

# Experimental observations of the main hypothesis employed in the definition of the wTCM finite element under compression

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## Abstract

Auxetic metamaterials, characterized by their negative Poisson's ratio, offer unique mechanical properties such as enhanced energy absorption, improved indentation resistance, and high shear stiffness, making them promising candidates for advanced engineering applications. This work presents experimental and numerical analyses of a 3D-printed coupon based on the General Auxetic Metamaterial (GAM) cell. A quasi-static compression test was performed to validate the auxetic behavior and to characterize the deformation and failure mechanisms. In parallel, an innovative multiscale finite element methodology based on the wTCM element was applied to replicate the mechanical response of the structure with significantly reduced computational cost. The results demonstrate strong agreement between experimental observations and numerical predictions in terms of global auxetic response, axial force-displacement behavior, and local failure modes. Once properly calibrated, the methodology enables accurate prediction of volumes with different sizes and geometries, thereby reducing the need for extensive experimental campaigns and enabling the efficient simulation of large-scale metamaterial structures.

*Keywords:* wTCM, metamaterial, experimental test, FEM calculation, multi-scale

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## 1. Introduction

Auxetic metamaterials (engineered architectures with a negative Poisson's ratio) exhibit the counterintuitive behavior of lateral expansion under axial compression or elongation under tension [11]. Their unique deformation mechanism enhance the energy absorption, gives excellent indentation and fracture resistance, and high shear stiffness qualities supported by extensive theoretical and experimental studies [5]. In fields such as aerospace, biomechanics, protective systems, or soft robotics, these advantageous properties position makes auxetics extremely promising candidates for future structures engineering [7].

Recent research has explored diverse auxetic architectures—including re-entrant honeycombs, chiral lattices, rotating rigid units, and origami-inspired designs—through advanced simulation and manufacturing techniques [10]. Specific structural designs like REC configurations have demonstrated notable gains in energy absorption via combining Finite Element analyses and physical testing [4].

Despite these advances, FEM-based simulations alone cannot fully capture real-world behavior of auxetic structures. Manufacturing defects, material heterogeneity, boundary conditions, and geometric imperfections or simply very complex geometries often lead to significant deviations between simulated and actual performance or simply make the FEM simulation unaffordable. Hybrid experimental-simulation approaches are vital: they

20 enable validation and calibration of FEM models—improving predictive accuracy—and  
 21 provide deeper insight into deformation mechanisms and failure modes under actual load-  
 22 ing.

23 In this study, a compression test on a 3D-printed auxetic metamaterial coupon struc-  
 24 ture is conducted, complemented by several simulation models that will capture the non-  
 25 linear behaviour of the structure. A detailed FEM model will be developed to obtain  
 26 the geometric nonlinearities of the coupon and an innovative methodology for multiscale  
 27 FEM simulations applied on metamaterial structures will be developed to capture both  
 28 geometric and material nonlinearities. The main goal is to: (1) validate the negative Pois-  
 29 son’s ratio behaviour of the metamaterial structure, checking its mechanical response, and  
 30 failure behavior; (2) validate an innovative methodology to fastly simulate metamater-  
 31 ial structures with quantitatively accurate results; (3) elucidate deformation mechanisms  
 32 and energy absorption phenomena driving auxetic performance under compression. This  
 33 integrated procedure strengthens proposed-FEM robustness and advances the application  
 34 potential of auxetic metamaterials in real-world engineering.

## 35 2. Methodology

36 This section provides a detailed analysis of both the experimental procedures and the  
 37 numerical simulations. First, it presents a comprehensive description of the manufactured  
 38 coupon, covering the manufacturing process and the development of the experimental  
 39 testing campaign. In parallel, the same test is analyzed through finite element (FE)  
 40 simulation models. A detailed FE model with large displacement capabilities (including  
 41 geometric nonlinearity) is developed to investigate the nonlinear response of the struc-  
 42 ture. In addition, the simulation is complemented by the formulation and development  
 43 of an equivalent multiscale FEM model, designed to efficiently reproduce the behavior of  
 44 metamaterial structures while capturing key nonlinearities such as buckling (geometric)  
 45 and damage (material). A detailed description of the manufactured coupon, a brief over-  
 46 view of the testing equipment, and a summary of the simulation models employed are  
 47 now exposed.

### 48 2.1. Coupon model geometry. 3D printing.

49 The proposed structure to be tested is based on the GAM (General Auxetic Metama-  
 50 terial) cell [3, 12]. This cell has the particularity of developing different behaviors de-  
 51 pending on the connectivity of the different metamaterial layers. For this case, auxetic  
 52 configuration is chosen, and cell parameters are exposed on the following table:

GAM Cell (Unit Dimensionless Cell)									
$v_1$	$v_2$	Step <sub>x</sub>	Step <sub>y</sub>	H <sub>star</sub>	D <sub>star</sub>	H <sub>prism</sub>	R <sub>bars</sub> [mm]	N. Cells	Scale Factor
-0.4	0.2	1	1	0.25	0.3	1.6	1.0	In Layer: 19 ; Layers: 7	17.5

Table 1: Auxetic and non auxetic cell structure parameters.

53 Based on these parameters, a hexagonal-based metamaterial structure is generated and  
 54 extruded, composed by 133 metamaterial cells. This configuration defines the coupon that  
 55 will be manufactured, which is shown below:

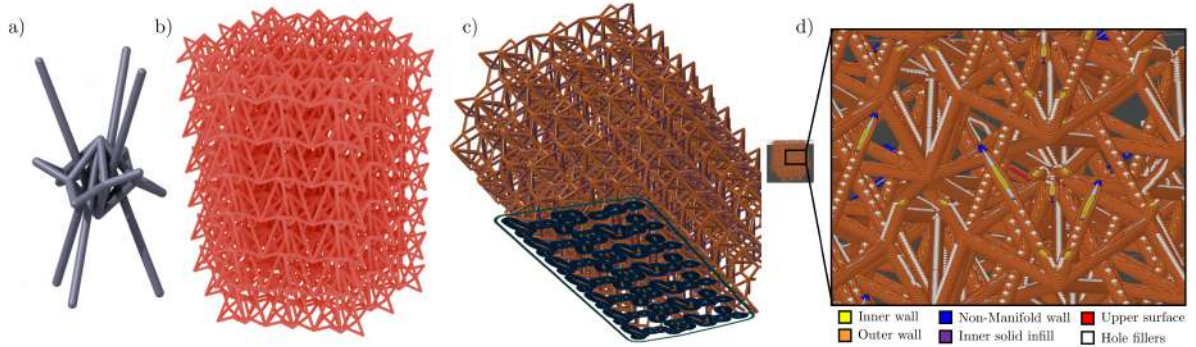


Figure 1: Metamaterial coupon. a) GAM cell geometry. b) Coupon geometry. c) Coupon manufacturing layout. d) Coupon geometry slicing strategy.

56 The coupon was produced using fused deposition modelling (FDM) technology and  
 57 a Bambu Lab X1-Carbon printer [1]. This printer is equipped with a high-precision  
 58 extrusion system with a hardened metal hotend, a 0.2 mm hardened steel nozzle, and  
 59 hardened steel extruder gears. The extruder can reach a maximum temperature of 300  
 60 °C, while the hot bed can operate up to 110 °C (at 220 V). The available manufacturing  
 61 volume is 256 x 256 x 256 mm<sup>3</sup>.

62 In terms of performance, the printer supports print speeds of up to 500 mm/s and  
 63 has a maximum acceleration of 20 m/s<sup>2</sup>. It features closed control fans for cooling the  
 64 hotend, the piece and the compartment to ensure optimal printing. The automatic bed  
 65 levelling system ensures proper filament adhesion throughout the printing process.

66 The material used was PLA Bambu Basic, a polylactic acid designed for high-speed  
 67 printing [2]. The filament has a nominal diameter of 1.75 mm and is supplied on 1 kg  
 68 spools. The mechanical properties of this PLA used are summarised in the table below:

Table 2: Mechanical and thermal properties of Bambu Basic PLA in X-Y plane and Z direction.

Direction	$E$ [GPa]	$\sigma_{UTS}$ [MPa]	$\varepsilon_{UTS}$ [%]	$\rho$ [kg/m <sup>3</sup> ]	$T_m$ [°C]
X-Y	$2.58 \pm 0.22$	$35 \pm 4$	$12.2 \pm 1.8$	1240	160
Z	$2.06 \pm 0.17$	$31 \pm 3$	$7.5 \pm 1.3$		

## 69 2.2. Experimental set up.

70 The compression test was performed using a Servosis servohydraulic frame equipped  
 71 with an Instron 8800 actuator of 250 kN capacity [13, 6]. Force was measured with a  
 72 100 kN Instron load cell. The experimental setup included a double-column frame with  
 73 a top-mounted hydraulic actuator, and a closed-loop electronic control system for force  
 74 and displacement.

75 The coupons were fixed by means of two flat compression plates, one upper and one  
 76 lower. This arrangement enables a uniform compression load to be applied, thereby  
 77 minimising the effects of slippage or misalignment. The plates are coaxially aligned and  
 78 adapted to rigidly clamp 3D-printed samples.

79 The test was carried out at a speed of 1 mm/min to ensure quasi-static conditions  
 80 during the deformation of the structure. This low speed minimises dynamic effects and  
 81 ensures a controlled load application, which is essential for an accurate analysis of the  
 82 overall mechanical behaviour of the PLA metamaterial specimen.

83 The system also features a digital control console, real-time monitoring and an emer-  
 84 gency stop button. Images of both machine and test set up are shown below:

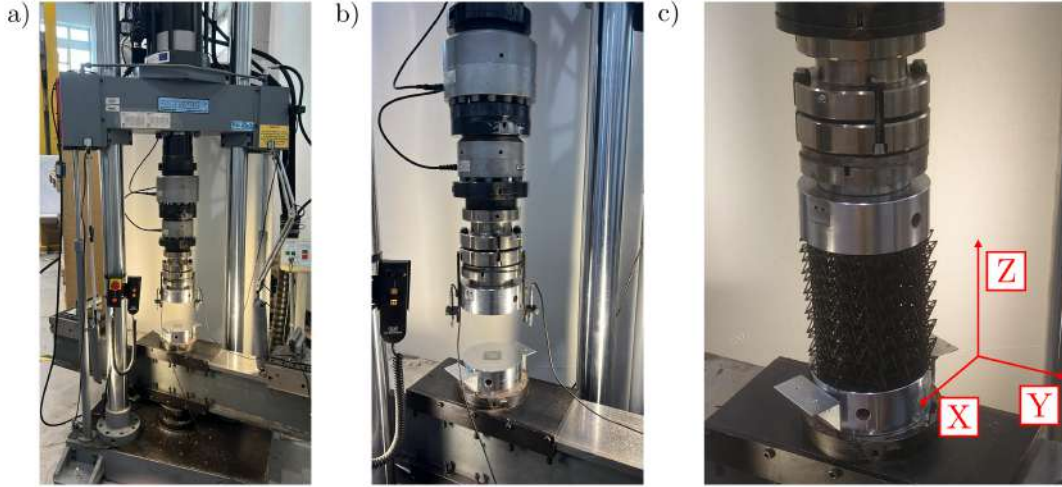


Figure 2: Tensile bench test layout. a) General view. b) Tie plate area view. c) Coupon positioned at tie plates.

85 *2.3. Geometrical nonlinearity. Explicit FEM.*

86 In order to rigorously validate the FEM methodology developed in the following section,  
 87 an explicit finite element (FE) model is first developed (a strategy commonly em-  
 88 ployed in the analysis of metamaterial structures). This model was implemented using  
 89 FEBio, an open-source finite element software primarily designed for biomechanical ap-  
 90 plications, but widely adopted for solving complex solid mechanics problems involving  
 91 large displacements and geometric nonlinearities [9]. FEBio enables the explicit simu-  
 92 lation of highly nonlinear problems, making it particularly suitable for modeling structures  
 93 with complex geometries, such as metamaterials, whose behavior is strongly influenced  
 94 by local buckling of the struts.

95 In the present study, a static loading scenario is simulated by gradually imposing  
 96 compressive displacements while recording the corresponding load response at the reac-  
 97 tion points throughout the process. The analysis explicitly accounts for large displace-  
 98 ments, allowing accurate capture of geometric nonlinear effects, such as local buckling, and  
 99 providing a high-fidelity representation of the structural response. The material model  
 100 employed is isotropic (neo-Hookean), with a Young’s modulus equal to half of the value  
 101 reported in Table 2. This reduction is attributed to inherent defects from the manufac-  
 102 turing process, as well as the effect of print directionality on the final material properties.  
 103 The finalized material parameters are summarized in Table 3.

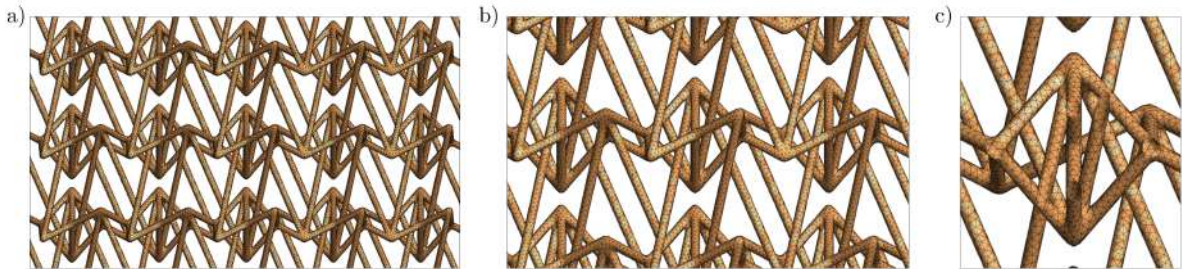


Figure 3: Detailed explicit FEM mesh: a) Through-layers mesh view. b) Cells mesh in a single layer view  
 c) Cell mesh detailed view.

104 The initial geometry for the development of this model is similar to that shown in  
 105 Fig. 1b). Due to the high geometric complexity of the coupon, a large number of finite  
 106 elements is required, and the only feasible meshing strategy is the use of tetrahedral ele-  
 107 ments. To reduce computational cost, a single-point integration scheme has been adopted,  
 108 significantly decreasing simulation time. No contact interactions are implemented in the  
 109 FE model. The generated mesh provides sufficient resolution in critical regions, enabling  
 110 accurate capture of the nonlinear phenomena associated with the complex geometry of  
 111 the metamaterial. A summarizing table for this case is exposed below:

Table 3: Configuration parameters for explicit finite element model.

$E$ [GPa]	$\nu$	Mat. Model	Contacts	Non Lin.	N. Nodes	N. Elements
0.9888	0.3	isotr. neo-Hookean	No	Geometric	481 888	1 351 050

112 This explicit FE approach, together with the experimental campaign, serves as a  
 113 benchmark for assessing the performance and accuracy of the subsequent multiscale FEM  
 114 methodology, particularly in reproducing nonlinear phenomena such as buckling and ma-  
 115 terial damage in metamaterial architectures.

#### 116 2.4. Geometrical and material nonlinearities. Implicit wTCM FEM methodology.

117 An innovative methodology is proposed for the development of simulation models  
 118 capable of quantitatively predict the behavior of metamaterial structures with significantly  
 119 reduced computational cost, in line with the approach presented by López-Salido and  
 120 Saucedo-Mora [8]. Firstly, the geometry of the metamaterial to be manufactured has  
 121 been developed using pentahedral elements. In this case, once the internal arrangement  
 122 of the struts within the elements is defined, it is replicated in space and connected to form  
 123 the geometry shown in Figure 1.

124 In parallel, a FEM model has been developed using pentahedral elements in which the  
 125 effect of the internal struts is retained. This effect is considered by accounting for their  
 126 local configuration and deformation at each calculation step. The element properties  
 127 (specifically, the Young’s modulus) are dynamically updated to accurately capture the  
 128 equivalent behavior of the metamaterial structure.

129 The inputs required for the FEM model are an initial value of Young’s modulus ( $E_0$ ),  
 130 which is updated dynamically during the first iteration until convergence is achieved,  
 131 thus having little influence on the final result. However, the Poisson’s ratio is constant  
 132 and must be defined for the entire simulation. In this case, a Poisson’s ratio of -0.5 was  
 133 selected based on the deformation observed in the experiment, which closely matches  
 134 the value derived from comparing the axial and cross deformations observed in it. The  
 135 measurement of the Poisson’s ratio is described in the Results section.

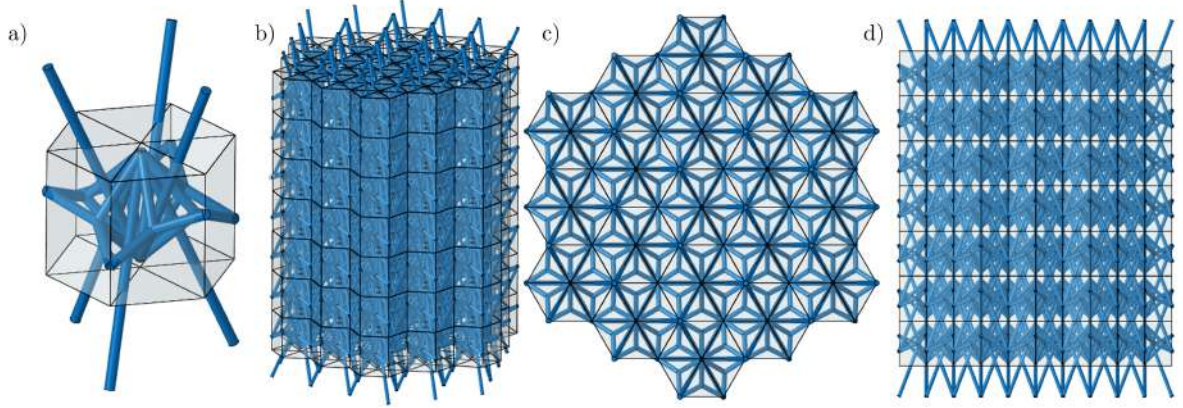


Figure 4: Metamaterial structure generated from pentahedral element. a) Cell equivalence. b) Coupon equivalence, iso view. c) Coupon equivalence, top view. d) Coupon geometry, front view.

136 As shown in Figure 4, the patterned structure within a single unit cell is replicated to  
 137 generate the target coupon model. Within this methodology, calibration curves are em-  
 138 ployed for the different struts composing the unit cell. These curves capture the behavior  
 139 of the struts across different regimes, including the linear elastic region and the nonlinear  
 140 regions, where various effects such as geometric buckling and material damage become  
 141 significant.

#### 142 *2.4.1. Implicit wTCM FEM Methodology with Geometric Nonlinearities*

143 The proposed methodology allows for the retention of all nonlinear effects through the  
 144 calibration curves assigned to the struts within the element. By using the curves developed  
 145 in the previous section, it is possible to reproduce all the nonlinear phenomena observed  
 146 during experimentation. For comparison with the explicit model, it is only necessary to  
 147 adjust the calibration curves to retain geometric nonlinearity while excluding material  
 148 nonlinearity, which is associated with stiffness degradation. Mesh model will be the same,  
 149 so computational cost will be similar.

### 150 **3. Results.**

151 This section analyzes the results obtained for the three proposed approaches. First,  
 152 the linear region of the explicit model and the experimental results are directly compared  
 153 with the innovative methodology proposed. Subsequently, the global structural response  
 154 is examined for the different cases, and local effects observed during compression are  
 155 analyzed for all approaches, assessing their validity and similarity.

#### 156 *3.1. Linear behaviour validation.*

157 This section presents the results obtained from the experimental test, the explicit FE  
 158 approach and the simulation using the wTCM element [8]. The primary aim is to demon-  
 159 strate how an appropriate calibration of the proposed simulation methodology enables  
 160 the quantitative prediction of the metamaterial's behaviour under specific loading condi-  
 161 tions. First, Digital Image Correlation measurement of the experimental test is compared  
 162 with the results obtained through FEM, at the moment when the test reaches an axial  
 163 compression of 3 mm.

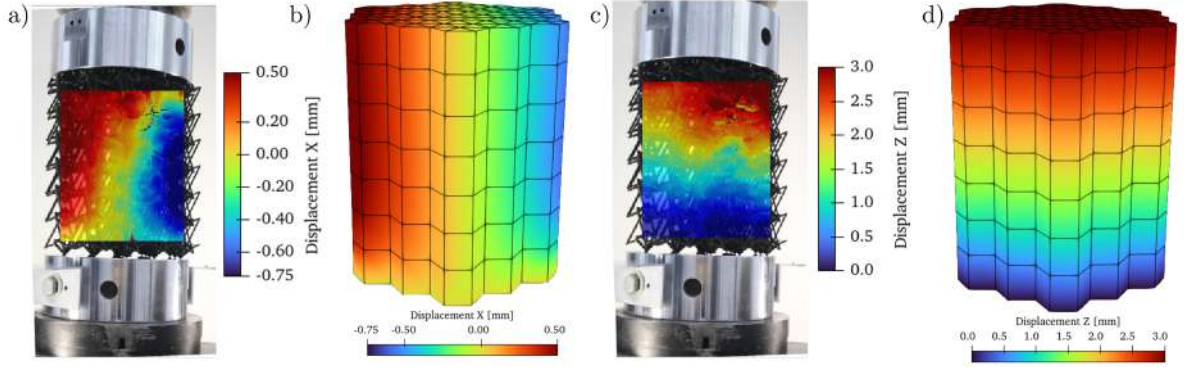


Figure 5: Displacement field for the test and the simulation at an intermediate load step. a) Test cross displacement. b) wTCM FEM cross displacement (buckling and damage nonlin.). c) Test axial displacement. d) wTCM FEM axial displacement (buckling and damage nonlin.).

164 At this stage, it can be observed that both the experiment and the simulation quant-  
 165 itatively record the same state of axial displacements, and a very similar state of cross  
 166 displacements. In the  $x$  displacement of Figure 5a there is a small misalignment that  
 167 can be given by a small out-of-plane movement of the sample, or a small anisotropy of  
 168 the metamaterial. With those measurements, and considering the size of the sample, a  
 169 Poisson's ratio of -0.5 is calculated. This demonstrates that the proposed methodology  
 170 provides an accurate approach to the real behavior of the structure and that the structure  
 171 has a negative Poisson's ratio.

172 Additionally, the same displacement state in the linear regime of the explicit FE model  
 173 is analyzed and compared with the model developed using the wTCM methodology.

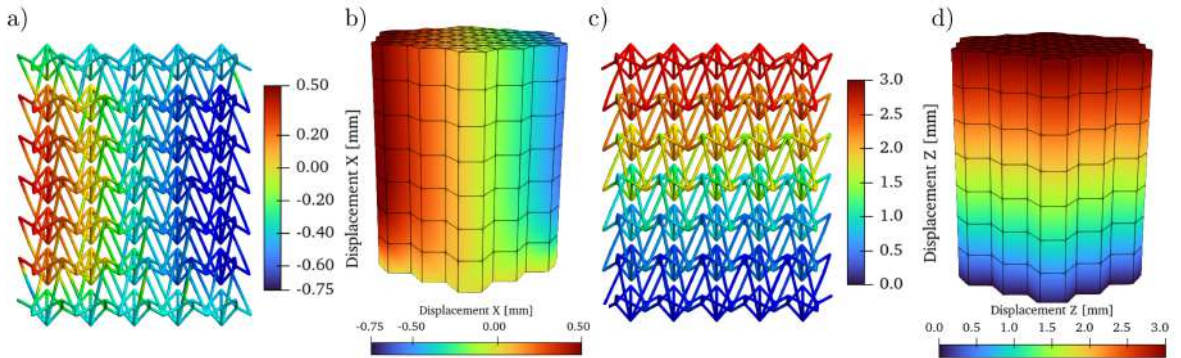


Figure 6: Displacement field for the detailed explicit FE simulation and wTCM simulation at an intermediate load step. a) Explicit FE cross displacement. b) wTCM FEM cross displacement (buckling and damage nonlin.). c) Explicit FE axial displacement. d) wTCM FEM axial displacement (buckling nonlin.).

174 Based on the results of the comparison, several important conclusions can be drawn.  
 175 First, a clear quantitative correlation in displacements is confirmed for both models. The  
 176 axial and crossed displacement fields are highly similar in both cases. Furthermore, in  
 177 the explicit model no anisotropy as the one found at image digitization process is present,  
 178 resulting in a homogeneous and continuous displacement distribution across the structure  
 179 for both approaches.

180 On the other hand, when analyzing the results obtained with the wTCM model con-  
 181 taining geometric nonlinearity, it is observed that both the displacement values and their  
 182 distribution are equal to those of the explicit FE model that includes damage effects

183 (hereafter referred to as the both buckling and damage-inclusive model). This outcome  
 184 can be explained by the fact that, although the two models account for different types  
 185 of nonlinear behavior in the nonlinear regime, their response in the linear regime is es-  
 186 sentially the same. Consequently, the displacement maps remain consistent across the  
 187 different wTCM models.

### 188 3.2. Global behaviour validation.

189 This section analyzes the global behavior of the structure across the three approaches.  
 190 First, the calibration curves employed in the wTCM models are examined in detail (Fig.  
 191 7a). The solid lines correspond to the model that includes both geometric and material  
 192 nonlinearities (G&M), while the dashed lines represent the model accounting just for  
 193 geometric nonlinearity (G). As anticipated, these curves are identical in the linear regime;  
 194 however, their responses diverge in the nonlinear regime, where the distinct effects of each  
 195 nonlinearity behaviour become evident.

196 Furthermore, Fig. 7b presents the force-displacement curves under compression for  
 197 the three approaches.

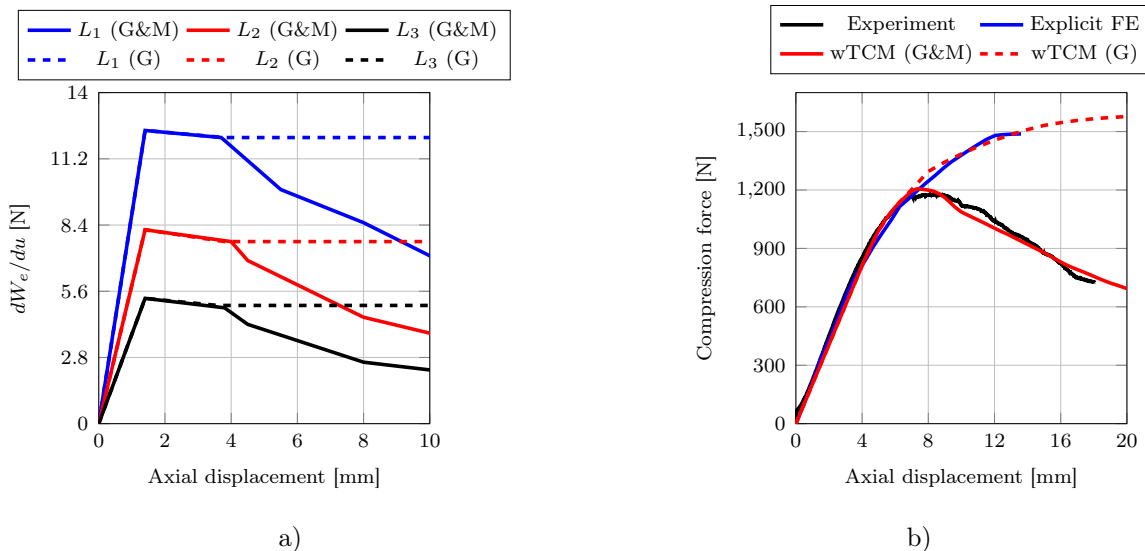


Figure 7: a) FEM calibration curves for axial compression with the wTCM element.  $L_1 = 10.79mm$ ,  $L_2 = 14.93mm$ ,  $L_3 = 43.54mm$ . Solid lines for geometric and material nonlinearities, dashed lines for just geometric nonlinearities. b) Axial compression force-displacement curves for all the approaches.

198 Based on the results exposed, the following conclusions can be drawn:

- 199 • The calibration curves are consistent. The curves for both wTCM models are  
 200 identical in the linear regions. Their divergence in the non-linear regime reflects  
 201 the stiffness loss of the struts in the damage-included model, which is coherent with  
 202 the phenomena captured.
- 203 • The results are consistent in the linear regime. The force-displacement curves ob-  
 204 tained from the experiment, the explicit FE model and the wTCM-based models all  
 205 show a clear and direct correlation in this region.
- 206 • The wTCM methodology proves to be versatile, and its validity is reaffirmed. The  
 207 model that incorporates both damage and buckling effects successfully reproduces  
 208 the experimental observations. Similarly, the model that considers only buckling fits

209 well with the explicit FE model curve, which considers only geometric nonlinearity.  
210 These outcomes strengthen the robustness and validity of the proposed methodology.

211 Thus, the correlation among the three approaches for the global behavior of the struc-  
212 ture is confirmed.

213 *3.3. Experimental local effects.*

214 During the experimental campaign, several local effects were identified. Some of these  
215 effects arise from the complex geometry of the metamaterial structure itself, while others  
216 are inherent to the manufacturing process of the coupon. These effects are analyzed in  
217 detail below, with reference to Fig. 8:

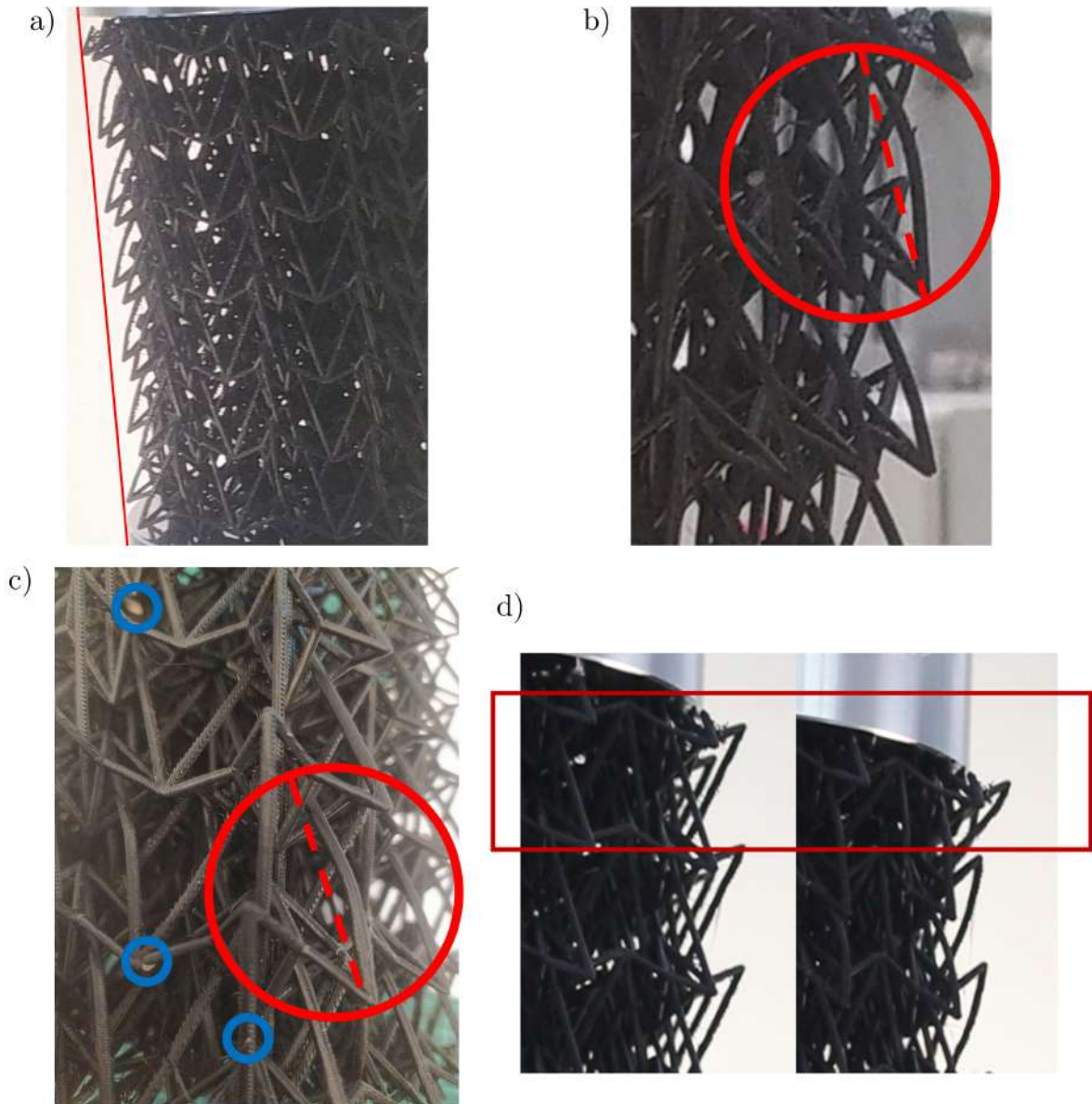


Figure 8: Auxetism effect on GAM structure along the compression test. a) Global auxetic effect at a specific step on compression test; b) Detailed view of the failure of the longest bars while the compression test is carried out; c) In red: remaining plastic strain deformation in GAM structure after unloading. In blue: local failure found at strut joints. d) Local failure of the first layer at final states of the compression loading.

218 As anticipated in Figure 5a, the global auxetic behaviour of the structure during com-  
 219 pression is clearly visible, and is also highlighted in Figure 8a. The onset of the nonlinear  
 220 regime is evident when nonlinear phenomena, such as buckling of the slenderest struts,  
 221 appear during the loading process, as shown in Figure 5b. Figure 5c illustrates material  
 222 nonlinearities through the failure modes observed after unloading the structure, including  
 223 breakage at certain joints and visible plastic deformation at other connections. Similarly,  
 224 permanent deformation was observed in the longest struts, which remain deformed once  
 225 the structure is unloaded.

226 Finally, Figure 5d clearly shows the local failure of the first layer of the auxetic  
 227 metamaterial, which is caused by the buckling and subsequent fracturing of the vertical  
 228 connectivity struts. This type of localised failure is particularly relevant from a simulation  
 229 perspective. Although it is highly localised, it has a strong impact on the global structural  
 230 collapse.

231 Overall, these local phenomena will be compared in detail with those observed in the  
 232 simulation models, which are analyzed in depth in the following section.

### 233 3.4. Simulation local effects.

234 Finally, the local effects are analyzed from the simulation perspective. As demon-  
 235 strated in the previous section, the first nonlinear phenomenon to appear is buckling,  
 236 which is accurately captured by the explicit FE model. This is particularly important  
 237 because the onset of buckling in slender struts largely governs the subsequent structural  
 238 response and failure mechanisms. The following figure provides a detailed visualization  
 239 of these effects on the explicit FE:

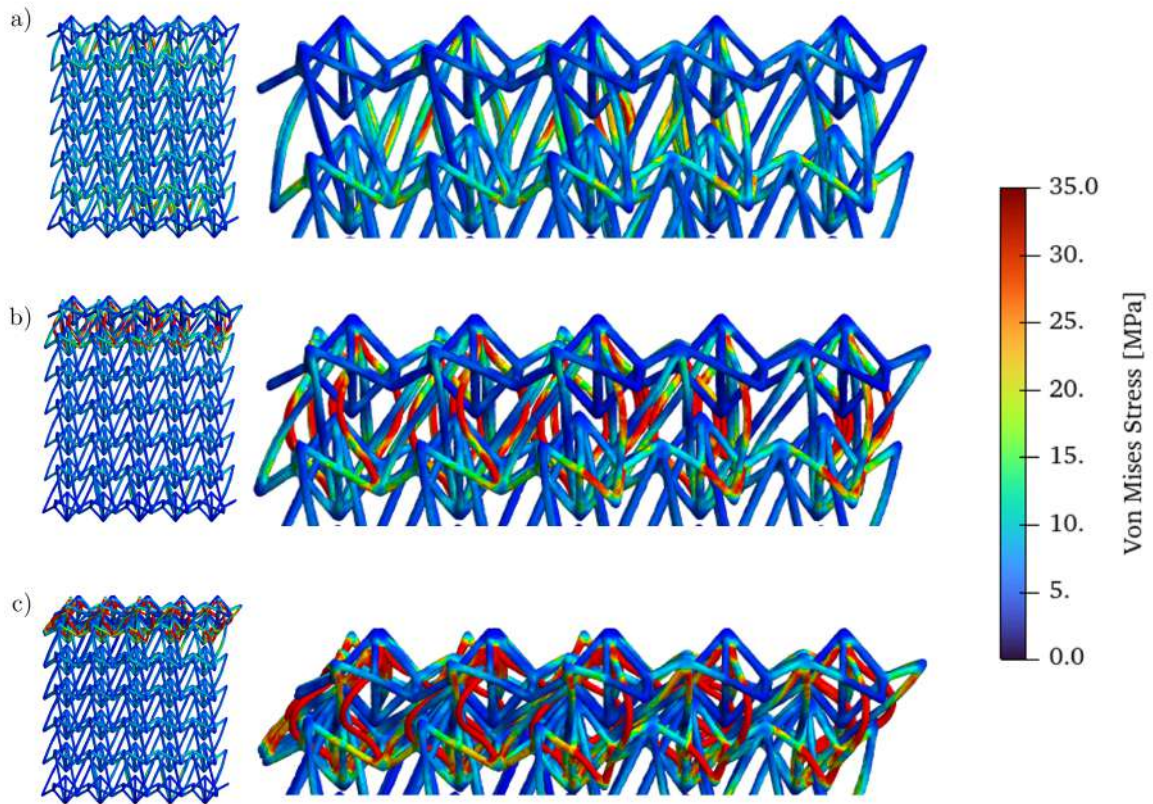


Figure 9: Local failure of first layer found on explicit FE model. a) Beginning of buckling phenomenon. b) Evolution of buckling phenomenon along compression process. c) Final state of local failure of first layer due to buckling phenomenon.

240 As shown in Figure 9a, geometric nonlinearity induces local buckling of the slenderest  
 241 struts in the explicit FE model. This phenomenon can also be examined in greater  
 242 detail in Figure 11b), where the localized buckling of these struts is clearly illustrated.  
 243 Notably, this response closely matches the experimental observations reported in Figures  
 244 8b) and c), confirming the ability of the explicit model to accurately capture the onset  
 245 and progression of local instabilities that dominate the structural behavior. Moreover, the  
 246 failure of these struts is localized in the first layer, (named as the boundary layer), which  
 247 coincides with the local failure observed experimentally. This phenomenon is also detected  
 248 by the wTCM model, where a change in stiffness is observed in the axial force-displacement  
 249 curve corresponding to the onset of buckling. However, the stiffness continues to increase  
 250 monotonically in the explicit model and the subsequent wTCM model, as no plasticity  
 251 model has been implemented for this case.

252 Figures 9b) and c) illustrate the development of this buckling behavior without consid-  
 253 ering strut failure. It is important to note that, while the small in-plane sliding observed  
 254 in the last figure appears to be captured experimentally, its magnitude is very limited.  
 255 Before this state could fully develop, other phenomena would occur, such as inter-layer  
 256 contact or strut fracture due to exceeding the ultimate tensile stress. This highlights  
 257 that certain localized effects observed in the simulation may be partially constrained or  
 258 suppressed in the real structure by additional failure mechanisms not explicitly modeled  
 259 in the FE simulations. Figure 10 provides a detailed analysis of this phenomenon too,  
 260 emphasizing its relevance as it anticipates through simulation the local effect that is later  
 261 observed experimentally:

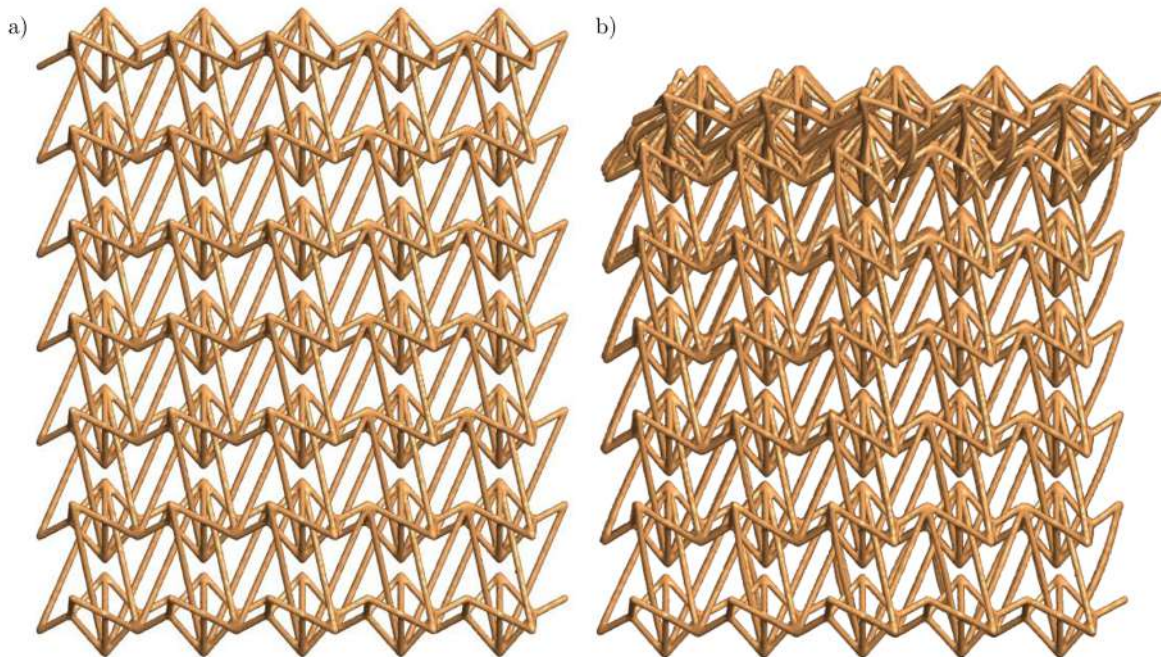


Figure 10: Explicit FE mesh. a) before compressing. b) after compression, where failure at boundary layer has been developed.

262 On the other hand, carefully analysing the model using the wTCM methodology, local  
 263 effect can be found too. Specifically, this is analysed in the following image.

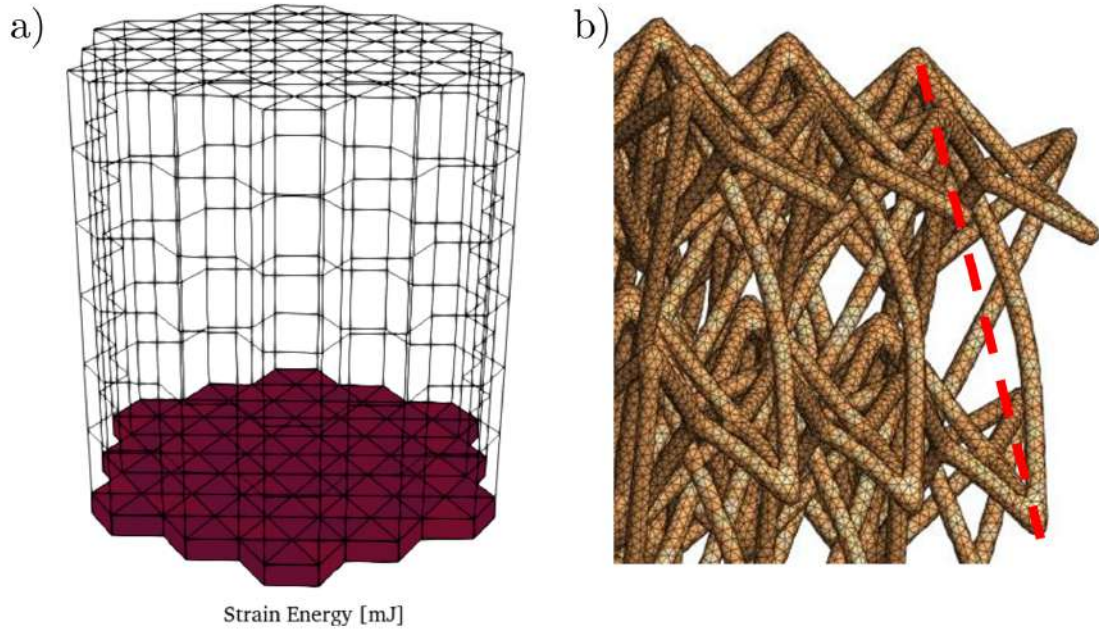


Figure 11: Isolated limit layer failure for the axial compression test: a) Captured phenomenon at the multi-scale FEM, filtered with a strain energy criterion of  $>50$  mJ. b) Local buckling of slenderest bars at explicit FE model.

264 As can be observed, the wTCM model shows a concentration of strain energy in the  
 265 elements of the boundary layer, clearly highlighting the local failure of the structure in  
 266 this layer in a much faster and more straightforward manner than the explicit model.  
 267 As expected, this local effect, observed during the experimental campaign, is successfully  
 268 captured by the proposed methodology.

269 This demonstrates the robustness of the approach, which employs an equivalent FEM  
 270 model with TCM elements that can be pre-calibrated to accurately predict the behavior of  
 271 auxetic metamaterial structures. Moreover, the methodology allows for the consideration  
 272 of several nonlinear phenomena, ranging from geometric buckling to moderate material  
 273 plasticity, as discussed throughout this article.

### 274 3.5. Discussion of problem complexity reduction

275 Finally, the impact of implementing this methodology on computational performance  
 276 is analyzed. It is evident that it leads to a significant reduction in resource requirements, as  
 277 the number of degrees of freedom is drastically reduced. One of the key advantages of the  
 278 wTCM element methodology lies in the fact that the mesh used across the different models  
 279 remains unchanged, with no need for further refinement. All the relevant information is  
 280 embedded in the calibration curves, which govern the behavior of the struts. Consequently,  
 281 the computational cost is not affected by how these curves evolve to retain different  
 282 nonlinear responses. This feature makes the approach particularly efficient, as it decouples  
 283 mesh complexity from material and geometric nonlinearities, allowing the methodology  
 284 to handle diverse structural behaviors without additional meshing effort. This point can  
 285 be checked in next figure:

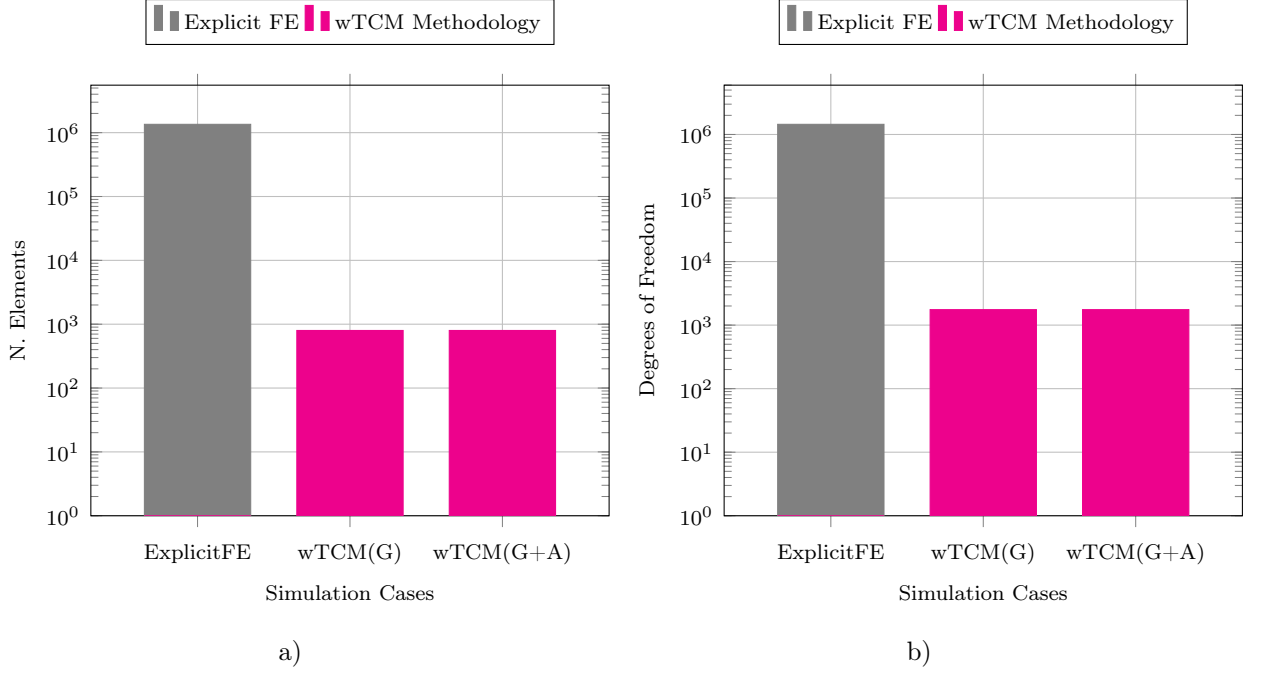


Figure 12: a) Bar chart comparing the number of elements across the three approaches. b) Bar chart comparing the number of degrees of freedom (DOFs) across the three approaches.

286 As illustrated in figure 12, a gain of three orders of magnitude is achieved both in  
 287 the number of elements and in the total degrees of freedom. Furthermore, as previously  
 288 demonstrated in [8], the main potential of the methodology lies in the ability to perform  
 289 a simple pre-calibration on reduced models, which then allows the reliable prediction  
 290 of the behavior of mesoscale models with high confidence. This capability makes the  
 291 methodology not only efficient but also scalable to larger and more complex structures.

292 By establishing an equivalence between the struts and pentahedral elements, the meth-  
 293 odology enables simulations to be carried out with significantly reduced computational  
 294 time and moderate hardware requirements. This represents a major advantage over other  
 295 modeling approaches, such as beam-element models or detailed tetrahedral-element mod-  
 296 els, which may involve hundreds of thousands of degrees of freedom. Remarkably, the  
 297 complete simulation was executed in just 33 minutes on a computer with 16 GB of RAM  
 298 and an 8-core processor, implemented in MATLAB using a serial code.

#### 299 4. Conclusions

300 After the development of all sections, it can be concluded that both the explicit model  
 301 and the wTCM models adequately correlate with the phenomena observed in the exper-  
 302 iment, while accounting for the specific effects captured by each model. On one hand,  
 303 the explicit FE model accurately captures the geometric nonlinearity, which is the first to  
 304 manifest when slender bars begin to buckle. This phenomenon aligns with experimental  
 305 observations and is similarly to the one captured by the wTCM model, which accounts for  
 306 the loss of stiffness. However, the explicit model diverges from the experimental results  
 307 when material nonlinearity becomes significant (plasticity and failure).

308 At this point, the model developed using the wTCM methodology becomes particularly  
 309 relevant, as it demonstrates its strength. Once properly calibrated for a single case,  
 310 the proposed methodology can predict the behavior of volumes of different sizes and  
 311 geometries. Furthermore, it retains the ability to capture multiple nonlinearities, such

312 as geometric and material effects, without imposing a higher computational cost. This  
313 capability significantly reduces the number of experimental tests required to characterize  
314 the response of metamaterial structures, leading to substantial savings in both cost and  
315 time.

316 Moreover, the methodology allows for the numerical simulation of large metamaterial  
317 volumes at an affordable computational cost, making it feasible to analyze large-scale  
318 structures from a simulation standpoint. Finally, it is important to emphasize that the  
319 simulation models capture the local effects that emerge during experimentation with con-  
320 siderable accuracy and detail, enhancing their validity and robustness.

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