

1                   Cold-Spray Repair of Corroded Steel Bridge Girders via an  
2                   Optimization-Driven Cyber-Physical Workflow and Robotic Deposition  
3                   Architecture

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12                   **Abstract**

13                   Corrosion-induced material loss in steel bridge poses persistent persistent challenges for inspection, load  
14                   rating, and rehabilitation, often leading to conservative decisions and labor-intensive repair strategies. This  
15                   paper presents a cyber-physical workflow for optimized repair design and a robotic cold-spray deposition  
16                   architecture targeting corroded steel bridge girders. The framework integrates laser scanning, corrosion  
17                   mapping, nonlinear finite element analysis, and gradient-based optimization to generate material-efficient  
18                   cold-spray repair geometries tailored to the as-is condition of deteriorated members. Three-dimensional point  
19                   cloud data are processed into a structured thickness field that captures localized corrosion while remaining  
20                   computationally efficient for iterative optimization. Using this representation, spatially varying cold-spray  
21                   deposition thickness fields are determined to maximize load-carrying capacity recovery while minimizing  
22                   added material. Both Pareto-based and penalty-based optimization formulations are explored, enabling  
23                   efficiency-driven trade-off analysis or direct targeting of prescribed capacity levels. The computational  
24                   framework is validated against full-scale experimental testing of a naturally corroded steel girder, demon-  
25                   strating close agreement between predicted and measured structural response. To connect optimized repair  
26                   design with execution, a robotic cold-spray deposition architecture and a dedicated slicing strategy are intro-  
27                   duced, together with a virtual environment for simulating deposition kinematics and process constraints. The  
28                   proposed workflow establishes an integrated, data-driven pathway toward automated, performance-informed  
29                   cold-spray repair of steel bridge infrastructure.

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31 **1. Introduction**

32 Corrosion is a complex, multi-physics degradation process governed by electrochemical reactions, en-  
33 vironmental exposure, and material heterogeneity, resulting in highly nonuniform and evolving patterns of  
34 material loss. In steel structural systems, this process manifests as spatially irregular section reduction that  
35 is strongly influenced by local geometry, detailing, and exposure conditions. For steel bridges, corrosion  
36 frequently localizes at beam ends, web-flange junctions, and other moisture-retaining regions. Even modest  
37 material loss can have disproportionate effects on stiffness, load path redistribution, and local or global  
38 stability phenomena [1, 2, 3, 4]. Experimental and numerical studies have shown that such localized de-  
39 terioration can govern failure modes and residual capacity even when overall section loss appears limited  
40 [5, 6, 7]. Despite this inherent geometric and mechanical complexity, corrosion is commonly represented in  
41 engineering practice using simplified or idealized descriptions that inadequately capture its spatial variability.  
42 This disconnect between the physical manifestation of corrosion and its engineering representation prop-  
43 agates uncertainty throughout inspection, load rating, and repair decision-making, often leading to overly  
44 conservative assumptions and interventions.

45 Current repair practices for corroded steel girders are well established but remain costly and labor-  
46 intensive. Conventional rehabilitation typically involves localized reinforcement through welded steel plates  
47 [8] or bolted steel sections [9], requiring extensive surface preparation, skilled labor, and prolonged traffic  
48 disruptions. Alternative approaches, such as carbon fiber-reinforced polymers (CFRP), have demonstrated  
49 effectiveness in restoring capacity while reducing added weight [5, 10], but raise concerns related to durability,  
50 fire resistance, and long-term performance under harsh environmental exposure. Other strategies include  
51 welded stiffeners or studs embedded in grout or resin systems [11, 6], as well as partial or full encasement  
52 of deteriorated regions using ultrahigh-performance concrete (UHPC) [12]. UHPC-based repairs have  
53 shown promising mechanical performance through push-out testing [13, 14] and durability under accelerated  
54 electrochemical corrosion [15], with recent efforts moving toward field implementation [16]. Despite their  
55 effectiveness, these repair methods are typically solutions that apply uniform strengthening measures over  
56 large regions, offering limited adaptability to the highly localized and irregular nature of corrosion damage.

57 As a result, repairs are often conservative, material-intensive, and difficult to tailor to the actual structural  
58 demand, highlighting the need for more flexible, data-informed, and mechanically efficient rehabilitation  
59 strategies.

60 Additive manufacturing (AM) technologies open new opportunities for structural repair by enabling  
61 spatially resolved material placement that can be directly informed by mechanics, damage state, and perfor-  
62 mance objectives. From a structural standpoint, AM allows reinforcement to be distributed non-uniformly  
63 and applied only where it contributes meaningfully to stiffness recovery, load redistribution, or delay of local  
64 instability mechanisms, rather than relying on discrete or uniform strengthening measures. AM therefore  
65 enables the integration of structural analysis and optimization with fabrication, supporting material-efficient  
66 repair strategies.

67 Among AM approaches, wire arc additive manufacturing (WAAM) and related directed energy deposition  
68 (DED) processes have demonstrated scalability for large steel components and have been shown to produce  
69 structural steels with favorable mechanical performance and controlled microstructures [17, 18, 19]. However,  
70 the reliance of these processes on localized melting and solidification introduces significant thermal input,  
71 residual stresses, and metallurgical transformations that can complicate on-site repair. In contrast, cold-spray  
72 additive manufacturing (CSAM) has emerged as a particularly promising alternative for infrastructure repair  
73 due to its solid-state deposition mechanism, in which high-velocity particles plastically deform and bond  
74 to the substrate without bulk melting [20, 21, 22]. Bonding in cold spray is generally attributed to severe  
75 plastic deformation, adiabatic shear instability, and localized interfacial mixing, enabling strong adhesion  
76 while largely preserving the base-metal microstructure and minimizing thermal distortion [23, 24]. Cold  
77 spray has been explored for repairing damaged steel components and localized section loss [25], although  
78 its structural application at bridge-relevant scales remains an active area of research, with ongoing efforts  
79 needed to better characterize interface behavior, mechanical performance, and long-term durability under  
80 realistic loading and environmental conditions. In this context, cold spray may be a compelling platform for  
81 mechanically informed, data-driven repair strategies.

82 The potential effectiveness such repair strategies is inherently tied to the quality and resolution of in-  
83 spection data. Traditional inspection practices for steel bridges rely heavily on visual assessment, isolated  
84 thickness measurements, and qualitative documentation, which fail to capture the spatial randomness and

85 severity of corrosion. In contrast, emerging sensing technologies such as 3D laser scanning, photogramme-  
86 try, and image-based reconstruction enable high-resolution mapping of surface geometry and deterioration  
87 patterns [26, 27, 28, 29]. These techniques have been successfully applied to damage detection [30, 31, 32]  
88 and quantitative assessment of corrosion in steel components [33, 4, 7]. Prior work by the authors has  
89 demonstrated that detailed corrosion morphology derived from 3D scans can be integrated directly into  
90 computational models for accurate capacity prediction of corroded steel girders [34]. Such data-rich repre-  
91 sentations provide the necessary geometric foundation for optimization-driven and additive repair strategies.

92 Building on these advances, this work presents a unified cyber–physical workflow tailored to cold-  
93 spray–based repair of corroded steel bridge girders, as schematically illustrated in Fig. 1. The framework  
94 integrates corrosion mapping by high-resolution laser-scanning with nonlinear finite element analysis and  
95 gradient-based optimization to determine spatially varying cold-spray deposition fields that efficiently restore  
96 structural capacity while minimizing added material. To enable translation from optimized repair design to  
97 execution, the study introduces a robotic cold-spray deposition architecture and an associated slicing and path-  
98 planning strategy that convert thickness fields into machine-interpretable trajectories. A virtual twin of the  
99 deposition system is developed to simulate kinematics, stand-off control, and process sequencing. Material  
100 behavior used in the computational framework is informed by experimental testing of cold-spray–repaired  
101 steel specimens, while the predicted structural response is validated against full-scale testing of a naturally  
102 corroded girder. Collectively, the proposed methodology establishes an end-to-end, data-driven pathway,  
103 addressing key limitations of conventional repair practice and supporting repeatable, performance-informed  
104 rehabilitation of steel bridge infrastructure.

## 105 **2. Scan-to-Model Corrosion Mapping**

106 Building on scan-to-FEM workflows previously developed and experimentally validated by the authors  
107 for residual capacity prediction of corroded steel girders [34], the present work refines and systematizes  
108 the corrosion representation to support gradient-based topology optimization. The key requirement for  
109 the subsequent design stage is a corrosion description that is (i) accurate to the measured deterioration,  
110 (ii) computationally efficient for repeated finite element analyses, and (iii) expressed in a parameterized  
111 form suitable for automated material-volume estimation, sensitivity analysis, and downstream fabrication

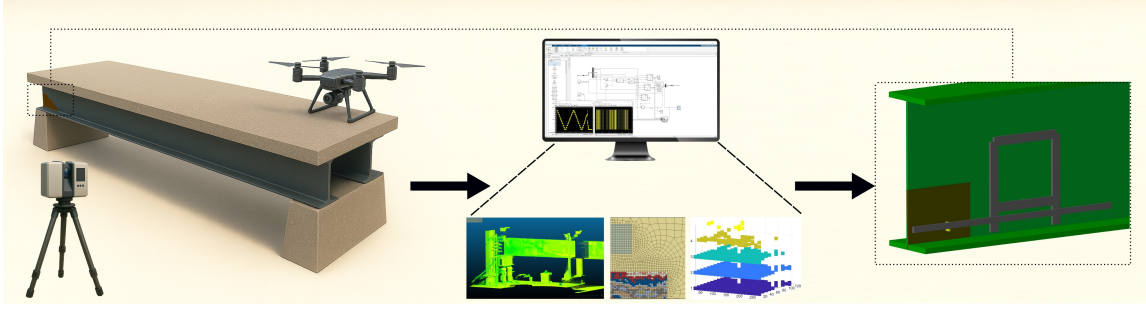


Figure 1: Overview of the proposed cyber-physical workflow for cold-spray repair of corroded steel bridge girders. High-resolution point cloud data are processed to derive spatially resolved web-thickness fields, which inform nonlinear finite element analysis and gradient-based optimization. The resulting optimized deposition fields are translated into executable trajectories for automated cold-spray repair.

112 planning. To meet these requirements, the contour-based thickness representation in [34] is reformulated  
 113 into a structured, block-wise thickness field.

114 Point cloud data in this study were acquired on a 24CB120 beam under laboratory conditions using a  
 115 RIEGL VZ-2000 LiDAR scanner [35]. The proposed algorithmic framework is not tied to specific hardware  
 116 and can be applied to other terrestrial, portable, or drone-mounted scanners, provided that the resulting point  
 117 clouds satisfy the accuracy and precision needed to capture local section-loss features relevant to capacity  
 118 and stability. The processing pipeline from raw point cloud to thickness field is fully scripted, enabling  
 119 deployment within automated inspection-to-repair workflows.

### 120 2.1. Converting scan data to an optimization-ready thickness field

121 Previous research by the authors demonstrated that scan-derived contour maps can represent corrosion  
 122 profiles with high fidelity and support accurate computational prediction of residual capacity [34]. While  
 123 well-suited for detailed assessment and one-off analyses, purely contour-based geometries are less compatible  
 124 with automated, iterative optimization frameworks. Specifically, (i) variable element sizes and irregular  
 125 partitions complicate automated estimation of deposited material volume, (ii) the large number of partitions  
 126 required to represent complex corrosion surfaces increases model generation time, and (iii) the resulting  
 127 model complexity limits scalability for repeated analyses.

128 To address these limitations, a structured grid-based representation is introduced to describe the remaining  
 129 web thickness field in a form suitable for optimization. Unlike the contour-based description shown in

130 Fig. 2a, which preserves the full geometric fidelity of the corrosion morphology through irregular, free-  
 131 form boundaries, the structured grid representation in Fig. 2b discretizes the same corrosion field into a  
 132 finite number of rectangular blocks with uniform in-plane dimensions. Each block is assigned a single  
 133 representative thickness value, transforming the continuous corrosion morphology into a piecewise-constant  
 134 field that is computationally tractable and directly compatible with optimization algorithms.

135 Prior experimental and numerical investigations by the authors determined that the lower part of the web  
 136 governs the load-carrying capacity and failure behavior of corroded girder ends [1, 2]. Accordingly, only this  
 137 region is discretized using the structured grid, while the remainder of the web is assumed to retain uniform  
 138 nominal thickness. This targeted discretization significantly reduces model size and computational cost  
 139 while preserving the structural fidelity required for capacity prediction. The validity of this representation is  
 140 assessed through comparison with full-scale experimental results reported previously by the authors [34].

141 To examine sensitivity to grid resolution, the corrosion domain ( $19\text{ cm} \times 40.6\text{ cm}$ ) is discretized using two  
 142 configurations: 576 blocks ( $18 \times 32$ ) and 2,368 blocks ( $37 \times 64$ ). The remaining thickness is quantized into  
 143 10 and 12 discrete thickness levels for the coarse and fine grids, respectively (Fig. 2c–d). This discretized  
 144 field constitutes a compact, machine-readable state variable that can be directly coupled with topology  
 145 optimization and fabrication path planning.

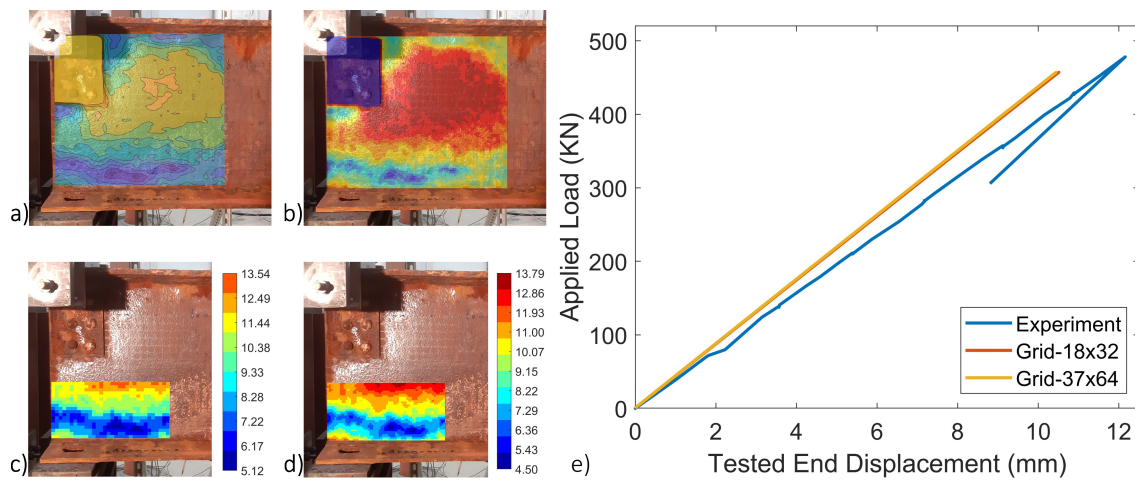


Figure 2: Corrosion mapping and experimental validation for a 24CB120 beam end. (a) Remaining web thickness represented using contour-based interpolation of 3D scan data. (b) Structured grid representation of the same corrosion profile. For computational efficiency, only the governing lower portion of the web is considered in the capacity evaluation, with a (c) coarse and (d) dense mesh being evaluated. (e) Comparison of experimental and numerical load–displacement responses for coarse and fine grid resolutions.

146 *2.2. Experimental benchmark and numerical validation*

147 A full-scale destructive test previously performed by the authors on a 24CB120 beam with the corrosion  
148 pattern shown in Fig. 2 is used as the benchmark for validating the proposed corrosion representation [34].  
149 For completeness, the experimental configuration is illustrated in Fig. 3b. The specimen is simply supported,  
150 and the load is applied upward using two hydraulic jacks positioned beneath the tested end. A crossbeam  
151 anchored to the strong floor is placed 1.2 m from the tested end to restrain vertical movement. Out-of-plane  
152 displacement of the top flange is restricted using lateral braces to suppress lateral–torsional buckling. The  
153 reaction force at the tested end is measured using three load cells (1x445 kN, 2x890 kN by Omega), and the  
154 corresponding deflection is recorded with a cable extension position transducer (Calesco PT101). The exact  
155 technical specifications of the implemented equipment are given in [34, 1].

156 For validation and for automated integration into the optimization framework, the scan-derived grid  
157 representation is embedded into a three-dimensional finite element model using Abaqus. The algorithmic  
158 pipeline developed in [34] is adapted to use the structured grid in place of contour maps. A MATLAB script  
159 extracts grid-line coordinates and generates the thickness map corresponding to Fig. 2b–d, while a Python  
160 script is used to partition the web surface data and assigns the associated thickness values automatically to  
161 the finite element model.

162 The girder is modeled using four-node linear S4R shell elements with a midsurface approximation,  
163 consistent with the slender web and flange geometry [34, 3, 2]. A mesh size up to 6.5 cm is used away from  
164 the corroded end, while one element is assigned to each rectangular block within the corrosion domain to  
165 preserve the imposed thickness field. Boundary conditions, loading, and material properties are defined to  
166 replicate the experimental configuration, with mechanical properties obtained from tensile testing of coupons  
167 extracted from the web and flanges, as reported in [34].

168 Figure 2d compares the experimentally measured load–displacement response to finite element predic-  
169 tions obtained using the two grid resolutions. The ultimate capacity is predicted as 456.7 kN and 457.0 kN  
170 for the coarse and fine grids, respectively, in close agreement with the experimentally measured capacity  
171 of 478 kN (discrepancy of  $-4.4\%$ ). The similarity of the coarse- and fine-grid predictions indicates that  
172 the coarse grid retains the governing corrosion features relevant to capacity and stability, while offering  
173 substantially improved computational efficiency. Accordingly, the coarse-grid representation is adopted in

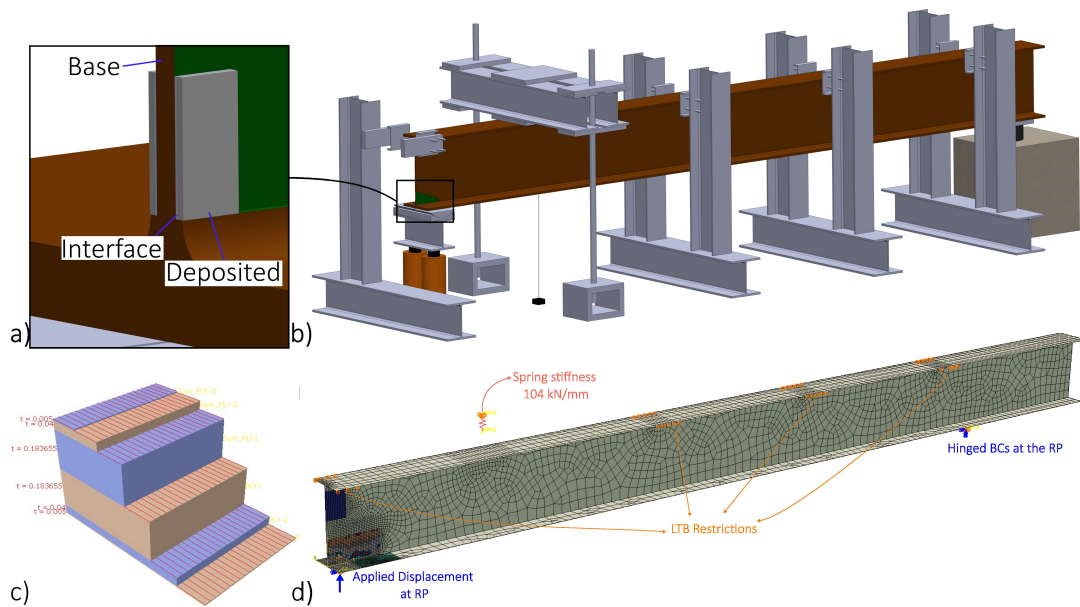


Figure 3: Repair strategy, experimental setup, and finite element model. Schematic of (a) the repair strategy where the added material is shown as a simplified rectangle of constant thickness and (b) the full-scale experimental test setup, showing the simply supported girder, applied vertical loading at the corroded end, and restraint provided by the strong floor. (c) Finite element representation of the three-layer composite shell model, including the base, interface, and additive layers applied symmetrically on both web surfaces. (d) Boundary and loading conditions used in the numerical simulations for the optimization studies.

174 the subsequent optimization studies.

### 175 3. Computational Optimization Framework for Additive Repair Design

176 Cold-spray additive manufacturing enables the controlled deposition of metallic particles to form a dense,  
 177 monolithic layer on a steel substrate, allowing corrosion-induced material loss to be rebuilt in a spatially  
 178 resolved manner. From a structural mechanics perspective, this capability creates a direct pathway for  
 179 restoring load-carrying capacity toward the pre-corroded (intact) condition of steel bridge components, rather  
 180 than relying on conservative, uniform strengthening measures. By selectively adding material where stiffness,  
 181 load-path continuity, or local stability have been compromised, cold spray repairs can recover structural  
 182 performance while minimizing unnecessary intervention. The free-form nature of additive deposition enables  
 183 reinforcement layouts that are tailored to the underlying mechanics of deterioration. This design freedom opens  
 184 the door to optimization-driven repair strategies, in which material placement and thickness distribution are

185 determined systematically to maximize capacity recovery and efficiency. To exploit this potential in a rigorous  
186 and automated manner, an optimization-based computational framework is formulated to determine where  
187 and how much material should be deposited to restore structural performance with minimal added material.  
188 Within the broader cyber-physical workflow introduced in this paper, the optimization module serves as  
189 the decision-making engine that translates scan-derived deterioration data into executable, material-efficient  
190 cold-spray repair designs.

191 The optimization problem seeks to determine the additional thickness field

$$\mathbf{t} = [t_1, t_2, \dots, t_N]^T, \quad (1)$$

192 applied symmetrically on both sides of the corroded web. Owing to the structured grid representation, each  
193 block  $i$  within the optimization domain has an identical in-plane area  $A$ , resulting in a fixed design space  
194 with a direct one-to-one correspondence between grid blocks and design variables. Consistent with the  
195 mid-surface shell formulation adopted in the finite element model, the geometry and loading are assumed  
196 to be symmetric about the web mid-plane, which reflects both the physical repair strategy and facilitates  
197 automated fabrication.

198 When a grid block is reinforced through cold-spray deposition, the repaired region is represented using  
199 a three-layer composite section (Fig. 3a), defined as:

- 200 i) **Base material layer**, representing the as-scanned remaining web thickness.
- 201 ii) **Interface layer**, a 1 mm transition zone with material properties representative of the bond region  
202 between the base metal and the deposited material, applied symmetrically on both sides.
- 203 iii) **Additive layer**, corresponding to the deposited cold-spray material and defined by the optimization  
204 variables  $t_i$ , applied symmetrically on both sides.

205 This layered representation provides a physically informed yet computationally tractable description of the  
206 repaired cross-section, allowing the mechanical contribution of the deposited material and the interface to  
207 be explicitly captured within the optimization loop.

208 To inform the layerwise properties to be incorporated in the model, mechanical tests were conducted on

209 reference specimens and specimens with cold spray deposits. Tests followed ASTM E9 using an Instron  
 210 5569 frame at a quasi-static nominal strain rate of  $2 \times 10^{-4} \text{ s}^{-1}$ . A non-contact AVE2 laser extensometer,  
 211 with a displacement resolution of  $0.5 \mu\text{m}$ , was used to track axial strains,  $\varepsilon$ , via fiducial dots placed on  
 212 opposing specimen faces to minimize grip compliance effects. Three specimen families were tested: (i) pure  
 213 A36 pillars, (ii) pure cold-spray pillars (SS0X), and (iii) composite pillars comprising cold-spray material  
 214 deposited on A36 with equivalent thickness. This test matrix enabled direct comparison of the  $\sigma$ - $\varepsilon$  response  
 215 across the different material systems.

216 The stress-strain curves shown in Fig. 4 distinguish the mechanical responses of pure A36 (black),  
 217 composite A36-SS0X (blue), and pure SS0X (orange) pillars fabricated using SS08 powder. Markers  
 218 indicate the yield stress,  $\sigma_y$  (rectangles), and the ultimate stress,  $\sigma_u$  (triangles). The A36 response exhibits  
 219 the expected initial linear elastic regime up to  $\sigma_y$ , followed by stable plastic flow with pronounced strain  
 220 hardening over a broad strain range (plotted up to 20% strain). For A36, the measured  $\sigma_y = 313 \pm 12 \text{ MPa}$  and  
 221 elastic modulus  $E = 211 \pm 13 \text{ GPa}$  establish the baseline stiffness and strength against which the composite  
 222 response is evaluated.

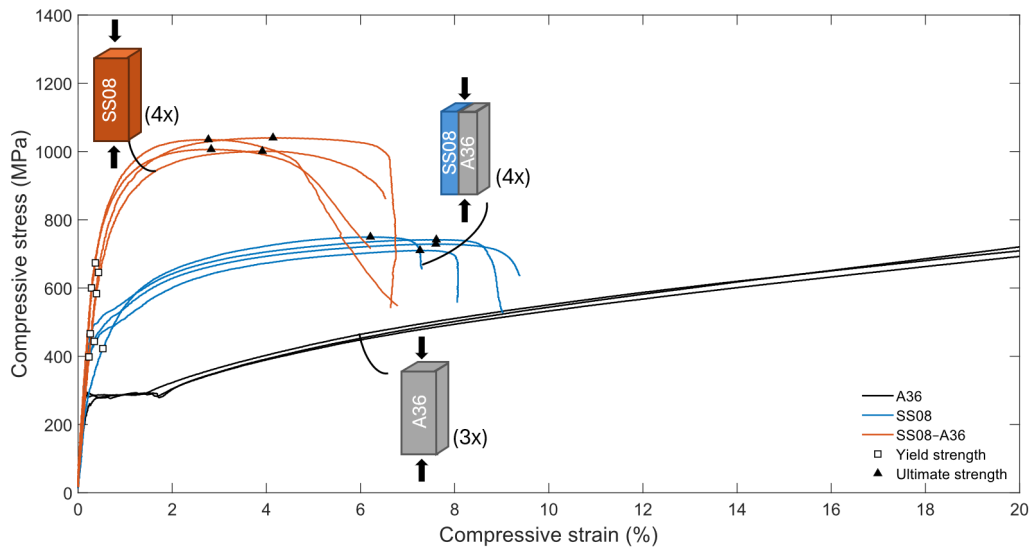


Figure 4: Stress-strain response of pillar specimens under uniaxial compression: (i) pure A36 specimens (black), (ii) composite SS0X-A36 specimens (blue), and (iii) pure SS0X specimens (orange).

223 Two complementary optimization strategies are investigated to address distinct repair design objectives

224 commonly encountered in bridge engineering practice and to support automated, repeatable decision-making.  
 225 The first strategy employs a Pareto-based formulation to explicitly quantify the trade-off between added ma-  
 226 terial volume and recovered structural capacity. This formulation enables systematic exploration of multiple  
 227 admissible repair solutions and quantifies how local material deposition influences global performance. Such  
 228 information is particularly valuable during preliminary assessment and option screening, where agencies of-  
 229 ten seek to understand efficiency trends, diminishing returns, and the structural consequences of alternative  
 230 intervention levels before committing to a specific repair strategy.

231 The second strategy adopts a penalty-based formulation that targets restoration to a prescribed capacity  
 232 level consistent with load-rating and serviceability objectives defined in AASHTO and MassDOT bridge  
 233 evaluation procedures. In this case, the optimization enforces a direct performance requirement, such as  
 234 recovery of the nominal pre-corrosion capacity, while minimizing the amount of deposited material. This  
 235 approach mirrors current practice in which repairs are designed to meet explicit capacity thresholds, but  
 236 does so within an automated, mechanics-based framework that replaces manual sizing and conservative  
 237 assumptions with data-driven thickness allocation. Together, the two formulations enable both exploratory  
 238 and target-driven repair design within a unified computational workflow, demonstrating how cold-spray  
 239 additive manufacturing can be systematically integrated into automated bridge assessment and rehabilitation  
 240 processes.

### 241 3.1. Pareto-Based Multi-Objective Optimization

242 The total added material volume and the corresponding gain in load-carrying capacity are defined as

$$V(\mathbf{t}) = 2 \sum_{i=1}^N A t_i, \quad L(\mathbf{t}) = \text{Cap}(\mathbf{t}) - \text{Cap}(0), \quad (2)$$

243 where  $\text{Cap}(\mathbf{t})$  denotes the global structural capacity associated with a reinforcement field  $\mathbf{t}$ , defined as the  
 244 peak reaction force in the nonlinear load–displacement response of the finite element model. The factor of  
 245 two accounts for symmetric deposition on both sides of the web. Based on these definitions, the optimization  
 246 objective function is expressed as

$$\Phi(\mathbf{t}) = a \frac{V(\mathbf{t})}{V_{\text{scale}}} - (1 - a) \frac{L(\mathbf{t})}{L_{\text{scale}}}, \quad a \in [0, 1], \quad (3)$$

247 where  $V_{\text{scale}}$  and  $L_{\text{scale}}$  are normalization factors chosen such that both terms have comparable magnitude. The  
 248 weighting parameter  $a \in [0, 1]$  controls the relative importance between material efficiency and structural  
 249 performance. A value of  $a = 1$  drives the optimization toward minimum added volume, whereas  $a = 0$   
 250 emphasizes maximum capacity recovery. Intermediate values generate the Pareto front, capturing the trade-  
 251 off between competing objectives.

252 The optimization follows a steepest descent scheme, where the descent direction is given by

$$\mathbf{d}_k = -\nabla\Phi(\mathbf{t}_k), \quad (4)$$

253 and the design variables are updated according to

$$\mathbf{t}_{k+1} = (\mathbf{t}_k + \eta\mathbf{d}_k), \quad (5)$$

254 with  $\eta$  denoting the step size, taken as a constant value of 0.6. This choice was found to be adequate  
 255 given the computational cost of nonlinear finite element evaluations and the numerical noise associated with  
 256 finite-difference sensitivity calculations. The use of a small, fixed step size ensures stable descent without  
 257 the need for line-search procedures.

258 The total gradient of the objective function is given by

$$\nabla\Phi(\mathbf{t}) = \frac{a}{V_{\text{scale}}}\nabla V(\mathbf{t}) - \frac{(1-a)}{L_{\text{scale}}}\nabla L(\mathbf{t}), \quad (6)$$

259 with

$$\nabla V(\mathbf{t}) = 2A, \quad \nabla L(\mathbf{t}) = \left[ \frac{\partial \text{Cap}(\mathbf{t})}{\partial t_1}, \dots, \frac{\partial \text{Cap}(\mathbf{t})}{\partial t_N} \right]^T. \quad (7)$$

260 The capacity sensitivities are approximated using forward finite differences,

$$\frac{\partial \text{Cap}(\mathbf{t})}{\partial t_i} \approx \frac{\text{Cap}(\mathbf{t} + \Delta t_{\text{side}}) - \text{Cap}(\mathbf{t})}{\Delta t_{\text{side}}}, \quad i = 1, \dots, N, \quad (8)$$

261 where  $\Delta t_{\text{side}}$  denotes the calibrated thickness increment applied symmetrically on both sides of the web.  
 262 Manufacturing and physical feasibility are enforced through the constraints

$$0.25 \text{ mm} \leq t_i \leq 0.5 t_{\text{web}}, \quad i = 1, \dots, N. \quad (9)$$

263 The iterative process is terminated when both

$$\|\mathbf{t}_{k+1} - \mathbf{t}_k\| < \varepsilon_t, \quad \|\nabla \Phi(\mathbf{t}_k)\| < \varepsilon_g, \quad (10)$$

264 are satisfied, with  $\varepsilon_t = 0.006$  and  $\varepsilon_g = 0.02$ .

### 265 3.2. Penalty-Based Optimization for Target Capacity Recovery

266 In bridge rehabilitation applications, repairs are often designed to restore the structure to a prescribed  
 267 target capacity associated with a specific load rating. To reflect this objective, a penalty-based optimization  
 268 problem is formulated to achieve a target capacity  $L_{\text{goal}}$  while minimizing the added material volume.

269 The penalized objective function is defined as

$$\min_{\mathbf{t}} \Phi_{\text{pen}}(\mathbf{t}) = V(\mathbf{t}) + \mu (L_{\text{goal}} - L(\mathbf{t}))^2, \quad V(\mathbf{t}) = 2 \sum_{i=1}^N A t_i, \quad (11)$$

270 where  $\mu$  is the penalty parameter controlling the relative emphasis placed on meeting the prescribed capacity  
 271 target  $L_{\text{goal}}$ .

272 The total gradient of the penalized objective function is expressed as

$$\nabla \Phi_{\text{pen}}(\mathbf{t}) = 2A - 2\mu(L_{\text{goal}} - L(\mathbf{t})) \nabla L(\mathbf{t}), \quad (12)$$

273 where the sensitivity of the recovered capacity with respect to the per-side thickness variable  $t_i$  is approximated  
 274 by

$$\frac{\partial L}{\partial t_i} \approx \frac{L(\mathbf{t} + \Delta t_{\text{side}}) - L(\mathbf{t})}{\Delta t_{\text{side}}}, \quad i = 1, \dots, N. \quad (13)$$

275 Here,  $\Delta t_{\text{side}}$  denotes the predetermined thickness increment applied symmetrically on both sides of the web.  
 276 The optimization proceeds via a projected gradient descent scheme,

$$\mathbf{d}_k = -\nabla\Phi_{\text{pen}}(\mathbf{t}_k), \quad \mathbf{t}_{k+1} = (\mathbf{t}_k + \eta_k \mathbf{d}_k), \quad (14)$$

277 where  $\eta_k$  is the step size, initially set to 0.2 and subsequently adapted based on observed numerical fluctua-  
 278 tions.

279 Convergence is achieved when both the change in the design variables and the gradient norm satisfy

$$\|\mathbf{t}_{k+1} - \mathbf{t}_k\| < \varepsilon_t, \quad \|\nabla\Phi_{\text{pen}}(\mathbf{t}_k)\| < \varepsilon_g. \quad (15)$$

280 Manufacturing and physical feasibility constraints identical to those employed in the Pareto-based for-  
 281 mulation are applied. Specifically, the per-side deposited thickness at each grid block is constrained to  
 282 remain within bounds that reflect both cold-spray process limitations and structural realism. A lower bound  
 283 of 0.25 mm is imposed to represent the minimum reliably achievable deposition thickness per side, below  
 284 which stable layer formation and repeatable material properties cannot be guaranteed. An upper bound of  
 285  $0.5 t_{\text{web}}$  is enforced to prevent excessive local thickening that could introduce unrealistic stiffness gradients,  
 286 numerical instability, or impractical repair geometries relative to the remaining web thickness.

### 287 3.3. Automated Optimization Workflow and Model Updating

288 The optimization framework is implemented through an iterative finite element analysis workflow, as  
 289 illustrated in Fig. 5. Starting from the corroded geometry, the procedure updates the thickness field  $\mathbf{t}$  until  
 290 convergence of both the objective function and the design variables is achieved.

291 At each iteration  $k$ , a set of modified finite element models (“delta files”) is automatically generated.  
 292 Each delta file corresponds to a predetermined thickness increment  $\Delta t$  of 2 mm applied symmetrically to both  
 293 sides of a single element within the optimization domain. These delta files represent localized perturbations  
 294 of the thickness field and can be interpreted as incremental candidate repair actions applied to individual grid  
 295 blocks. If a block has not been previously repaired, an interface layer is introduced symmetrically; otherwise,  
 296 the thickness increment  $\Delta t$  is applied on top of the existing repair layer.

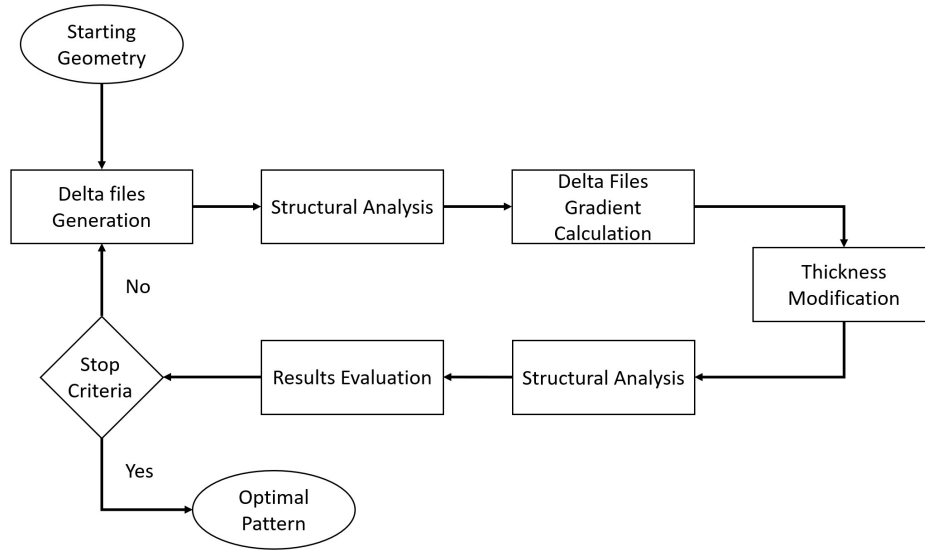


Figure 5: Flowchart of the gradient-based optimization algorithm. For each element, the effect of a predefined local thickness increase is evaluated by finite element analysis. The corresponding gradients are used to iteratively update the thickness field until convergence to the optimal repair pattern.

297 Each modified model is solved to evaluate the structural capacity, defined as the peak reaction force  
 298 developed at the bearing of the corroded end. To enable efficient batch processing, the corresponding reaction  
 299 forces are extracted automatically from the Abaqus output (.dat) files using the algorithmic framework.

300 Once the batch computation of reaction forces for all perturbations is completed, the element-wise  
 301 sensitivities of the objective function are evaluated. The thickness distribution is then updated according to  
 302 the gradient descent rules defined in Eqs. (5) and (14), followed by enforcement of the previously defined  
 303 bound constraints

$$0.25 \text{ mm} \leq t_i \leq 0.5 t_{\text{web}}. \quad (16)$$

304 The updated geometry is reanalyzed and the convergence criteria are checked. If convergence is not satisfied,  
 305 the procedure advances to the next iteration; otherwise, the optimization terminates and the final repair  
 306 pattern is obtained.

### 307 3.4. Finite Element Modeling of Repaired Beam Sections

308 The finite element model described previously is extended to incorporate the additional layers introduced  
309 in the repaired regions. This is achieved through symmetric composite shell section definitions in Abaqus,  
310 where each layer in the stacking sequence is specified by its thickness and corresponding material properties  
311 (Fig. 3c). The base, interface, and additive layers are assigned the experimentally derived constitutive models  
312 shown in Fig. 4b.

313 To reduce computational cost while retaining the governing structural response, the boundary and loading  
314 conditions are slightly simplified relative to the validation model described in [34]. Specifically, the self-  
315 weight of the girder and the weight of the crossbeam present in the experimental setup are omitted. The  
316 applied boundary and loading conditions used in the optimization analyses are shown in Fig. 3d.

317 These simplifications, combined with the structured grid representation of corrosion, result in a substantial  
318 reduction in computational effort. For the same hardware configuration and number of processors, the  
319 required analysis time is reduced from approximately 25 minutes for the contour-based model (Fig. 2a) to  
320 approximately 90 seconds for the grid-based representation applied to the lower portion of the web (Fig. 2c).  
321 This reduction in runtime is critical for enabling repeated nonlinear analyses within the iterative optimization  
322 procedure.

## 323 4. Optimization Results and Repair Design Outcomes

324 While the preceding sections establish the computational framework used to derive optimized cold-  
325 spray repair geometries, the practical value of the proposed methodology lies in the structural behavior and  
326 efficiency of the resulting repair patterns. This section therefore focuses on the outcomes of the optimization  
327 process, examining how spatially varying thickness fields influence load-carrying capacity recovery, material  
328 efficiency, and governing failure mechanisms in a corroded steel girder. Results are presented for both  
329 Pareto-based and target-capacity formulations, allowing direct comparison between trade-off-driven and  
330 performance-driven repair strategies. Emphasis is placed on interpreting the resulting deposition patterns  
331 in terms of structural mechanics, load-path modification, and their relevance to bridge load-rating and  
332 rehabilitation decisions.

333 *4.1. Pareto-Optimal Repair Patterns and Trade-Offs*

334 Next the Pareto front optimization technique is applied to the corroded beam shown in Fig. 2, using the  
335 optimization domain indicated by the black rectangle in Fig. 6c. The size of this domain is consistent with  
336 the area requirements used for evaluating the residual capacity of corroded beams in the MassDOT Bridge  
337 Manual [36] and with previous studies by the authors [37]. Fig. 6e illustrates the application of a thickness  
338 increment  $\Delta t$  to an individual grid element for gradient evaluation, as described in Section 3.3.

339 Figure 6 summarizes the resulting deposition patterns, along with the corresponding capacities and  
340 efficiencies obtained for values of  $\alpha$  ranging from 0.0 to 0.8. Results for  $\alpha > 0.8$  are omitted, as the thickness  
341 distribution remains unchanged relative to the unrepaired geometry. For  $\alpha < 0.2$ , examination of the finite  
342 element model results indicates that the failure mode is governed by yielding at the crossbeam location, away  
343 from the corroded end. This behavior is reflected in Fig. 6a–b, where the beam capacity converges on the  
344 left side of each diagram and the additional load sustained due to the repair approaches zero for  $\alpha = 0.8$  in  
345 Fig. 6b.

346 In Fig. 6a, the dashed blue line denotes the nominal capacity of an intact beam. Although solutions  
347 with  $\alpha < 0.4$  exceed this baseline value, the most efficient repairs, defined as the ratio of recovered capacity  
348 to deposited material volume, occur for higher  $\alpha$  values, where the optimization emphasizes minimizing  
349 material use. For example, increasing the deposited volume by  $45 \text{ cm}^3$  when moving from  $\alpha = 0.3$  to  
350  $\alpha = 0.2$  yields only 26.9 kN of additional capacity, whereas adding just  $25 \text{ cm}^3$  at  $\alpha = 0.7$  results in a  
351 significantly larger increase of 189 kN.

352 The morphology of the corresponding cold spray deposition patterns is depicted in Fig. 6d, f, and h,  
353 showing respectively the deposited thickness, the total thickness, and the amount exceeding the nominal web  
354 thickness. As expected, the deposited volume increases progressively as  $\alpha$  decreases. Notably, the solutions  
355 corresponding to  $\alpha = 0.4, 0.6,$  and  $0.7$  share a consistent structural layout characterized by two prominent  
356 vertical reinforcement zones positioned near the beginning and midpoint of the optimization region, and  
357 extend along the height of the optimization domain. These zones function similarly to added stiffeners and  
358 contribute substantially to the recovered capacity. The configuration corresponding to  $\alpha = 0.6$  is shown in  
359 detail in Fig. 6g.

360 In contrast, the reinforcement patterns obtained for  $\alpha = 0.3$  and  $\alpha = 0.5$  follow a different strengthening

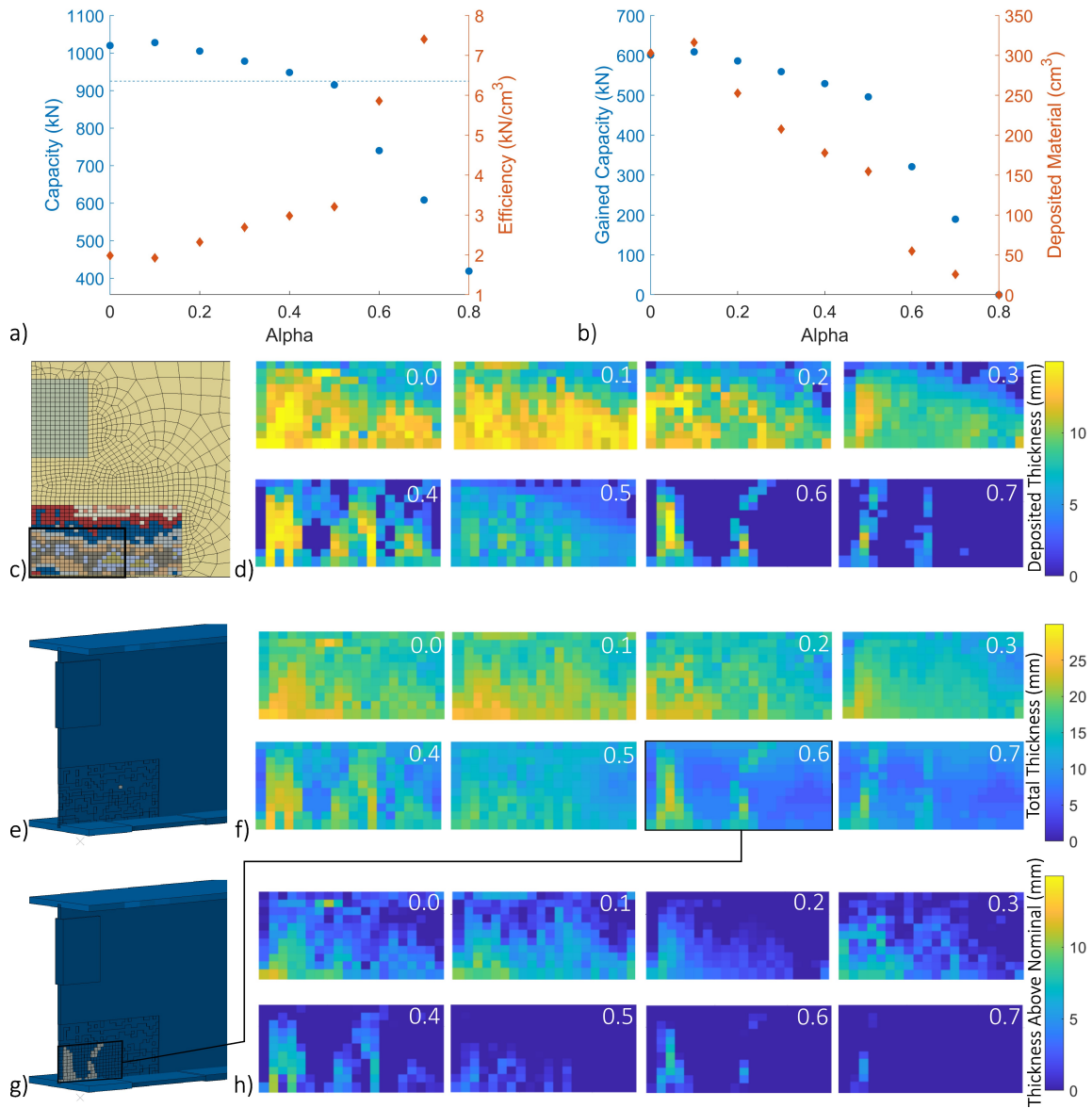


Figure 6: Results of the Pareto formulation for optimization of deposited reinforcement thickness. (a) Girder capacity versus efficiency and (b) recovered capacity versus deposited material for various  $\alpha$  values. (c) Optimization domain indicated by the black box. (d) Resulting deposition thickness fields and total deposited thickness along both sides, (f) resulting thickness distributions, and (h) regions where the thickness exceeds the nominal web value within the prescribed domain (per side). (e) In the gradient-descent optimization scheme, each element in the optimization space is assigned a thickness increment  $\Delta t$ , and its influence on the overall capacity is evaluated. (g) Finite element model corresponding to the optimal solution for  $\alpha = 0.6$ .

361 strategy, distributing material more uniformly across a larger portion of the optimization domain. This  
 362 distinction is particularly evident in Fig. 6h, where these solutions exceed the nominal web thickness over a  
 363 noticeably greater area compared to the other  $\alpha$  values.

364 The stopping criteria defined in Section 3.1 were intentionally selected to avoid overly restrictive con-  
 365 vergence requirements, allowing a consistent optimization framework across all values of  $\alpha$ . For each case,  
 366 a sufficiently large number of iterations was performed to generate multiple admissible solutions. The final  
 367 solution for each  $\alpha$  was selected as the one yielding the minimum value of the objective function among all  
 368 candidates. Figure 7 presents the evolution of capacity and deposited material, the gradient norm, and the  
 369 objective function value for the representative case of  $\alpha = 0.3$ . These results confirm stable convergence of  
 370 the optimization procedure.

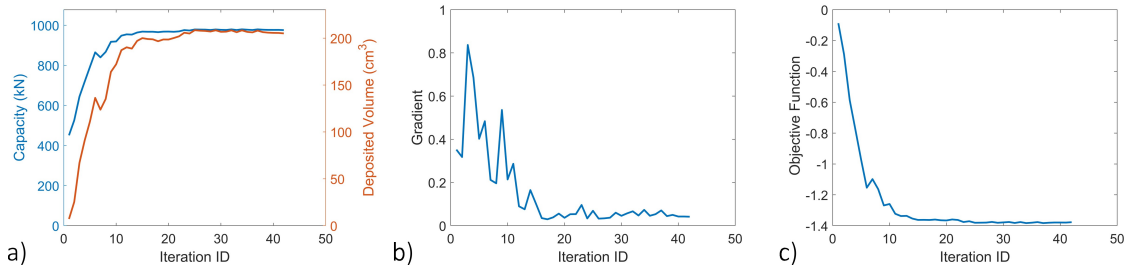


Figure 7: Convergence behavior of Pareto front optimization technique for  $\alpha = 0.3$ . a) Evolution of capacity and deposited material per iteration, b) gradient norm at the end of each iteration, and c) objective function value.

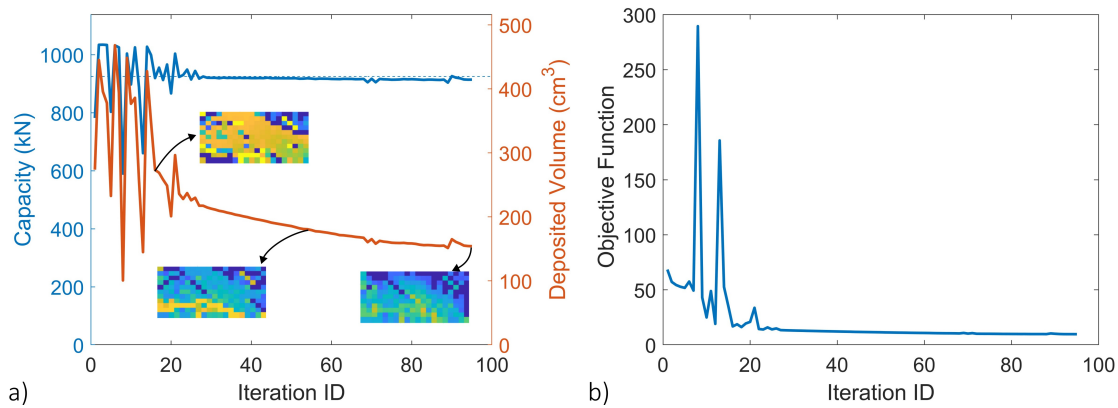


Figure 8: Penalty-based optimization results for complete capacity restoration. a) Iteration-by-iteration evolution of capacity, material deposition and three indicative repair scenarios, and b) objective function convergence.

#### 371 4.2. Target-Capacity Repair Design Using Penalty Optimization

372 Repair of the same corroded beam end is next modeled using the penalty-based formulation introduced  
373 in Section 3.2. In this case, the optimization is tasked with restoring the nominal capacity of the intact  
374 section, defined as  $L_{\text{goal}} = \text{Cap}_{\text{intact}}$ . Unlike the Pareto-based formulation, which explores trade-offs through  
375 the parameter  $\alpha$ , the penalty method enforces a direct capacity target and therefore yields a unique repair  
376 pattern. The penalty parameter  $\mu$  was selected empirically to ensure convergence to the target capacity.

377 Figure 8 illustrates the progressive evolution of predicted load capacity and deposited material with each  
378 iteration of the optimization process. A rapid initial increase in capacity is observed during the early iterations,  
379 as the optimizer identifies the most influential regions of the web and allocates material accordingly. During  
380 this phase, the violation of the capacity constraint ( $L_{\text{goal}} - L(\mathbf{t})$ ) is large, causing the penalty term in the  
381 objective function to dominate the gradient. As a result, material is preferentially added to regions exhibiting  
382 high sensitivity  $\partial L / \partial t_i$ .

383 As the target capacity is approached, the magnitude and direction of the gradient change significantly.  
384 The optimization gradually transitions from aggressively increasing local thickness to selectively refining the  
385 repair pattern by redistributing material toward regions with sustained structural influence. This transition is  
386 reflected in the curvature of the capacity and volume trajectories shown in Fig. 8. Once  $|L_{\text{goal}} - L(\mathbf{t}_k)|$  becomes  
387 sufficiently small, the gradient of the penalized objective is dominated by the volume term, discouraging  
388 further deposition unless it yields a meaningful capacity increase.

389 In contrast with the Pareto front formulation, an adaptive step-size update strategy is employed for the  
390 penalty-based optimization. The step size  $\eta_k$  is reduced from its initial value of 0.20 to 0.04 and subsequently  
391 to 0.01 in response to oscillations observed during the early iterations (Fig. 8b). This reduction dampens  
392 the iterative updates and facilitates smooth convergence as both the design variables and the gradient norm  
393 decrease below the prescribed thresholds.

394 The final repaired pattern produced by the penalty method (Fig. 8a) deviates from the vertical reinforce-  
395 ment zones solutions observed for several Pareto-optimal cases (e.g., for  $\alpha = 0.6$  or  $\alpha = 0.7$  in Fig. 6d) and  
396 instead resembles the more broadly distributed reinforcement associated with the  $\alpha = 0.5$  case. Notably, the  
397 total amount of deposited material for the penalty-based solution ( $154.19 \text{ cm}^3$ ) and for the  $\alpha = 0.5$  Pareto  
398 solution ( $154.66 \text{ cm}^3$ ) are nearly identical, and both achieve comparable capacities of 914 kN and 915 kN,

399 respectively. A visual comparison further indicates that the penalty-based repair applies material to fewer  
400 grid elements overall, yielding a more compact pattern despite the similar total deposited volume. The close  
401 agreement between these independently obtained solutions provides additional confidence in the robustness  
402 and credibility of the proposed optimization framework.

## 403 **5. Cold-Spray Deposition Architecture for Automated Repair Execution**

404 While manual cold-spray repair has been demonstrated on in-service bridges in the Commonwealth  
405 of Massachusetts [38], the execution of optimization-derived, spatially programmed deposition patterns  
406 demands a mechanically guided and computationally coordinated deposition architecture. This section  
407 introduces a robotic cold-spray deposition architecture developed to bridge optimized repair design and  
408 physical execution. This deposition architecture could be applied to many other cases of structural steel  
409 repair, and the upstream optimization, choice of materials, and other suitable constraints could be adjusted  
410 accordingly.

### 411 *5.1. Slicing and Path Planning*

412 A dedicated post-processing script was developed to convert the optimized repair thickness field into an  
413 ordered, layer-wise deposition path suitable for automated execution. The script retrieves the Abaqus input  
414 file from the final optimization iteration, parses the nodal and elemental data, and identifies all repaired  
415 element sets within the web region. For each repaired element, the original shell thickness, added repair  
416 thickness, and nodal coordinates are extracted directly from the corresponding shell section definitions.

417 Deposition parameters, including nominal deposition (bead) width and layer height ( $t_{\text{layer}}$ ), are specified  
418 based on the characteristics of the cold-spray equipment. To construct a continuous and kinematically feasible  
419 deposition sequence, element centroids are grouped according to their  $Z$ -coordinates, forming horizontal  
420 rows. When the bead width is smaller than the vertical spacing between adjacent element rows, linear  
421 interpolation is applied to enrich the coordinate set. Rows are processed sequentially from top to bottom or  
422 the opposite, with elements within each row ordered by increasing  $Y$ -coordinate. To reduce non-deposition  
423 travel and ensure continuous motion, every second row is traversed in reverse order (Fig. 9b-f), generating a  
424 serpentine (“snake-path”) trajectory.

425 Layer discretization is performed by subdividing the required deposited thickness using the user-defined  
 426 layer height  $t_{\text{layer}}$ . For each element,

$$n_i = \left\lceil \frac{t_{\text{side},i}}{t_{\text{layer}}} \right\rceil$$

427 layers are required, where  $t_{\text{side},i}$  denotes the total deposited thickness per side for element  $i$ . Each element  
 428 is included in layers  $L = 1, \dots, n_i$ . For each layer, the algorithm stores the ordered deposition coordinates,  
 429 element indices, remaining thickness, and cumulative path length.

430 The resulting hierarchical data structure, containing all deposition layers and their corresponding paths,  
 431 serves as direct input for generating machine-executable instructions for the automated deposition system.

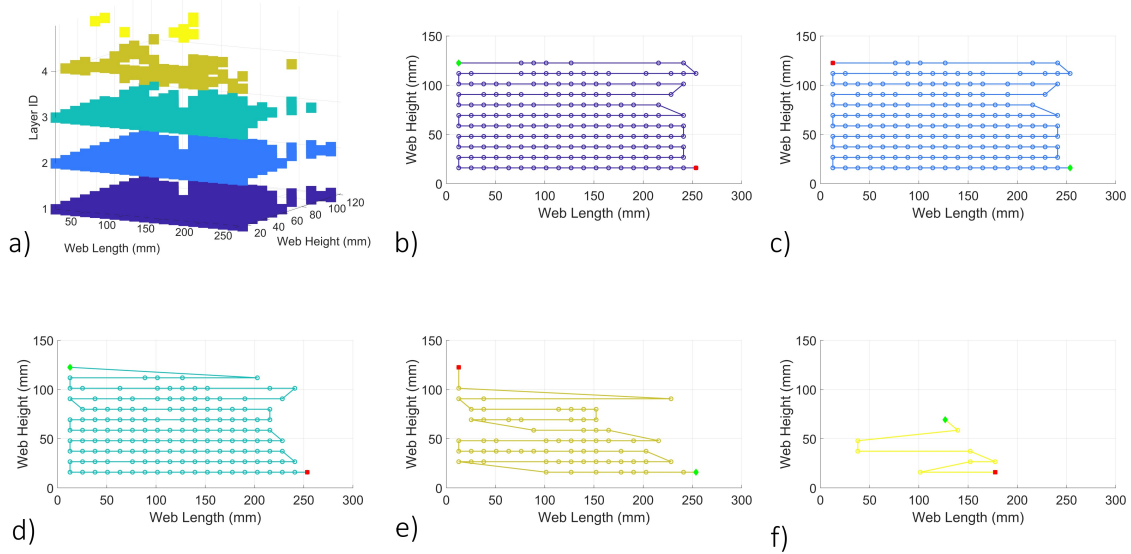


Figure 9: Conversion of optimized thickness fields into printing paths. (a) Indicative slicing of the optimal pattern obtained from the penalty method into five layers. (b–f) Illustration of the corresponding printing paths and generated machine-readable instructions. Markers along the paths indicate the locations of printable volumes, while the green and red colors denote the start and end points of each layer, respectively.

## 432 5.2. Functional Architecture and Design Constraints for Cold-Spray Repair

433 The design of a field-deployable cold-spray deposition system for bridge repair is governed by a combi-  
 434 nation of structural, geometric, and operational constraints that differ fundamentally from those encountered

435 in controlled manufacturing environments. Unlike conventional additive manufacturing systems, the depo-  
436 sition architecture must operate directly on existing steel girders, often in confined spaces, under variable  
437 environmental conditions, and with limited tolerance for misalignment or positional drift. These constraints  
438 strongly influence both the mechanical configuration of the system and the level of control required for  
439 reliable execution of optimized repair patterns.

440 A primary architectural requirement is the ability to establish and maintain accurate spatial registration  
441 between the deposition system and the corroded web region. Since optimized repair geometries are derived  
442 in a web-attached coordinate system, the deposition head must be positioned and actuated relative to the  
443 same reference frame, with consistent control of stand-off distance and nozzle orientation. This requirement  
444 places emphasis on rigid attachment to the girder and on minimizing compliance or vibration that could  
445 degrade positional accuracy during deposition.

446 Access constraints further shape the system architecture. Corrosion-driven section loss frequently initiates  
447 near the web-flange junction, necessitating unobstructed access to the full web height, including regions  
448 immediately adjacent to the bottom flange. The deposition system must therefore avoid geometric interference  
449 with the flange or surrounding structural components while still providing sufficient reach and maneuverability  
450 to execute spatially varying deposition paths.

451 Portability and deployability are equally critical considerations. To support practical use in bridge  
452 maintenance operations, the system must be sufficiently lightweight and compact to be transported and  
453 installed by a single operator, without reliance on cranes or specialized lifting equipment. Rapid attachment,  
454 detachment, and repositioning are essential for minimizing traffic disruption and enabling repairs at multiple  
455 locations along a structure. At the same time, the architecture must accommodate variability in girder  
456 geometry, particularly rolled I-shaped sections with depths representative of typical U.S. bridge construction.

457 Once installed, the system must provide a rigid and repeatable mechanical interface with the girder. The  
458 attachment mechanism must resist in-plane shear forces, out-of-plane bending moments, and dynamic loads  
459 induced by motion of the deposition head, ensuring that commanded trajectories remain consistent with the  
460 optimized repair maps. Any relative motion between the system and the substrate would directly translate  
461 into deposition errors and compromise the fidelity of the repair.

462 Finally, the architectural design must support robust operation in outdoor environments. Exposure to

463 moisture, temperature fluctuations, dust, and debris imposes additional demands on materials, actuation  
464 components, sensors, and electronics. The system must tolerate handling during transport and installation  
465 while maintaining reliable performance throughout the deposition process. Collectively, these constraints  
466 define the functional architecture of the proposed cold-spray repair system and motivate the mechanically  
467 simple, web-attached, and kinematically constrained design introduced in the following subsection.

### 468 *5.3. Geometry and Mechanical Configuration*

469 The proposed system, illustrated in Fig. 10a, consists of a rigid rectangular frame mounted directly onto  
470 the steel web. The frame dimensions are selected to accommodate beam depths between 50 cm and 91 cm,  
471 thereby covering the majority of rolled I-sections used in U.S. bridge construction. The two vertical members  
472 extend below the deposition mechanism, enabling unobstructed access to the web-flange junction where  
473 corrosion commonly initiates.

474 A cantilevered horizontal carriage rail is mounted on the frame and supports lateral translation of the  
475 deposition head. Positioned outboard of the web plane, this rail provides clearance from the magnetic  
476 attachment housings and ensures a consistent stand-off distance throughout the deposition process. This  
477 configuration minimizes mechanical complexity while maintaining access to the full height of the repair  
478 region.

479 The mechanical architecture provides three controlled degrees of freedom:

- 480 1. **Horizontal translation of the deposition head**, defining the primary raster direction for material  
481 placement;
- 482 2. **Vertical translation of the carriage rail**, enabling layer-wise advancement along the web height;
- 483 3. **In-plane stand-off adjustment**, achieved through controlled translation of the frame normal to the  
484 web plane to compensate for deposited material buildup.

485 This configuration supplies the minimum kinematic capability required for layer-by-layer additive de-  
486 position while avoiding the mass, complexity, and vibration sensitivity associated with multi-axis robotic  
487 arms. The frame is secured to the web using four magnetic attachment points. A preliminary sizing study  
488 accounting for operational loads and an assumed 0.1 mm protective coating on the web indicated that a

489 holding force of approximately 800 N per magnet is required. Suitable commercial magnets meeting these  
490 specifications are readily available in compact form factors.

491 During installation, a diagonal activation sequence is employed: the upper-left and lower-right magnets  
492 are engaged first to constrain rotation and in-plane translation, followed by activation of the remaining two  
493 magnets to fully lock the frame. Integrated bubble levels on the horizontal and vertical members allow  
494 rapid verification of alignment within the web-attached coordinate system, ensuring consistency between  
495 commanded deposition paths and finite element–derived repair maps.

#### 496 *5.4. Virtual System Development and Virtual Twin*

497 Following the conceptual mechanical design, a digital representation of the cold spray architecture system  
498 was developed in MATLAB/Simulink using a model-based systems engineering approach. The resulting  
499 virtual twin reproduces the kinematic behavior of the moving components and enables simulation of the  
500 additive repair process under realistic geometric and operational constraints.

501 The Simulink environment includes an integrated interface allowing the user to select the girder type from  
502 a predefined library of commonly used beam sections (Fig. 10g). After girder selection, the user specifies  
503 the initial placement of the deposition head by defining global  $x$  and  $y$  offsets, analogous to registering the  
504 system at the upper-left corner of the repair region during field installation (Fig. 10a). Additional parameters  
505 allow adaptation of system characteristics based on geometric configuration and design requirements.

506 To simulate deposition, the relationship between deposition-head velocity, stand-off distance, and re-  
507 sulting bead geometry (width and height) is prescribed. Using these parameters in combination with the  
508 previously generated deposition paths, the virtual twin executes a full kinematic simulation of the repair  
509 process. The simulation animates the system motion in real time, visualizing each controlled degree of  
510 freedom as well as the activation sequence of the deposition process (Fig. 10b–f).

511 The developed digital environment is modular and supports conceptual, preliminary, and detailed system  
512 design. It enables rapid evaluation of alternative geometries, kinematic configurations, and control strategies.  
513 Furthermore, the modular structure allows future integration with a physical system: binary signals such  
514 as deposition activation, sensor feedback, and limit-switch states can be directly interfaced with Simulink  
515 blocks, providing a foundation for closed-loop control and real-time execution of automated additive repairs.

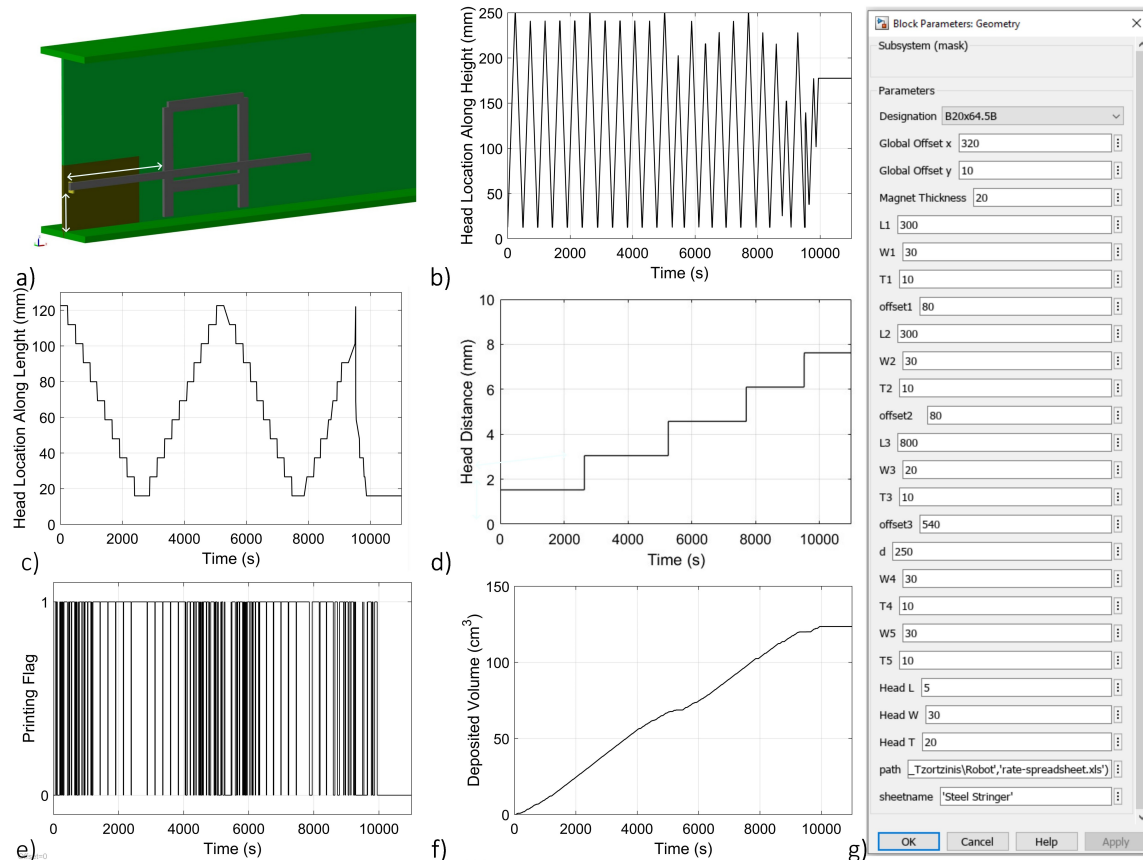


Figure 10: Robotic deposition architecture. (a) Conceptual design and virtual operation of a field-deployable robotic deposition architecture. (b–d) Simulated print-head motion along the three axes. (e) Printing-activation signal and (f) evolution of deposited volume during printer operation. (g) The developed digital environment, which integrates beam geometries from a built-in library, offset definitions for registering the printer to a global coordinate system, and modular geometric characteristics for flexible configuration.

516 In addition, variations in positioning and actual deposition thickness can be fed back to the finite element  
 517 simulation routine, along with actual post-repair scan data, to enable virtual and on-site qualification of the  
 518 repair outcomes.

## 519 6. Discussion and Future Work

520 The methodology and results presented here represent a fundamental shift in how corrosion-induced  
 521 material loss in steel bridge girders, and other structures, can be assessed and repaired. Conventional repair  
 522 strategies rely heavily on manual surface preparation, including abrasive cleaning, removal of delaminated

523 steel, and application of protective coatings prior to the installation of welded or bolted reinforcement. These  
524 operations are labor-intensive, time-consuming, and often dominate the overall repair cost. In contrast,  
525 the cold-spray additive manufacturing process inherently cleans the substrate through high-velocity particle  
526 impact, which mechanically cleans and activates the steel surface during deposition. This characteristic  
527 suggests the feasibility of integrating a dedicated surface-conditioning or pre-cleaning pass directly within  
528 the automated deposition sequence, thereby reducing the need for extensive manual preparation. Given that  
529 surface cleaning is frequently among the most costly components of steel bridge repair operations, such  
530 integration has the potential to significantly improve both economic and operational efficiency.

531 A key contribution of this work is the high degree of automation achieved across the entire digital repair  
532 workflow. Each stage—laser-based corrosion mapping, structured thickness-field generation, finite element  
533 modeling, optimization, deposition-path planning, and virtual execution—is implemented using custom-  
534 developed algorithmic tools designed for seamless data exchange. By minimizing manual data handling  
535 and subjective interpretation, the workflow enables consistent and repeatable generation of repair strategies  
536 directly from measured deterioration states. This level of integration establishes a unified digital environment  
537 in which inspection data, structural analysis, and repair execution are coherently linked.

538 Future work will focus on experimentally validating and refining the material-deposition parameters  
539 that govern the physical execution of the optimized repairs. In particular, systematic testing is required to  
540 quantify the relationships among deposition-head velocity, stand-off distance, and resulting bead geometry.  
541 These experimentally derived relationships will provide the necessary inputs for the slicing algorithm and  
542 the virtual system model, enabling more accurate prediction of deposited geometries. In parallel, fabrication  
543 of the full-scale deposition system will allow laboratory validation of kinematics, attachment mechanisms,  
544 and deposition accuracy, followed by controlled field trials on representative steel girder segments.

545 The proposed workflow aligns closely with the principles of Industry 4.0 through its integration of  
546 cyber-physical systems and data-driven decision-making. The developed virtual twin provides a foundation  
547 for future coupling with the physical deposition system, enabling simulation, optimization, and execution  
548 within a unified control architecture. Through structured data exchange among sensing, computation, and  
549 actuation modules, the framework supports informed decisions regarding repair extent, deposition strategy,  
550 and expected structural performance. Such tightly integrated systems are central to emerging paradigms in

551 automated infrastructure maintenance.

552 Beyond the specific application to steel bridge girders, the methodology developed in this study has  
553 broader applicability to other corrosion-prone infrastructure systems. Maritime and offshore structures, in  
554 particular, experience localized material loss under constrained access conditions and harsh environments,  
555 making automated surface-conditioning and additive repair technologies especially attractive. By adapting  
556 the scanning strategy, geometric parameterization, and deposition hardware to different structural forms, the  
557 same detection, quantification, optimization, and repair pipeline could enable safer, more precise, and more  
558 efficient maintenance across multiple industrial sectors.

## 559 **7. Conclusions**

560 The main contributions and conclusions are summarized as follows:

- 561 • A structured grid-based representation of corrosion was shown to provide accurate prediction of  
562 residual beam structural capacity while significantly reducing model complexity and computational  
563 cost, enabling iterative optimization analyses.
- 564 • A gradient-based optimization framework was developed to identify material-efficient reinforcement  
565 patterns. Pareto-front solutions revealed distinct strengthening strategies that balance added material  
566 volume and recovered load-carrying capacity.
- 567 • A penalty-based optimization formulation successfully achieved prescribed target capacities relevant  
568 to bridge load rating, producing repair patterns consistent with Pareto-optimal solutions and demon-  
569 strating the robustness of the computational approach.
- 570 • A fully integrated digital workflow was established, spanning laser scanning, corrosion mapping,  
571 finite element modeling, optimization, deposition-path planning, and virtual execution, with minimal  
572 reliance on manual intervention.
- 573 • A conceptual cold spray architecture and its virtual twin were developed to translate optimized depo-  
574 sition fields into machine-executable repair actions under realistic field constraints.

575 • The overall methodology aligns with Industry 4.0 principles through the coupling of cyber–physical  
576 systems, digital twins, and data-driven decision-making for automated infrastructure maintenance.

577 While demonstrated for steel bridge girders, the proposed framework is readily adaptable to other  
578 corrosion-prone infrastructure systems, including maritime and offshore structures, offering an action-  
579 able pathway toward precise, automated, resource-efficient, and data-informed repair technologies.

## 580 **8. Data Statement**

581 Selected data are available from the corresponding author upon reasonable request.

## 582 **9. Author Contributions**

583 Georgios Tzortzinis: Conceptualization, Formal analysis, Investigation, Methodology, Visualization,  
584 Software, Writing – original draft. Kaushik Abhyankar: Software, Methodology. Bruno Guilherme Christoff:  
585 Methodology. Brian Schagen: Investigation. A. John Hart: Writing – review and editing. Simos Gerasimidis:  
586 Writing – review and editing, Investigation. Maik Gude: Writing – review and editing.

587

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