imaging have confirmed that saline sands can retain  
125 continuous liquid bodies up to the eutectic temperature (Gao et al., 2024). The cooling rate  
126 also plays a critical role: rapid freezing traps brine in continuous networks, maintaining higher  
127 permeability, while slow freezing promotes brine segregation into disconnected pockets  
128 (Wang et al., 2023). This duality is particularly relevant for engineering applications such as  
129 artificial ground freezing, where the rate of freezing is controlled by the applied thermal  
130 gradient.

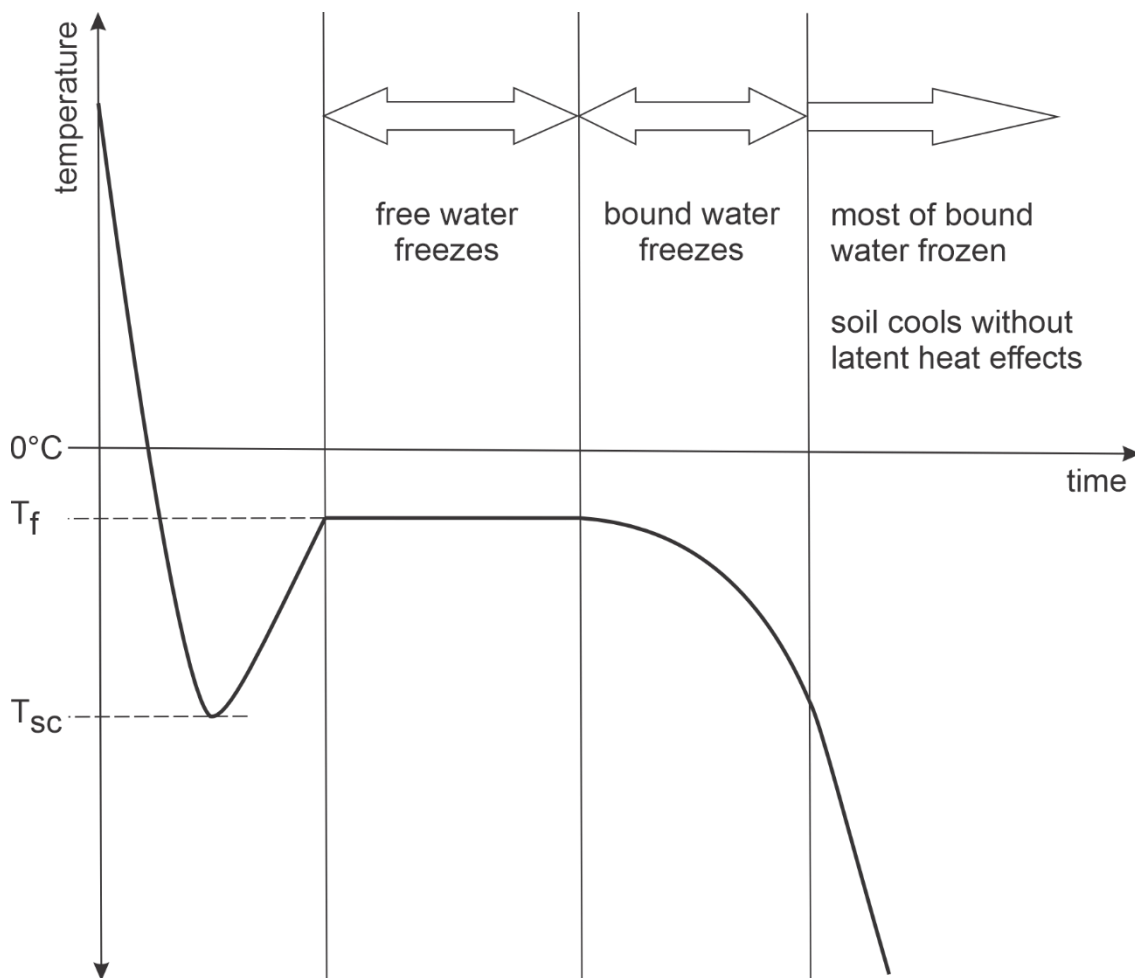
131

## 132 **2.4 Thermal and mechanical implications**

133 The influence of salts extends beyond freezing temperature. Salinity also affects thermal  
134 properties and, ultimately, soil strength. Laboratory tests show that chloride salts reduce  
135 thermal conductivity by  $\sim 0.11 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ , whereas sulfate salts reduce it by  $\sim 0.07 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$   
136 (Ju et al., 2023).

137 The unfrozen water content (UWC) plays a central role in strength development: higher  
138 salinity results in more unfrozen water at a given temperature, leading to weaker ice–soil  
139 bonding (Watanabe & Mizoguchi, 2002; Tilston et al., 2010). Conversely, once the eutectic  
140 temperature is reached and residual brine solidifies, the ice–soil matrix regains continuity,  
141 though salt crystals are incorporated into the structure. This transition results in a different  
142 form of mechanical stabilization that is not observed in fresh water soils (Amankwah et al.,  
143 2021; Luo et al., 2023).

144 The sequence of freezing in soils can also be represented by a cooling curve. Figure 2  
145 illustrates this process: after an initial supercooling ( $T_{sc}$ ), ice nucleation releases latent heat,  
146 stabilizing the temperature at the freezing point ( $T_f$ ). Larger pores freeze first, followed by  
147 smaller pores as temperature decreases further. Adhesive forces in the finest pores may  
148 prevent complete freezing, leaving residual unfrozen water. In saline soils, this residual  
149 fraction is significantly larger due to solute-induced freezing point depression, explaining why  
150 brine can persist at temperatures as low as  $-10 \text{ }^\circ\text{C}$  (Andersland & Ladanyi, 2004; Wan et al.,  
151 2015; Luo et al., 2023).



153

154 **Fig. 2.** Cooling curve for soil water and ice (after Andersland & Ladanyi, 2004)

155

156 **2.5 Constitutive modelling of saline soil freezing**

157 The generalized Clapeyron equation (GCE) provides the thermodynamic foundation for  
 158 describing soil freezing, linking water potential, temperature, and ice–water equilibrium. In its  
 159 traditional form, the GCE includes only matric potential. For saline soils, however, osmotic  
 160 potential must be added to capture freezing point depression and UWC behaviour (Luo et al.,  
 161 2023; Wan et al., 2024). Yet even this modification may underpredict freezing depression at  
 162 higher salinities, where salt exclusion and precipitation must also be accounted for  
 163 (Amankwah et al., 2021). Recent models explicitly incorporating these mechanisms provide  
 164 significantly better fits to both laboratory and field SFCC data.

165

## 166 **3 Methodology**

### 167 **3.1 Material and sample preparation**

168 Narrowly graded sand with particle sizes between 0.5 mm and 1.0 mm was selected for the  
169 experiments. The use of coarse-grained material avoids pore-size freezing effects that  
170 typically occur when pore diameters are smaller than 1  $\mu\text{m}$  (Watanabe & Mizoguchi, 2002;  
171 Xiao et al., 2018). For this reason, the observed freezing point depression in the present  
172 study can be attributed primarily to salinity rather than pore geometry.

173 Sodium chloride (NaCl) was chosen as the solute. Unlike salts such as  $\text{Na}_2\text{SO}_4$ , which may  
174 precipitate and alter pore structures, NaCl remains dissolved until the eutectic point is  
175 reached, making it suitable for isolating the thermodynamic effects of salinity (Wan et al.,  
176 2015).

177 Cylindrical specimens with a diameter of 50 mm and a height of 100 mm were prepared for  
178 freezing curve measurements and unconfined compression testing. This 1:2 height-to-  
179 diameter ratio follows established practice for frozen soil testing (Andersland & Ladanyi,  
180 2004). Specimens were cast in cylindrical polyurethane (PU) moulds with a base containing  
181 a lead-through for insertion of a temperature sensor.

182 To ensure full saturation, specimens were prepared under saline water. The required amount  
183 of NaCl solution was first poured into the mould, and the sand was then placed in four layers,  
184 each lightly compacted. This underwater preparation minimized entrapped air, yielding  
185 degrees of saturation  $S_r$  between 0.95 and 1.0. Homogeneity of the method was verified by  
186 cutting frozen specimens into horizontal layers and determining density and water content by  
187 oven drying.

188 The NaCl solution concentrations ranged from 0.0% (distilled water) to 10.0% by mass. For  
189 example, a solution of 3.5% NaCl corresponds to 35 g NaCl per 1000 g of solution. After  
190 preparation, specimens were frozen for 24 h in the freezing laboratory chamber.

191 To account for the ~8% volumetric expansion of water upon freezing, moulds were left open  
192 at the top, allowing excess pore water to escape. This prevented cracking or specimen

193 distortion. After freezing, any excess ice lens formed at the specimen top was carefully  
194 removed to achieve uniform dimensions of 100 mm in height.

195

### 196 **3.2 Experimental setup and execution**

197 Experiments were performed in the controlled freezing laboratory at GUT, where ambient  
198 temperatures between  $-4\text{ }^{\circ}\text{C}$  and  $-30\text{ }^{\circ}\text{C}$  can be maintained with  $\pm 0.5\text{ }^{\circ}\text{C}$  accuracy.

199 Specimens remained inside the laboratory throughout preparation, freezing, and testing,  
200 ensuring no thermal disturbance.

201 Temperature control and gradients were carefully monitored. For freezing-curve specimens,  
202 a PT100 probe was placed at mid-height. Temperature was logged at 1-second intervals  
203 during freezing. In unconfined compression specimens, additional probes were installed at  
204 the top and base, enabling assessment of axial gradients. Before testing, specimens were  
205 considered at steady state when the temperature difference between top, middle, and base  
206 did not exceed  $0.3\text{ }^{\circ}\text{C}$  for at least one hour. All PT100 sensors were factory-calibrated ( $\pm 0.1$   
207  $^{\circ}\text{C}$  accuracy) and cross-checked in an ice–water bath prior to the test series. Typical  
208 gradients at failure were  $< 0.5\text{ }^{\circ}\text{C}$  across the 100 mm specimen height.

209 Unconfined compression tests were performed at constant strain rate on specimens frozen  
210 for at least 24 h. This ensured that all specimens had completed their primary freezing  
211 process (see freezing curves, Section 4). The strain rate was  $0.1\%/min$ , consistent with the  
212 recommendations of Andersland & Ladanyi (2004) for frozen soils at moderately low  
213 temperatures. A lower rate was chosen (rather than  $1.0\%/min$ ) to account for the expected  
214 presence of unfrozen brine at  $-10\text{ }^{\circ}\text{C}$ , which could otherwise bias failure modes. Tests were  
215 terminated at 20% axial strain.

216 Axial deformation was measured with linear variable displacement transducers (LVDTs),  
217 while load was recorded with a 2-ton load cell. For the reference samples (0% NaCl), a 10-  
218 ton load cell was used due to their higher strength. The LVDTs have an accuracy of  $< \pm 0.05$   
219 mm, both load cells have an accuracy of  $< \pm 0.5\%$  of nominal load. Temperatures at the  
220 specimen base, top, and core were recorded continuously during loading.

221

## 222 **4 Experimental results**

### 223 **4.1 Soil freezing curves**

#### 224 **4.1.1 Soil freezing curves at -10 °C**

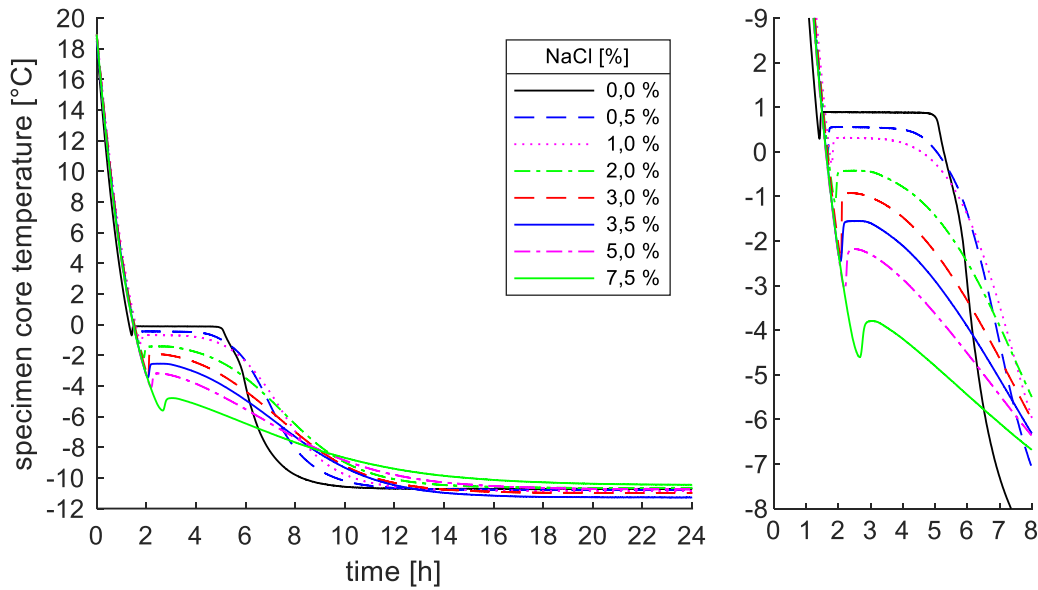
225 At an ambient temperature of  $-10\text{ °C}$ , which is above the eutectic temperature of NaCl ( $-$   
226  $21.15\text{ °C}$ ), freezing occurs in the two-stage manner described earlier. Figure 3 presents the  
227 freezing curves of specimens with different NaCl concentrations.

228 For the reference sample with 0.0% NaCl, the classic freezing curve shape is observed: after  
229 supercooling to  $-0.7\text{ °C}$  ( $T_{SC}$ ), crystallization initiates, releasing latent heat and stabilizing the  
230 temperature at the freezing point  $T_f = -0.1\text{ °C}$  for approximately 3.5 hours. Once this plateau  
231 ends, the temperature gradually decreases to  $-3.0\text{ °C}$  over one hour, most likely reflecting  
232 the freezing of bound water. Subsequently, the specimen cools rapidly to the ambient  
233 temperature.

234 With increasing NaCl content, three systematic effects are evident:

- 235 1. Both the supercooling temperature ( $T_{SC}$ ) and freezing temperature ( $T_f$ ) decrease.
- 236 2. The duration of the steady freezing plateau shortens, implying that less ice forms and  
237 a larger fraction of brine remains unfrozen.
- 238 3. The cooling rate slows, such that specimens with higher salinity require longer to  
239 reach the ambient temperature. This is attributed to ongoing separation of pure water  
240 from the brine during cooling, which then freezes and releases latent heat (Banin &  
241 Anderson, 1974; Wan et al., 2015).

242



243

244 **Fig. 3.** Freezing curves of specimen with varying NaCl-contents at -10 °C with detail (right)

245

#### 246 4.1.2 Soil freezing curves at -25 °C

247 When ambient temperature is lowered to -25 °C, below the eutectic point of NaCl, complete  
 248 freezing of all specimens is achieved. Figure 4 shows the cooling curves at -25 °C.

249 Initially, cooling occurs more rapidly than at -10 °C due to the larger temperature gradient.

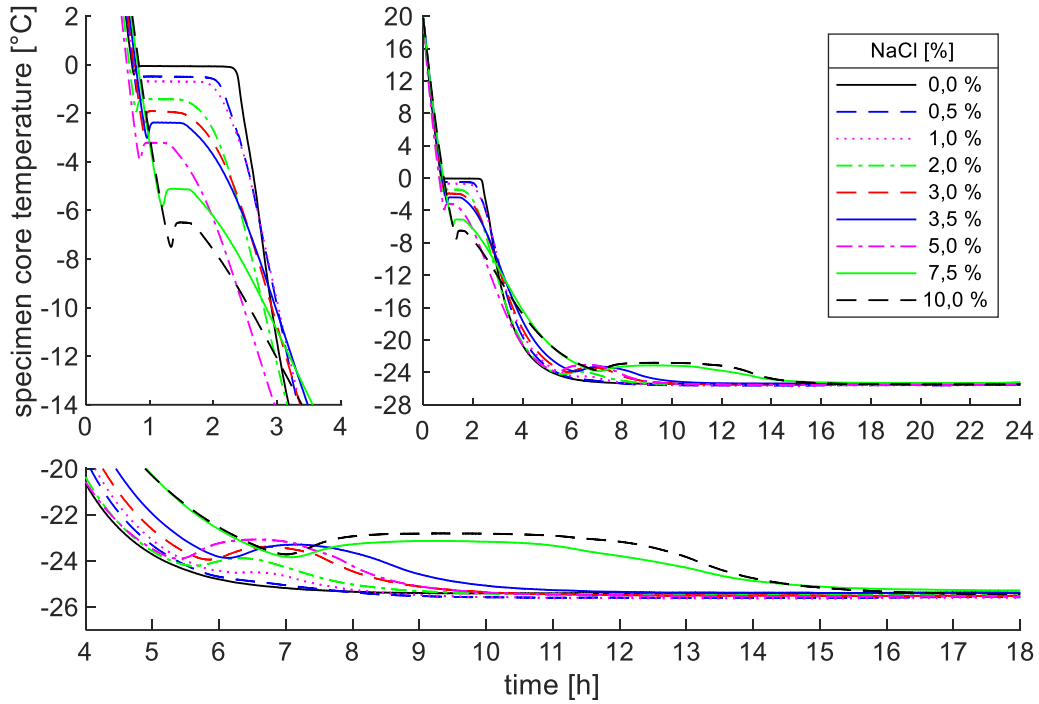
250 As a result, the supercooling ( $T_{sc}$ ) and freezing ( $T_f$ ) stages occur earlier in time. However,  
 251 differences in  $T_f$  values are observed: at -25 °C, the higher cooling rate gives less time for  
 252 brine segregation, so less pure ice forms and less latent heat is released, lowering the  
 253 effective freezing temperature (Gao et al., 2024; Wang et al., 2023).

254 The duration of the first freezing plateau is shorter than at -10 °C, reflecting faster kinetics  
 255 and reduced ice formation. After this stage, specimen core temperatures decline towards -23  
 256 to -24 °C. At this point, samples with NaCl content show a second temperature plateau,  
 257 indicating a second freezing phase. This phase corresponds to the crystallization of the  
 258 remaining eutectic brine, consistent with the NaCl-H<sub>2</sub>O phase diagram (Figure 1).

259 The duration of this second plateau increases disproportionately for salinities above 5%. For  
 260 example, specimens with 7.5% and 10% NaCl require much longer to complete eutectic  
 261 freezing, though the incremental difference between them is small. This behaviour confirms

262 that once a threshold salinity is reached, freezing of the residual brine becomes a slower  
 263 process governed by salt precipitation kinetics (Ying et al., 2025).

264



265

266 **Fig. 4.** Freezing curves of specimen with varying NaCl-contents at -25 °C with details (left and below)

267

### 268 4.1.3 Simple 1D verification.

269 A simple one-dimensional heat-transfer estimate confirms that the observed plateau  
 270 durations are physically consistent and provides a simple means for prediction. The  
 271 specimens ( $\varnothing$  50 mm  $\times$  100 mm) had a volume of  $1.96 \times 10^{-4}$  m<sup>3</sup> and a surface area of  
 272  $1.96 \times 10^{-2}$  m<sup>2</sup>, giving a characteristic length of  $\sim$ 0.01 m. The associated sensible-cooling  
 273 time constant is 0.9–1.8 h, consistent with the non-plateau portions of the curves.

274 Plateau durations are then governed by latent heat release:

275

276

$$t_L = \frac{m_w L \Delta\theta_i(T, S)}{hA \Delta T_{\text{eff}}}$$

277

278 where  $m_w$  is the specimen water mass,  $L$  the latent heat of fusion, and  $\Delta\theta_i(T, S)$  the ice  
 279 fraction formed at temperature  $T$  and salinity  $S$ . The ice fraction was taken from the NMR-  
 280 measured liquid water contents. At  $-10$  °C, liquid fractions increased nearly linearly with  
 281 salinity, from  $\sim 0.05$  (0% NaCl) to  $\sim 0.80$  (10% NaCl). Using  $m_w = 0.069$  kg,  $L = 333.7$  kJ kg $^{-1}$ ,  
 282  $A = 0.0196$  m $^2$ ,  $\Delta T_{\text{eff}} \approx 10$  K and two different convective coefficients: one for no salt,  
 283  $h_{\text{Sand,Water}} = 9.0$  W m $^{-2}$  K $^{-1}$ , and one for the salty soils of  $h_{\text{Sand,Brine}} = 35.0$  W m $^{-2}$  K $^{-1}$ , the  
 284 predicted plateau durations agree well with the freezing curves (Table 1). These convective  
 285 coefficients are back-calculated and represent two effective overall surface coefficients.  
 286 However, the fact that a single coefficient provides a good estimate for all salty cases  
 287 supports this lumped approach as a rough estimate. Additionally, with a thermal conductivity  
 288 of frozen sand  $k \approx 1.7$  W m $^{-1}$  K $^{-1}$  and the convective coefficients (Incropera et al., 2007), the  
 289 Biot number is  $\ll 0.1$  for the lower coefficient justifying a lumped-capacity approach, although  
 290 it is only marginal for the brine.

291

292 **Table 1.** Predicted vs. observed plateau durations at  $-10$  °C

NaCl content [% by mass]	Liquid pore water due NMR [% by vol]	Predicted plateau duration [h]	Observed plateau duration [h]
0.0	0.91	3.59	$\sim 3.5$
2.0	13.06	0.81	$\sim 0.8$
3.5	24.87	0.70	$\sim 0.7$
7.5	58.11	0.39	$\sim 0.4$
10.0	78.29	0.20	$\sim 0.2$

293

294 At  $-25$  °C, the first freezing stage is accelerated by the larger temperature gradient, but a  
 295 second plateau appears near  $-21$  °C due to eutectic freezing of residual brine. This can be  
 296 described by the same expression, with  $\Delta\theta_i$  representing the remaining brine fraction and  
 297  $\Delta T_{\text{eff}}$  reduced to  $3-5$  °C. The disproportionate lengthening of this second plateau at salinities

298 above 5% is thus explained by the greater brine volume and the smaller driving temperature  
299 difference at the eutectic.

300

## 301 **4.2 Unconfined compression tests**

### 302 **4.2.1 Unconfined compression tests at -10 °C ambient temperature**

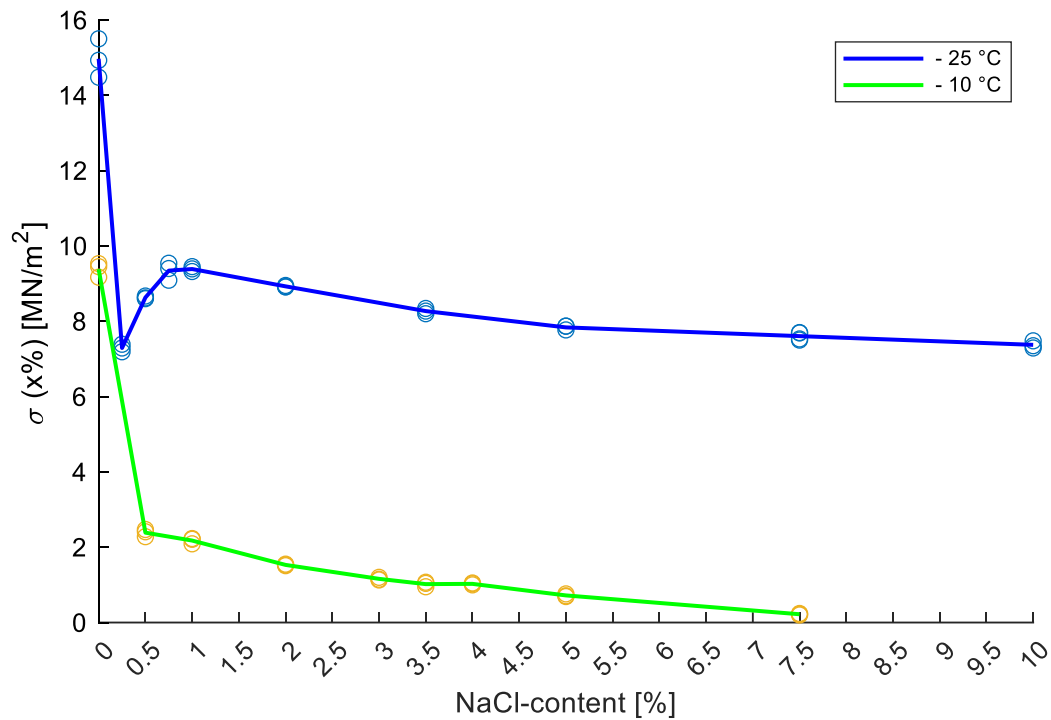
303 After freezing for 24 h, all specimens had completed their freezing process (Figure 3 and 4).

304 Unconfined compression tests were conducted at -10 °C for NaCl concentrations up to  
305 7.5%. Three tests are presented for each salt concentration. We do not report error bars  
306 because all tests yielded very similar results. The deviation between the standard deviation  
307 and the mean value is < 6.0 % for the experiments until 5.0 % NaCl. For 7.5 % NaCl the  
308 deviation is 9.1 %. Higher concentrations could not be tested due to insufficient specimen  
309 strength as too much UWC was present.

310 Figure 5 shows the mean peak stresses from the tests. The most significant reduction in  
311 strength occurs already at very low salt contents. The specimen with 0.5% NaCl exhibits only  
312 about 25% of the peak stress of the reference specimen (0.0% NaCl). From this point  
313 onward, the reduction is approximately linear with increasing salinity, although local  
314 deviations (e.g., at 3.5–4.0% NaCl) are observed.

315 These results confirm earlier findings by Jagow-Klaff (2001), who reported that at -10 °C, a  
316 specimen with 3.0% NaCl had only ~20% of the strength of a salt-free specimen. The  
317 disproportionate loss of strength at very low salt contents highlights the sensitivity of frozen  
318 soil strength to even minor salinity, which can be explained by the high unfrozen water  
319 content relative to ice bonding at this temperature (Watanabe & Mizoguchi, 2002; Tilston et  
320 al., 2010).

321



322

323 **Fig. 5.** Mean failure stresses of uniaxial compression tests at -10 °C and -25 °C for different NaCl  
 324 contents. The dots show the three repetitions at each salt content.

325

#### 326 4.2.2 Unconfined compression tests at -25 °C ambient temperature

327 At -25 °C, specimens were fully frozen, including the residual eutectic brine. Figure 5 shows  
 328 the mean peak stresses as a function of NaCl concentration (0–10%). Again, three tests are  
 329 presented for each salt concentration. The deviation between the standard deviation and the  
 330 mean value < 1.3 % for the experiments containing NaCl. For 0.75 % NaCl the deviation is  
 331 2.5 %. The deviation for the reference sample (0% NaCl) is 3.4 %. This is justified by the  
 332 usage of the 10-t load cell instead of the 2-t load cell for the measurement of the reference  
 333 sample.

334 The reference sample (0% NaCl) exhibited significantly higher strength than at -10 °C,  
 335 reflecting the stronger, more continuous ice matrix at lower temperature. Interestingly also,  
 336 strength does not decrease monotonically with salinity. At low concentrations (up to 0.25%  
 337 NaCl), strength decreases, but between 0.25% and 1.0% NaCl, strength partially recovers,  
 338 forming a plateau before declining again exponentially with higher salinity.

339 We hypothesise that this non-linearity is caused by microstructure effects. At  $-25\text{ }^{\circ}\text{C}$ ,  
340 essentially all pore water is frozen, but at very low salinity ( $<0.5\%$ ), brine channels can still  
341 weaken intergranular bonding by creating micro-defects during freezing. At slightly higher  
342 salinity ( $\sim 0.5\text{--}1.0\%$ ), the segregated salt crystals or solidified brine pockets may “fill in” voids  
343 and act as local stiffeners, giving a temporary plateau in strength. Instead of isolated  
344 defects, there is a “packing effect” where salt precipitates partly stabilize the skeleton.  
345 Hence, the sharp strength drop halts, and you see a temporary plateau or partial recovery in  
346 the stress curve. At higher salinities ( $>1\text{--}2\%$ ), the increasing fraction of salt crystals  
347 incorporated into the matrix weakens the ice skeleton again because inclusions become too  
348 abundant, interrupting the continuity of the ice bonds. Instead of reinforcing, they act as  
349 weak, brittle inclusions within the ice–soil matrix. Strength therefore decreases again, now in  
350 a more systematic exponential fashion with salinity. A further factor affecting this hypothesis  
351 is that we observed that SC2 crystals show a semi-viscous behaviour (as a sludge) rather  
352 than Ice Ih that is harder and more brittle. This interplay also contributes to the above  
353 hypothesis, as SC2 is clearly stronger than liquid brine, but softer than Ice Ih. This will be  
354 further investigated in future work.

355 If we normalize the peak stresses (Figure 6) of the experiments at  $-10\text{ }^{\circ}\text{C}$  and  $-25\text{ }^{\circ}\text{C}$  to the  
356 respective reference samples with 0 % NaCl strength is reduced about 50 % highest at -  
357  $25\text{ }^{\circ}\text{C}$ . This is a significant difference to the observations at  $-10\text{ }^{\circ}\text{C}$  where the smallest  
358 observed amount of NaCl (0.5 %) decrease the strength to a value of about 25 % of the  
359 reference sample.

360

### 361 **4.3 NMR testing for determining the amount of liquid phase at $-10\text{ }^{\circ}\text{C}$**

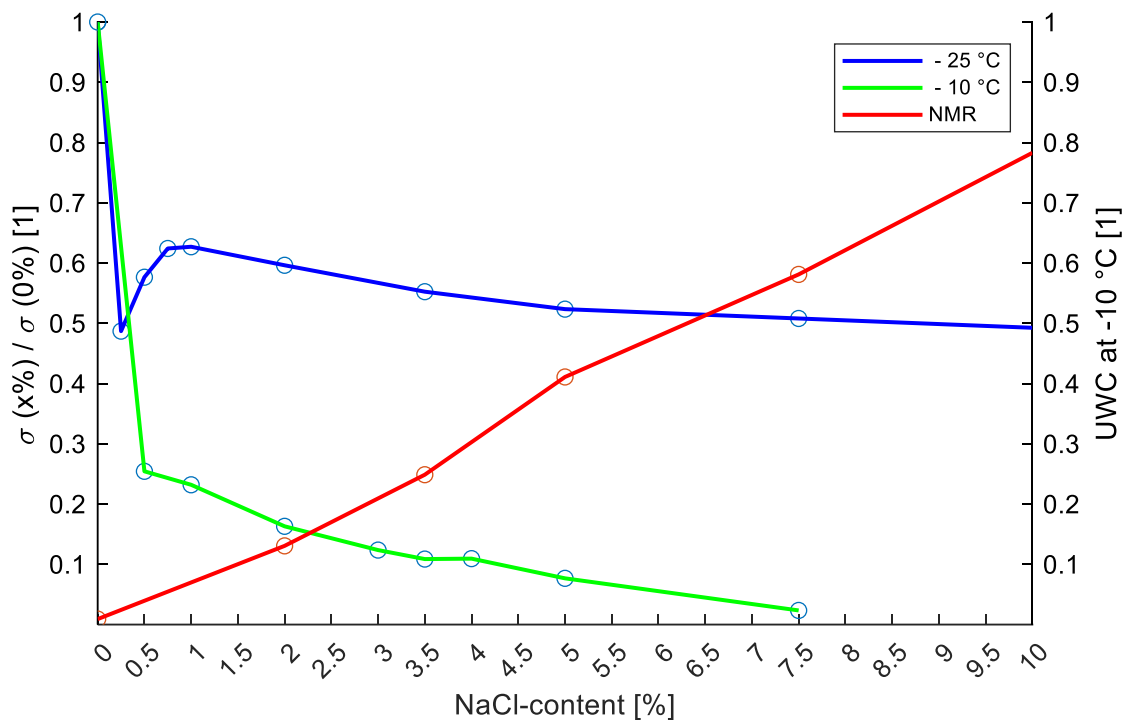
362 To directly measure the UWC, additional tests were performed using nuclear magnetic  
363 resonance (NMR).

364 All NMR relaxation measurements presented in this work are conducted with a low field  
365 Halbach NMR spectrometer with a frequency of 3.91 MHz (Halbach, 1980; Anferova et al.  
366 2007) using the Carr-Purcell-Meiboom-Gill (CPMG) pulse sequence (Carr & Purcell, 1954;

367 Meiboom & Gill, 1958). The shortest possible echo time in our setup is  $TE = 320 \mu\text{s}$  and,  
 368 depending on the saturation and relaxation behavior of the corresponding sample, up to  
 369 2500 echoes were recorded, yielding signal lengths up to 0.8 s. Initially, each CPMG echo  
 370 train was averaged until a signal-to-noise ratio of  $S/N \sim 200$  was reached. Details about the  
 371 measurement procedure can be found in the Appendix.

372

373



374

375 **Fig. 6.** To 0 % NaCl normalized mean failure stresses at -10 °C and -25 °C and determination of the  
 376 liquid phase related to the pore-volume with NMR at -10 °C for different NaCl contents

377

378 The results (Figure 6) show that the fraction of unfrozen liquid increases nearly linearly with  
 379 salinity. At 10% NaCl, approximately 80% of the pore water remained liquid at -10 °C,  
 380 leaving only 20% frozen.

381 The NMR measurements of unfrozen water content at -10 °C align well with predictions from  
 382 the NaCl-H<sub>2</sub>O phase diagram when the lever rule is applied. In a binary ice-brine system,  
 383 the lever rule gives the relative proportions of the two phases at a given bulk concentration  
 384  $C$  and temperature  $T$ :

385

386 
$$f_{\text{liq, ideal}}(C, T) = \frac{C - C_{\text{sol}}(T)}{C_{\text{liq}}(T) - C_{\text{sol}}(T)}$$

388

387 where

- 389 •  $f_{\text{liq, ideal}}$  is the theoretical liquid (brine) fraction,
- 390 •  $C$  is the bulk NaCl concentration,
- 391 •  $C_{\text{sol}}(T)$  is the solidus composition (ice boundary),
- 392 •  $C_{\text{liq}}(T)$  is the liquidus composition (brine boundary).

393 However, even salt-free specimens retain a small liquid fraction due to pore-scale forces  
394 (e.g. van der Waals interactions). NMR tests on the 0% NaCl sample indicated ~1% residual  
395 liquid water. To account for this, the corrected liquid fraction is expressed as:

396

398 
$$f_{\text{liq}}(C, T) = f_{\text{liq, ideal}}(C, T) + 0.01$$

397

399 Comparison of this corrected lever rule with NMR results (Table 2) shows excellent  
400 agreement up to about 5% NaCl. At higher concentrations, deviations become larger, likely  
401 due to pore-scale effects and salt redistribution not captured by the idealized phase diagram.  
402 This highlights important areas of future research.

403 At  $-25\text{ }^{\circ}\text{C}$ , the system enters the ice + NaCl·2H<sub>2</sub>O (SC2) stability field, and the coexisting  
404 liquid fraction predicted by the lever rule tends to zero (apart from the residual 0.01). This  
405 corresponds to the second plateau observed in the freezing curves (Figure 4).

406 Comparing these NMR results with the unconfined compression tests reveals a nonlinear  
407 strength–liquid relationship: the largest relative strength loss occurs already at very low salt  
408 concentrations, while further increases in liquid fraction reduce strength more gradually. This  
409 suggests that factors beyond liquid fraction alone — such as microstructural disruption of the  
410 ice–soil matrix — contribute significantly to strength reduction at low salinities (Arenson &  
411 Sego, 2004; Luo et al., 2023).

412 **Table 2.** Calculated liquid phase by lever-rule approach and measured liquid phase by NMR.

$\% \text{NaCl}$	$f_{\text{liq, ideal}}(C, T)$	$f_{\text{liq}}(C, T)$	<b>NMR results</b>
0.5	0.033	0.043	-
1.0	0.067	0.077	-
2.0	0.133	0.143	0.131
3.5	0.233	0.243	0.249
5.0	0.333	0.343	0.411
7.5	0.500	0.510	0.581
10.0	0.667	0.677	0.783

413

## 414 **5 Conclusions**

415 This study provides one of the few systematic experimental datasets that combine freezing  
 416 curve measurements and mechanical strength testing of saline sands, interpreted within the  
 417 framework of the NaCl–H<sub>2</sub>O phase diagram. While freezing point depression of saline soils is  
 418 well known, the disproportionate reduction in strength at very low salinities and the partial  
 419 recovery at eutectic conditions represent new insights into the coupled thermodynamic and  
 420 mechanical behaviour of frozen soils. These findings extend classical knowledge and have  
 421 direct implications for artificial ground freezing and permafrost engineering. The results  
 422 presented here are limited to a narrow-graded, fully saturated sand tested with NaCl  
 423 solutions at two ambient temperatures and a fixed strain rate, and should not be directly  
 424 extrapolated to soils containing fines, other pore-water chemistries, or different loading  
 425 conditions without caution

426 The main conclusions are as follows:

- 427 1. Increasing NaCl content systematically reduced both the supercooling temperature  
 428 ( $T_{\text{sc}}$ ) and equilibrium freezing point ( $T_f$ ). The observed freezing curves agree with the  
 429 NaCl–H<sub>2</sub>O phase diagram (Journaux et al., 2023) and confirm that brine remains

430 liquid above the eutectic temperature of  $-21.15\text{ }^{\circ}\text{C}$ . A simple lever rule confirms this  
431 and provides a simple, initial, way to quantify UWC.

- 432 2. At  $-25\text{ }^{\circ}\text{C}$ , specimens exhibited a second plateau in the cooling curves,  
433 corresponding to eutectic freezing of residual brine. The duration of this plateau  
434 increased disproportionately for concentrations above 5%, consistent with salt  
435 precipitation kinetics.
- 436 3. At  $-10\text{ }^{\circ}\text{C}$ , even 0.5% NaCl reduced strength to  $\sim 25\%$  of the salt-free reference value,  
437 confirming the disproportionate sensitivity of frozen soil strength to minor salinity. This  
438 effect is explained by the high unfrozen water content relative to ice bonding.
- 439 4. At  $-25\text{ }^{\circ}\text{C}$ , residual brine solidified, restoring ice continuity and resulting in higher  
440 overall strength. A temporary strength plateau between 0.25% and 1.0% NaCl  
441 suggests that salt crystallization may partially stabilize the matrix before higher  
442 salinities cause further strength loss. A microstructural plus crystal form explanation is  
443 provided but yet needs to be validated.
- 444 5. NMR results showed a nearly linear increase in unfrozen brine with salinity at  $-10\text{ }^{\circ}\text{C}$ ,  
445 reaching  $\sim 80\%$  liquid at 10% NaCl. However, the strength–liquid relation was  
446 nonlinear: the greatest relative strength loss occurred at low salinities, indicating that  
447 microstructural disturbance of the ice–soil skeleton is as important as liquid fraction  
448 alone.
- 449 6. For artificial ground freezing and saline permafrost, even low salinities can  
450 significantly compromise frozen soil strength at moderate subzero temperatures. At  
451 lower temperatures approaching the eutectic, strength partly recovers, but the  
452 presence of embedded salt crystals results in a different mechanical response than in  
453 salt-free soils. Design must therefore consider both freezing temperature depression  
454 and strength loss, with site-specific calibration for salinity.

455

456

457

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462

463 **References**

464 Amankwah, S. K., Ireson, A. M., Maulé, C., Brannen, R., & Mathias, S. A. (2021). A model  
465 for the soil freezing characteristic curve that represents the dominant role of salt  
466 exclusion. *Water Resources Research*, 57(8), e2021WR030070.

467 Andersland, O. B., & Ladanyi, B. (2004). *Frozen ground engineering*. John Wiley & Sons.

468 Anferova, S., Anferov, V., Arnold, J., Talnishnikh, E., Voda, M. A., Kupferschläger, K., ... &

469 Blümich, B. (2007). Improved Halbach sensor for NMR scanning of drill cores.

470 *Magnetic resonance imaging*, 25(4), 474-480.

471 Arenson, L. U., & Segó, D. C. (2004). Freezing processes for a coarse sand with varying

472 salinities. In *Proceedings of the Cold Regions Engineering & Construction*

473 *Conference, Edmonton, Alta* (Vol. 16719).

474 Atkins, P. W. (1996). *Physikalische Chemie*, 2. Auflage. VCH.

475 Banin, A., & Anderson, D. M. (1974). Effects of salt concentration changes during freezing

476 on the unfrozen water content of porous materials. *Water Resources*

477 *Research*, 10(1), 124-128.

478 Carr, H. Y., & Purcell, E. M. (1954). Effects of diffusion on free precession in nuclear

479 magnetic resonance experiments. *Physical review*, 94(3), 630-638.

480 Gao, X., Tian, R., Jiang, Y., Guo, Z., & Lei, L. (2024). Frozen saline sand can be highly

481 permeable. *Geophysical Research Letters*, 51(19), e2024GL111946.

482 Haghighi, H., Chapoy, A., & Tohidi, B. (2008). Freezing point depression of electrolyte

483 solutions: experimental measurements and modeling using the cubic-plus-

484 association equation of state. *Industrial & engineering chemistry research*, 47(11),

485 3983-3989.

486 Halbach, K. (1980). Design of permanent multipole magnets with oriented rare earth  
487 cobalt material. *Nuclear instruments and methods*, 169(1), 1-10.

488 Jessberger, H., & Jagow-Klauff, R. (2001). Bodenvereisung. *Grundbau-Taschenbuch, Teil*  
489 *2: Geotechnische Verfahren*, S. 121-166.

490 Journaux, B., Pakhomova, A., Collings, I. E., Petitgirard, S., Boffa Ballaran, T., Brown, J.  
491 M., ... & Hanfland, M. (2023). On the identification of hyperhydrated sodium  
492 chloride hydrates, stable at icy moon conditions. *Proceedings of the National*  
493 *Academy of Sciences*, 120(9), e2217125120.

494 Ju, Z., Lu, S., Guo, K., & Liu, X. (2023). Changes in the thermal conductivity of soil with  
495 different salts. *Journal of Soils and Sediments*, 23(9), 3376-3383.

496 Loomis, E. H. (1896). On the freezing-points of dilute aqueous solutions. *Physical Review*  
497 *(Series I)*, 3(4), 270.

498 Luo, C. L., Yu, Y. Y., Zhang, J., Tao, J. Y., Ou, Q. J., & Cui, W. H. (2023). Thermal-water-  
499 salt coupling process of unsaturated saline soil under unidirectional freezing.  
500 *Journal of Mountain Science*, 20(2), 557-569.

501 Meiboom, S., & Gill, D. (1958). Modified spin-echo method for measuring nuclear  
502 relaxation times.

503 Mitchell, J., Webber, J. B. W., & Strange, J. H. (2008). Nuclear magnetic resonance  
504 cryoporometry. *Physics Reports*, 461(1), 1-36.

505 Orth, W., Solf, O., Perl, C. & Rizos, D. (2021). *STUVA Conference 2021, Karlsruhe*. ISBN  
506 978-3-00-070615-8.

507 Rizos, D., Orth, W., Perl, C., Solf, O., Eramo, N. & Amin, T. (2022). Port Said Tunnels  
508 under the Suez Canal - Cross passages with ground freezing in aggressive  
509 conditions. *In Proceedings of the World Tunnel Congress (WTC). Copenhagen:*  
510 *ITA Bookshop*. ISBN 978-2-9701436-7-3

511 Tilston, E. L., Sparrman, T., & Öquist, M. G. (2010). Unfrozen water content moderates  
512 temperature dependence of sub-zero microbial respiration. *Soil Biology and*  
513 *Biochemistry*, 42(9), 1396-1407.

514 Wan, X., Lai, Y., & Wang, C. (2015). Experimental study on the freezing temperatures of  
515 saline silty soils. *Permafrost and Periglacial Processes*, 26(2), 175-187.

516 Wan, X., Liu, E., & Qiu, E. (2021). Study on ice nucleation temperature and water freezing  
517 in saline soils. *Permafrost and Periglacial Processes*, 32(1), 119-138.

518 Wan, X., Zhu, J., Lai, Y., Lu, J., & Yan, Z. (2024). Premelting theory-based mechanism for  
519 water freezing in saline soil. *Water Resources Research*, 60(10),  
520 e2024WR038013.

521 Wang, C., Li, K., Cai, H., Wu, Y., Lin, Z., & Li, S. (2023). Study of Supercooling  
522 Phenomena in Soil-Water Systems Based on Nucleation Theory: Quantifying  
523 Supercooling Degree. *Water Resources Research*, 59(11), e2023WR035935.

524 Watanabe, K., & Mizoguchi, M. (2002). Amount of unfrozen water in frozen porous media  
525 saturated with solution. *Cold Regions Science and Technology*, 34(2), 103-110.

526 Xiao, Z., Lai, Y., & Zhang, M. (2018). Study on the freezing temperature of saline  
527 soil. *Acta Geotechnica*, 13, 195-205.

528 Ying, S., Cao, Y., Zhang, Q., Xia, X., Li, G., Zhou, F., & Wen, T. (2025). The effect of salt  
529 on the freezing temperature of saline soil. *Soils and Foundations*, 65(1), 101566.

530 Zhou, J., Wei, C., Lai, Y., Wei, H., & Tian, H. (2018). Application of the generalized  
531 Clapeyron equation to freezing point depression and unfrozen water content.  
532 *Water Resources Research*, 54(11), 9412-9431.

533

534 **APPENDIX A - NMR measurements**

535 For measurement purposes, samples with an inner diameter of 2.7 cm (outer diameter 3.0  
536 cm) and a height of 5.5 cm were prepared in sealed glass tubes as recommended by Mitchell  
537 et al. (2008). This maintained a ratio of 1:2 again. Subsequently, the samples were frozen at  
538 -10 °C. A saturated NaCl solution without sand was also prepared to serve as a reference  
539 during measurement.

540 To carry out NMR measurements first, washers had to be placed in the NMR device to bring  
541 the sample to the correct height. The NMR device has a sensitive measuring range between  
542 heights of 70 mm and 100 mm and a highly sensitive range between 80 mm and 90 mm.

543 Since the sample had a height of 55 mm, it was raised by adding spacers up to 60 mm  
544 beneath it. Thus, the centre of the sample lay within the sensitive measuring range.

545 Subsequently, fine-tuning of excitation frequency was performed since it should have a value  
546 of 3.91 MHz for accurate measurement results

547 The measurement process for a sample proceeded as follows:

- 548 1. Measure temperature
- 549 2. NMR measurement of reference sample NaCl without sand
- 550 3. Measure temperature
- 551 4. NMR measurement of sand sample
- 552 5. Measure temperature
- 553 6. NMR measurement of reference sample NaCl without sand
- 554 7. Measure temperature

555 Temperature measurements between NMR measurements were necessary because during  
556 NMR measurements, cooling had to be switched off. Otherwise, electrical frequencies  
557 emitted by the freezer would disturb measurements. Each measurement took approximately  
558 half an hour during which time temperatures in the freezer increased by up to a maximum of  
559 0.9 °C during measurement periods.

560 To obtain meaningful reference measurements, averages from reference measurements  
561 before and after measuring sediment samples were calculated so that any temperature  
562 difference occurring during these measurements could be corrected.

563