

# DEM simulation of mechanical arcs in granular flow

Paulo Lopes<sup>1</sup> • Milene S Lana<sup>2</sup> • José M Silva<sup>3</sup> • Hernani M Lima<sup>4</sup>

Received: / Accepted: / Published online:

**Abstract** Numerical methods are an important tool in engineering as they allow the approximate resolution of problems that do not have exact analytical solution. Recently, several research fields, including geomechanics, engineering, chemistry, physics and applied mathematics, have shown a renewed interest in accurately modeling the granular materials, and examine both the break, flow and deformation. The two main lines of research are continuous mechanical approach and, in contrast, the discrete mechanical approach. This work will focus the discrete approach, from real data flow test in a silo with crushed gneiss, we perform numerical simulation tests, with the discrete elements method, using the PFC2D software. This back analysis elucidated some questions about constitutive properties of the studied material and their behavior during the granular flow, which allowed from a few experimental data, reproduce reasonably the physical phenomenon in question. The simulated granular flow has a difference of less than 5% for the finer size fraction which was tested.

**Keywords** discrete elements method; numerical modeling; granular flow

---

<sup>1</sup> Beyond Mining – Belo Horizonte– Brazil – [paulo@beyondmining.tech](mailto:paulo@beyondmining.tech)

<sup>2</sup> Federal University of Ouro Preto (UFOP) – Department of Mining Engineer (DEMIN) – Ouro Preto – Brazil – [milene@demin.ufop.br](mailto:milene@demin.ufop.br)

<sup>3</sup> Federal University of Ouro Preto (UFOP) – Department of Mining Engineer (DEMIN) – Ouro Preto – Brazil – [jms@ufop.edu.br](mailto:jms@ufop.edu.br)

<sup>4</sup> Federal University of Ouro Preto (UFOP) – Department of Mining Engineer (DEMIN) – Ouro Preto – Brazil – [hernani.lima@ufop.edu.br](mailto:hernani.lima@ufop.edu.br)



## 1 Introduction

Granular materials may be defined as a set of discrete or agglomerated solids immersed in a fluid, macroscopic particles characterized by losing energy whenever there is interaction between them. A typical example of these interactions is friction during the collision between grains. The particles that make up such a granular material should be large enough so that they are not subject to fluctuations, convection movements of thermal origin, or Brownian movement. Thus, the minimum size of particle diameter is  $1\mu\text{m}$  of order, and the maximum size varies according to the dimensions of the system being considered. In these cases, it becomes more important that the relative size between the particles and the system than its absolute size.

In the discrete approach, each particle of the granular medium is treated individually as well as their interactions with each other, respecting the basic principles of mechanisms. Despite being easily conceptualized, application of this method requires algorithms and computational routines, in order to process the huge volume of transactions relating thereto.

To this end, we have developed the method of discrete elements, to simulate the movement and interaction of a large number of particles, and is the main tool used in this work number.

Table 1 summarizes step-by-step the basic routine operations, data entry and boundary conditions, generically. The implementation of this algorithm indeed should obey the rules, syntax and constraints inherent in the language or platform used.

**Table 1** Generic algorithm illustrating the method of discrete elements  
(adapted from Göncü, 2012)

<b>INPUT:</b>	Initial positions and velocities Time end of simulation T
<b>BALANCE:</b>	Initialize the time and particle positions, velocities and forces.

---

```

while t < T do
    for all particles do
        Find contacts or interacting pairs
        Compute and add up forces
    end for
    for all particles do
        Integrate the equations of motion
        Update positions and velocities
    end for
    Update system boundaries
    t = t + Δt
end while

```

---

**OUTPUT:**                      Monitoring history  
    Vector fields  
    Scalar fields

---

Many authors dedicated to the study, including the works of Balevičius (2008 and 2011), Capriz (2008), Cleary & Sawley (2002), Coetzee & Els (2009 and 2010), Göncü (2012), Hill & Selvadurai (2005), Mishra & Thornton (2002), Nedderman (2005), Neves (2009) and Silva (2005 and 2006), which was extracted this case study.

## 2 Case study

Silva (2005), Silva (2005) used reduced scale physical models to study the influence of several factors on the behavior of the bulk material flow, applicable to underground mining among them were the principal:

- Material column height
- Angle of the passage
- Humidity
- Change of direction (knee) in the passage
- Presence of clay and other fines
- Flow obstruction problems
- Discharge section
- Particle size range of the material
- Material type (gneiss, dolomite, sand)

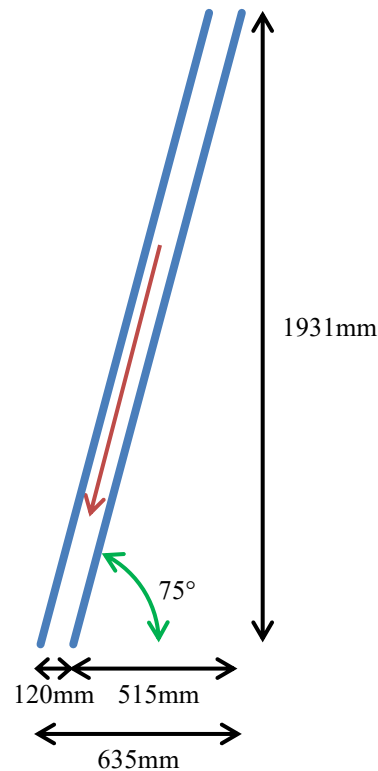
In Fig. 1 we can observe the actual small-scale model used for the flow tests, as well as an example of the formation of a mechanical arc.



**Fig. 1** a) Experimental ore pass used for testing. b) Example of granular flow obstruction due to the formation of a mechanical arc

### **3 Numerical simulation**

From this study, we defined practical application factors in the design of bulk material flow situations. Fig. 2 shows the measures of the physical models, extracted and implemented for numerical simulation.



**Fig. 2** Conceptual design of the ore pass of case study, to be implemented in the numerical simulation model

The value used on the simulations for the angle of repose was  $35^\circ$  (friction coefficient = 0.7), both the internal friction between the particles and the friction between the particles and the wall of the ore pass. The density value of the gneiss used was  $2.63\text{g/cm}^3$ .

After construction, the numerical model was filled with particles of sizes from 25 to 19mm (gravel 2), 19 to 9.5mm (gravel 1) and 9.5 to 4.8mm (gravel 0).

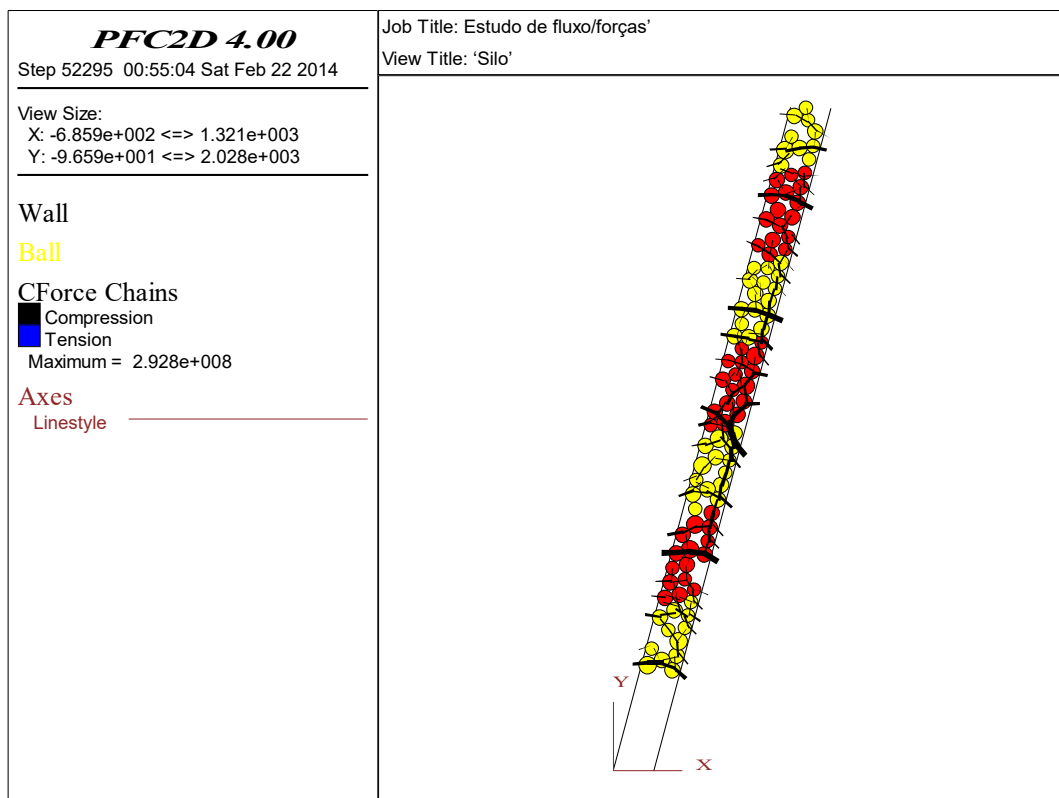
Following the generation of particles was started early iteration of the model in order to balance the unbalanced forces of the system, in the condition before the flow.

Finally, after stabilization of the system before the flow, this was released, and there was the formation of a mechanical arc or granular flow, as the particle size range studied.

To measure the mean flow velocity in cases where it occurred were monitored 10 points along the axis of the silo, to create a history of velocities, showing their evolution over the simulation.

#### 4 Results and discussion

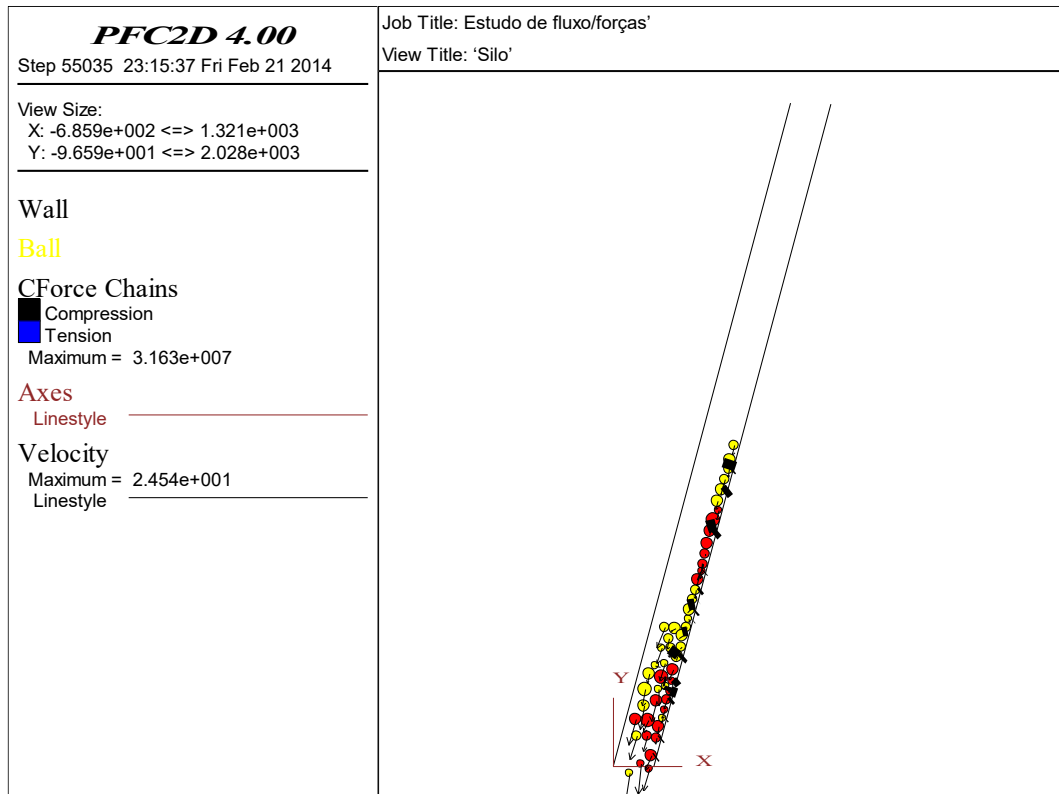
The results of the numerical model using the method of discrete elements were divided according to different particle sizes used in the case study reproduction, for comparison of both results. The Fig. 3 shows the formation of a mechanical arc upon releasing the flow into the gravel 2.



**Fig. 3** Mechanical arc after release the flow in the numerical model, for particle size ranging from 25 to 19mm

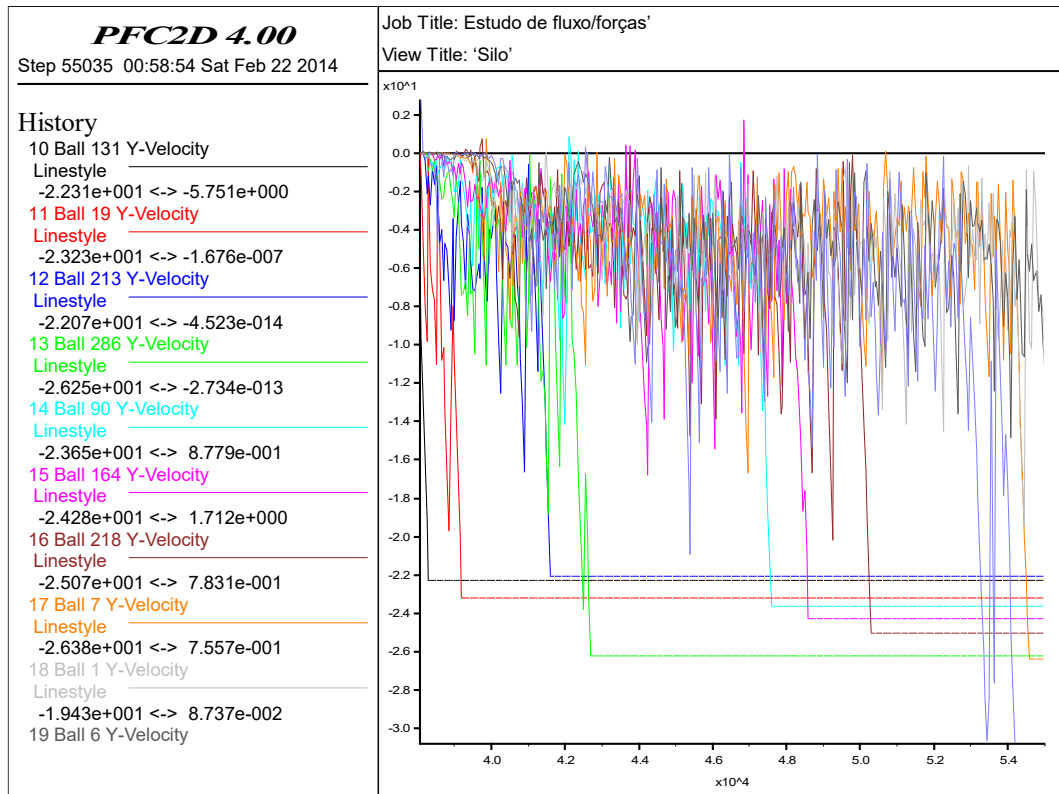
The numerical model for the particle size ranging from 25 to 19mm was consistent with data from Silva's work (2005), where there was a mechanical arc in all tests.

The Fig. 4 shows the full granular flow after release of the gravel 1.



**Fig. 4** Full flow occurrence in the numerical model, the particle size range from 19 to 9.5mm

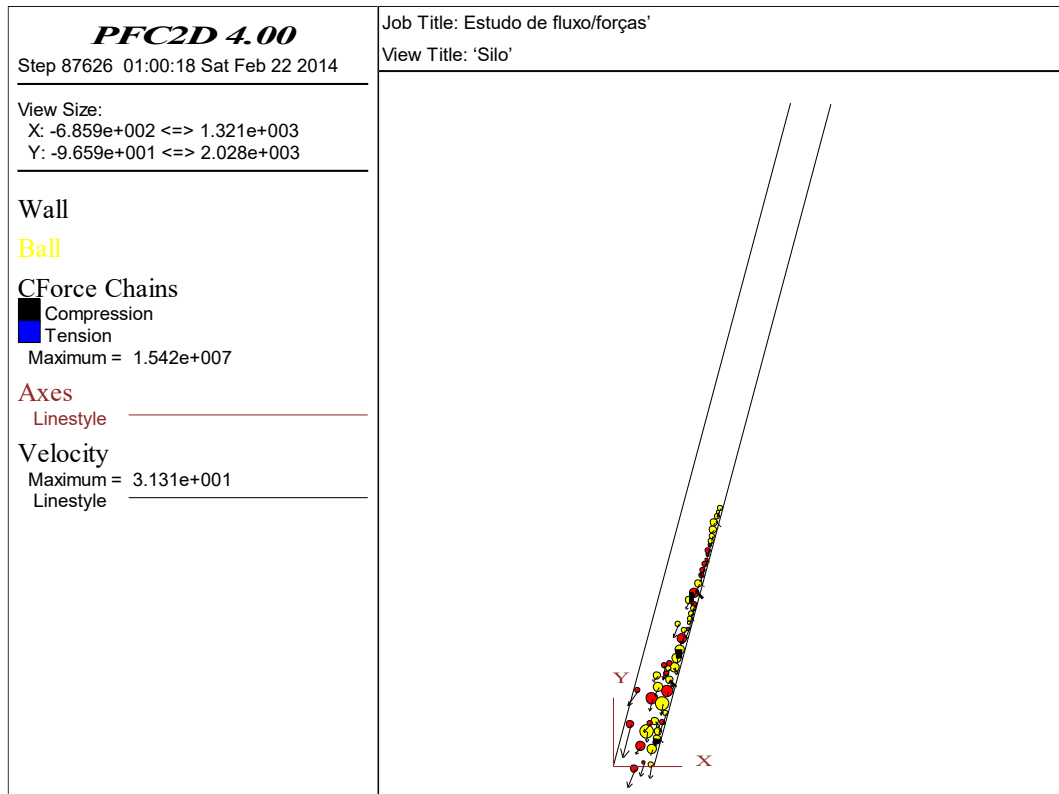
The numerical model for the particle size range from 19 to 9.5mm was consistent with experimental data, where there full granular flow in all tests. It was measured the evolution of the mean flow velocity as the velocity history shown in Fig. 5.



**Fig. 5** History of the descending flow velocities in numerical model along its axis in the particle size ranging from 19 to 9.5mm

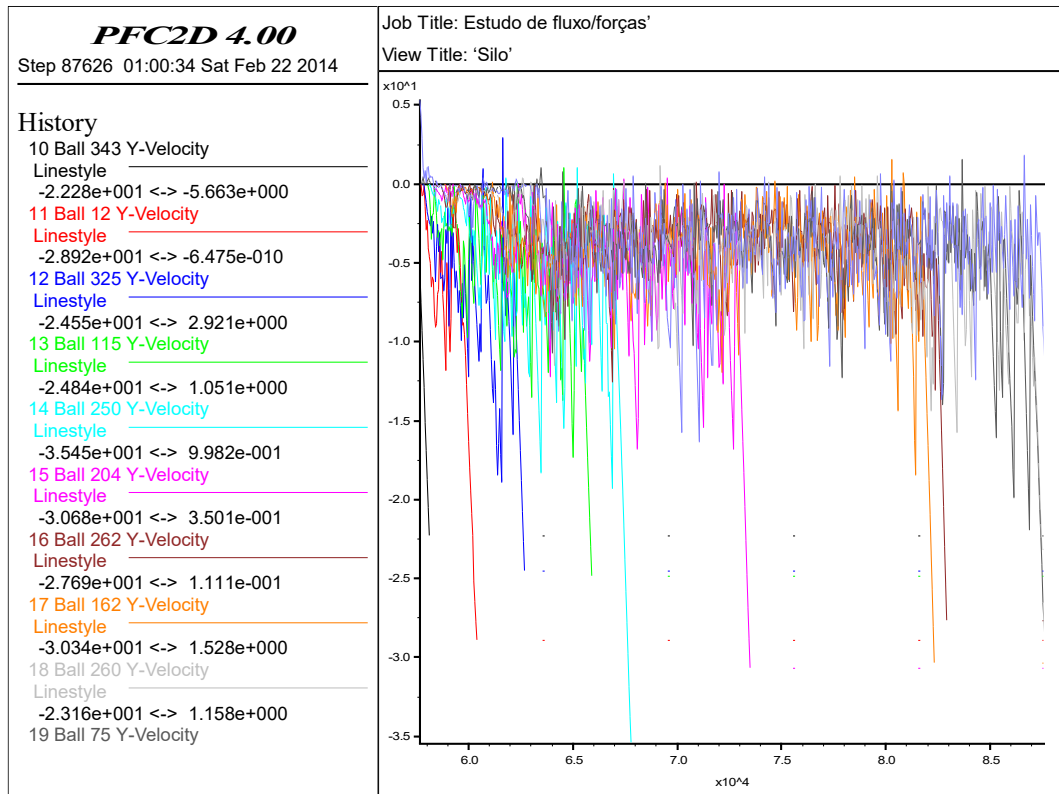
The mean flow reached an stable velocity, at each monitored point, of 23.63 cm/s. This value is consistent with the results obtained in the physical modeling experiments which was 20.73 cm/s.

The Fig. 6 shows the full granular flow after releasing the gravel 0.



**Fig. 6** Full flow occurrence in the numerical model, the particle size ranging from 9.5 to 4.8mm

The numerical model for the particle size ranging from 9.5mm to 4.8mm was consistent with experiments data, where there full granular flow in all tests The mean flow velocity evolution was measured and recorded as show in Fig. 7.



**Fig. 7** History of the descending flow velocities according to the numerical model along its axis in the particle size ranging from 9.5 to 4.8mm

The mean flow reached an stable velocity, at each monitored point, of 27.55cm/s. This value is consistent with the results obtained in the physical modeling experiments which was 28.55cm/s

The difference of the velocities for the particle size range from 19mm to 9.5mm are the result of the spherical shape of real particles, which in conditions arising from the case study of scale, allow greater packaging and exert more pressure on the walls of the ore pass, hindering the flow.

Note that the difference of velocities for the particle size range from 9.5mm to 4.8mm in results was smaller, due to the better response to the flow of gravel 0 ( $D/d=16.78$ ) in the actual situation, allowing a closer numerical simulation.

## 5 Conclusions

Table 2 shows the results obtained in different simulations compared to the physical model reproduced. Note that you as the  $D/d$  decreases, the adherence of the numerical model increases.

**Table 2** Comparison and results between models

<b>Type</b>	Gravel 2	Gravel 1	Gravel 0
<b>Size range (mm)</b>	25 to 19	19 to 9.5	9.5 to 4.8
<b>D/d</b>	4.8	6.3	12.6
<b>Mean flow velocity (physical model)</b>	-	20.73	28.55
<b>Mean flow velocity (DEM model)</b>	-	23.63	27.55
<b>Relative difference (%)</b>	-	12.3%	-3.6%

The numerical reproduction of the experimental model was satisfactory because it allowed evaluate the sensitivity of granular flow friction both between particles and between particles and wall. The sphericity was also a point of discussion as it is an obstacle to be overcome for conducting a close simulation of the real phenomenon, once the sphericity of the crushed gneiss was not measured. Finally, the numerical model makes room for further analysis of the sensitivity of other variables such as the state of stress and deformability in granular media.

## Acknowledgments

Special thanks to Dr. José M. Silva, for providing the data of your thesis, as well as assist in the preparation of the paper, and for the support from Federal University of Ouro Preto, in association with the Vale Institute of Technology.

## References

[1] BALEVIČIUS, R. et al. Discrete-particle investigation of friction effect in filling and unsteady/steady discharge in three-dimensional wedge-shaped hopper. *Powder Technology*, v. 187, n. 2, p. 159-174, 2008.

- [2] BALEVIČIUS, R. et al. Analysis and DEM simulation of granular material flow patterns in hopper models of different shapes. *Advanced Powder Technology*, v. 22, n. 2, p. 226-235, 2011.
- [3] CAPRIZ, G. et al. *Mathematical Models of Granular Matter*. Springer. 2008. 212 p.
- [4] CLEARY, P. W.; SAWLEY, M. L. DEM modelling of industrial granular flows: 3D case studies and the effect of particle shape on hopper discharge. *Applied Mathematical Modelling*, v. 26, n. 2, p. 89-111, Feb 2002.
- [5] COETZEE, C. J.; ELS, D. N. J. Calibration of discrete element parameters and the modelling of silo discharge and bucket filling. *Computers and Electronics in Agriculture*, v. 65, n. 2, p. 198-212, 2009.
- [6] COETZEE, C. J.; ELS, D. N. J.; DYMOND, G. F. Discrete element parameter calibration and the modelling of dragline bucket filling. *Journal of Terramechanics*, v. 47, n. 1, p. 33-44, 2010.
- [7] GÖNCÜ, F. *Mechanics of Granular Materials: Constitutive Behavior and Pattern Transformation*. PhD Thesis. Delft University of Technology – Delft Center for Computational Science and Engineering – DCSE. 2012.
- [8] HILL, J. M.; SELVADURAI, A. P. S. *Mathematics and Mechanics of Granular Materials*. Springer. 2005. 324 p.
- [9] ITASCA CONSULTING GROUP. PFC2D – Particle Flow Code in 2D dimensions. Version 4.0 – 32 bit. 2008.
- [10] MISHRA, B. K.; THORNTON, C. An improved contact model for ball mill simulation by the discrete element method. *Advanced Powder Technology*, v. 13, n. 1, p. 25-41, 2002.
- [11] NEDDERMAN, R. M. *Statics and Kinematics of Granular Materials*. Cambridge University Press. 2005. 372 p.

[12] NEVES, C. E. V. Comportamento de materiais granulares usando o método dos elementos discretos. 2009. 166 p. Dissertação (Mestrado em Geotecnia) – Universidade de Brasília – UnB, Brasília, 2009.

[13] SILVA, J. M. Estudo do fluxo de material fragmentado na mineração subterrânea, com uso de modelos físicos. Tese de doutorado. Universidade Federal de Minas Gerais – UFMG. 2005.

[14] SILVA, J. M.; GRIPP, M. F. A. Fluxo de material fragmentado em passagem de minério nas minas subterrâneas: a prática corrente. Rem: Rev. Esc. Minas, Ouro Preto, v. 59, n. 3, Sep 2006.

## Appendix A: Source code of simulation (gravel 2)

```
new
set random
title 'Estudo de fluxo/forças'
DEF create_hopper
  command
    wall id=1 kn=1e8 ks=1e8 friction=0.7 nodes (0,0) (120,0)
    wall id=2 kn=1e8 ks=1e8 friction=0.7 nodes (120,0) (635.615,1931.8587)
    wall id=3 kn=1e8 ks=1e8 friction=0.7 nodes (515.615,1931.8587) (0,0)
    plot wall black
  end_command
END
DEF create_balls
  command
    gen id 1 120 rad 19 25 x 525.615 625.615 y 1931.8587 7000
  end_command
END
DEF acomodate_balls
  command
    wall id=4 kn=1e8 ks=1e8 nodes (635.615,1931.8587) (635.615,7000)
    wall id=5 kn=1e8 ks=1e8 nodes (515.615,7000) (515.615,1931.8587)
    prop kn 1e8 ks 1e8 friction=0.7 dens 1000
    hist id 1 diagnostic muf
    solve
    cycle 30000
    del ball range y 1930 10000
    Delete wall 4
    Delete wall 5
  end_command
END
DEF diferenciate_balls
  Command
    prop color 1
    prop color 0 range y 250 500
    prop color 0 range y 750 1000
    prop color 0 range y 1250 1500
    prop color 0 range y 1750 2000
  end_command
END
DEF create-_hist_vel
```

```

        command
            his nstep 50
            his id 10 ball yvelocity 60,0
            his id 11 ball yvelocity 111.561,193.239
            his id 12 ball yvelocity 163.123,386.479
            his id 13 ball yvelocity 214.684,579.718
            his id 14 ball yvelocity 266.246,772.957
            his id 15 ball yvelocity 317.807,966.196
            his id 16 ball yvelocity 369.369,1159.436
            his id 17 ball yvelocity 420.930,1352.675
            his id 18 ball yvelocity 472.492,1545.914
            his id 19 ball yvelocity 524.053,1739.153
            his id 20 ball yvelocity 575.615,1925.000
        end_command
    END
    DEF hist_vel
        command
            plot hist 10 11 12 13 14 15 16 17 18 19 20
        end_command
    END
    DEF monitor
        whilestepping
            skip = skip + 1
            if skip < 100
                exit
            endif
            skip = 0
            bp_ = ball_head
            loop while bp_ # null; escaneia todas as bolas
                bnext = b_next(bp_)
                if b_y(bp_) < -50.0; deleta as bolas
                    ii=b_delete(bp_)
                endif
                bp_ = bnext
            endloop
            bnext = null
            bp_ = null
        END
; create plot
create_hopper
plot set back White
SET grav 0.0 -9.81
create_balls
plot add ball yellow
SET disk on ;
acomodate_balls
diferenciate_balls
plot add cforce black blue
plot add axes brown
plot set title text 'Silo'
plot add vel
delete wall 1
create~_hist_vel
cycle 10000
solve

```

## Appendix B: Source code of simulation (gravel 1)

```

new
set random
title 'Estudo de fluxo/forças'
DEF create_hopper

```

```

        command
            wall id=1 kn=1e8 ks=1e8 friction=0.7 nodes (0,0) (120,0)
            wall id=2 kn=1e8 ks=1e8 friction=0.7 nodes (120,0) (635.615,1931.8587)
            wall id=3 kn=1e8 ks=1e8 friction=0.7 nodes (515.615,1931.8587) (0,0)
            plot wall black
        end_command
END
DEF create_balls
    command
        gen id 1 300 rad 9.5 19 x 515.615 635.615 y 1931.8587 7000
    end_command
END
DEF acomodate_balls
    command
        wall id=4 kn=1e8 ks=1e8 nodes (635.615,1931.8587) (635.615,7000)
        wall id=5 kn=1e8 ks=1e8 nodes (515.615,7000) (515.615,1931.8587)
        hist id 1 diagnostic muf
        prop kn 1e8 ks 1e8 friction=0.7 dens 1000
        solve
        cycle 10000
        del ball range y 1930 10000
        Delete wall 4
        Delete wall 5
    end_command
END
DEF diferenciate_balls
    Command
        prop color 1
        prop color 0 range y 250 500
        prop color 0 range y 750 1000
        prop color 0 range y 1250 1500
        prop color 0 range y 1750 2000
    end_command
END
DEF create-_hist_vel
    command
        his nstep 50
        his id 10 ball yvelocity 60,0
        his id 11 ball yvelocity 111.561,193.239
        his id 12 ball yvelocity 163.123,386.479
        his id 13 ball yvelocity 214.684,579.718
        his id 14 ball yvelocity 266.246,772.957
        his id 15 ball yvelocity 317.807,966.196
        his id 16 ball yvelocity 369.369,1159.436
        his id 17 ball yvelocity 420.930,1352.675
        his id 18 ball yvelocity 472.492,1545.914
        his id 19 ball yvelocity 524.053,1739.153
        his id 20 ball yvelocity 575.615,1925.000
    end_command
END
DEF hist_vel
    command
        plot hist 10 11 12 13 14 15 16 17 18 19 20; o principal e lembrar o id alocado
    end_command
END
DEF hist_fdes
    command
        plot hist 1
    end_command
END
DEF monitor
    whilestepping
        skip = skip + 1
        if skip < 100

```

```

        exit
    endif
    skip = 0
    bp_ = ball_head
    loop while bp_ # null
        bnext = b_next(bp_)
        if b_y(bp_) < -50.0
            ii=b_delete(bp_)
        endif
        bp_ = bnext
    endloop
    bnext = null
    bp_ = null
END

```

```

; create plot
create_hopper
plot set back White
SET grav 0.0 -9.81
create_balls
plot add ball yellow
SET disk on
acomodate_balls
diferenciate_balls
plot add cforce black blue
plot add axes brown
plot set title text 'Silo'
plot add vel
delete wall 1
create-_hist_vel
monitor

cycle 17000

```

## Appendix C: Source code of simulation (gravel 0)

```

new
set random
title 'Estudo de fluxo/forças'
DEF create_hopper
    command
        wall id=1 kn=1e8 ks=1e8 friction=0.7 nodes (0,0) (120,0)
        wall id=2 kn=1e8 ks=1e8 friction=0.7 nodes (120,0) (635.615,1931.8587)
        wall id=3 kn=1e8 ks=1e8 friction=0.7 nodes (515.615,1931.8587) (0,0)
        plot wall black
    end_command
END
DEF create_balls
    command
        gen id 1 400 rad 4.8 19 x 515.615 635.615 y 1931.8587 7000
    end_command
END
DEF acomodate_balls
    command
        wall id=4 kn=1e8 ks=1e8 nodes (635.615,1931.8587) (635.615,7000)
        wall id=5 kn=1e8 ks=1e8 nodes (515.615,7000) (515.615,1931.8587)
        hist id 1 diagnostic muf
        prop kn 1e8 ks 1e8 friction=0.7 dens 1000
        solve
        cycle 10000
        del ball range y 1930 10000
        Delete wall 4
    end_command
END

```

```

        Delete wall 5
    end_command
END
DEF diferenciate_balls
    Command
        prop color 1
        prop color 0 range y 250 500
        prop color 0 range y 750 1000
        prop color 0 range y 1250 1500
        prop color 0 range y 1750 2000
    end_command
END
DEF create~_hist_vel
    command
        his nstep 50
        his id 10 ball yvelocity 60,0
        his id 11 ball yvelocity 111.561,193.239
        his id 12 ball yvelocity 163.123,386.479
        his id 13 ball yvelocity 214.684,579.718
        his id 14 ball yvelocity 266.246,772.957
        his id 15 ball yvelocity 317.807,966.196
        his id 16 ball yvelocity 369.369,1159.436
        his id 17 ball yvelocity 420.930,1352.675
        his id 18 ball yvelocity 472.492,1545.914
        his id 19 ball yvelocity 524.053,1739.153
        his id 20 ball yvelocity 575.615,1925.000
    end_command
END
DEF hist_vel
    command
        plot hist 10 11 12 13 14 15 16 17 18 19 20; o principal e lembrar o id alocado
    end_command
END
DEF hist_fdes
    command
        plot hist 1
    end_command
END
DEF monitor
    whilestepping
        skip = skip + 1
        if skip < 100
            exit
        endif
        skip = 0
        bp_ = ball_head
        loop while bp_ # null
            bnext = b_next(bp_)
            if b_y(bp_) < -50.0
                ii=b_delete(bp_)
            endif
            bp_ = bnext
        endloop
        bnext = null
        bp_ = null
END

; create plot
create_hopper
plot set back White
SET grav 0.0 -9.81
create_balls
plot add ball yellow
SET disk on

```

```
acomodate_balls
diferenciate_balls
plot add cforce black blue
plot add axes brown
plot set title text 'Silo'
plot add vel
delete wall 1
create-_hist_vel
monitor
cycle 30000
```